Basics of Smith Charts

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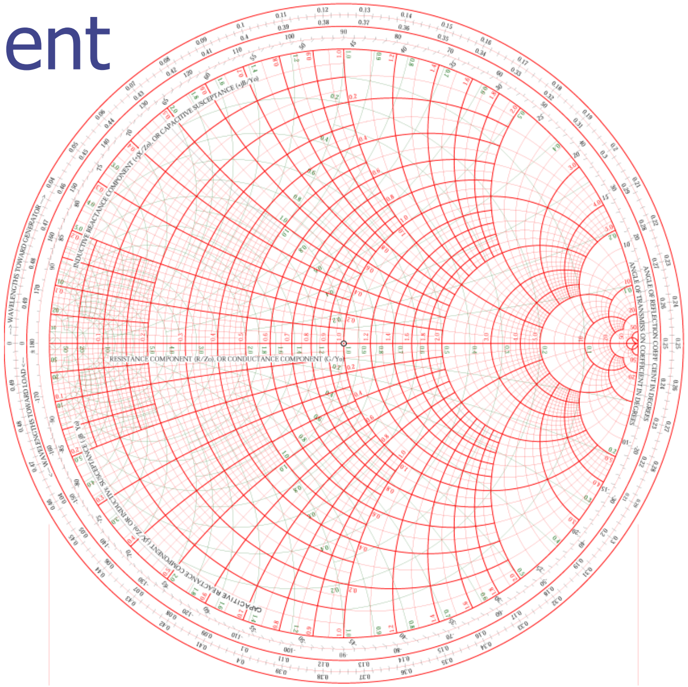
What is a Smith Chart

- A graphical tool to plot and compute:
  - Complex impedance
  - Complex reflection coefficient
  - VSWR
  - Transmission line effects
  - Matching networks
  - …and more
- Let's break it down….



Normalized Impedance

- Normalized Z = Actual Z / System Z_0
  - For Z_0=50Ω, divide values by 50
- Example:
  - $Z = 37 + j55$
  - $Z' = \frac{37}{50} + j\frac{55}{50}$
  - $Z' = 0.74 + j1.10$

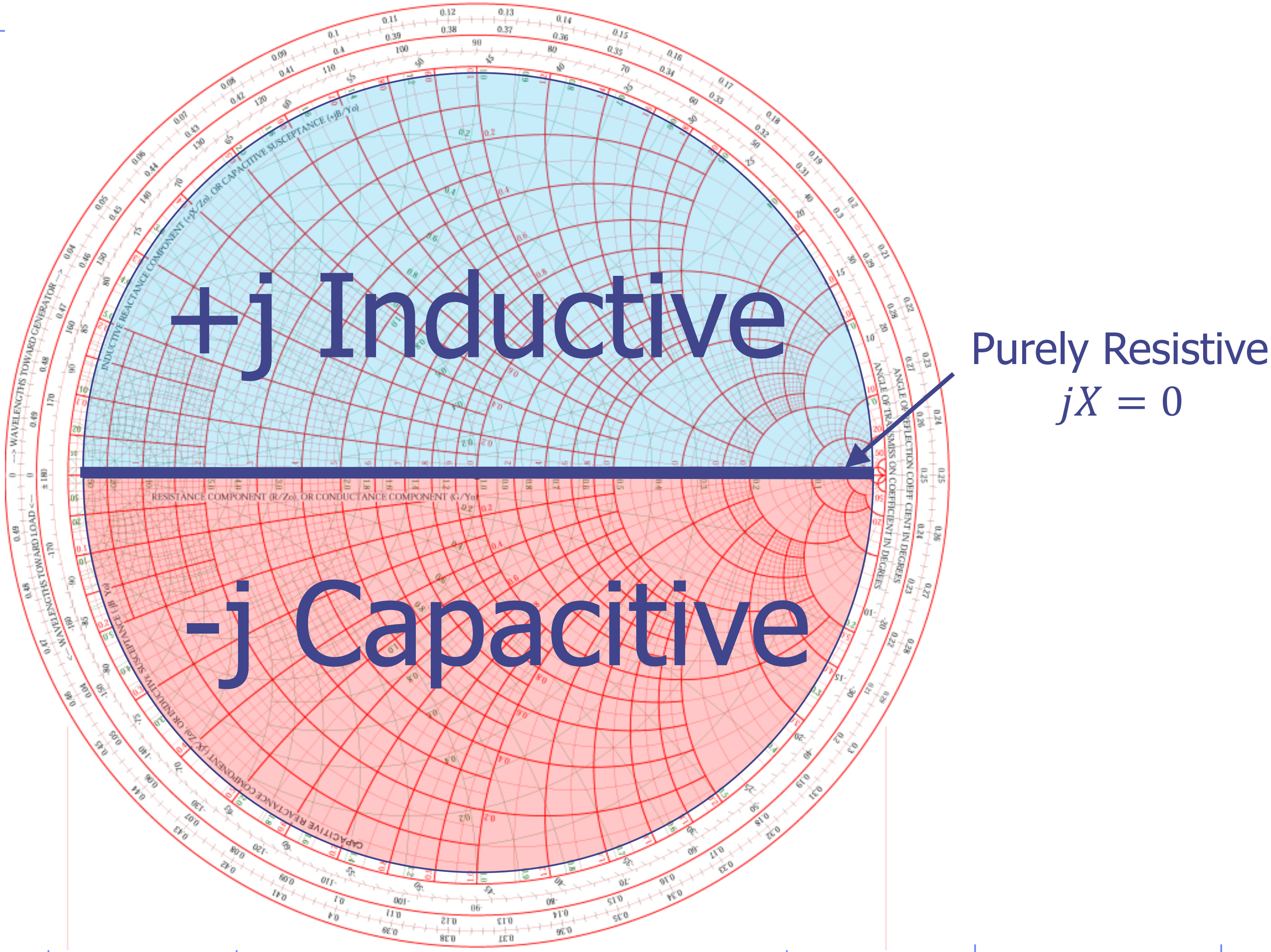
This is what we plot on the chart

- **Makes it usable for any system Z_0**

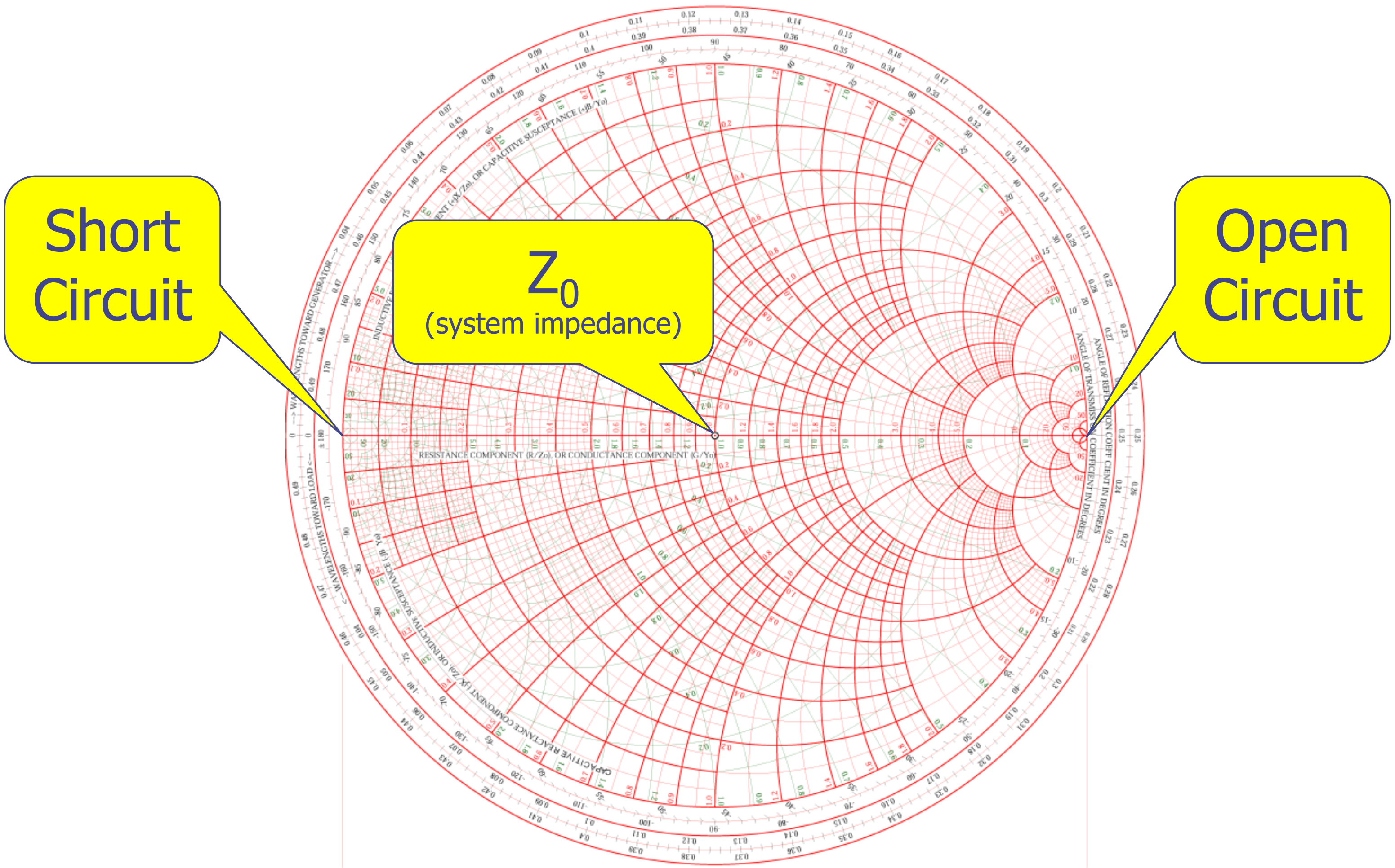
Z Regions on the Smith Chart

$R + jX$

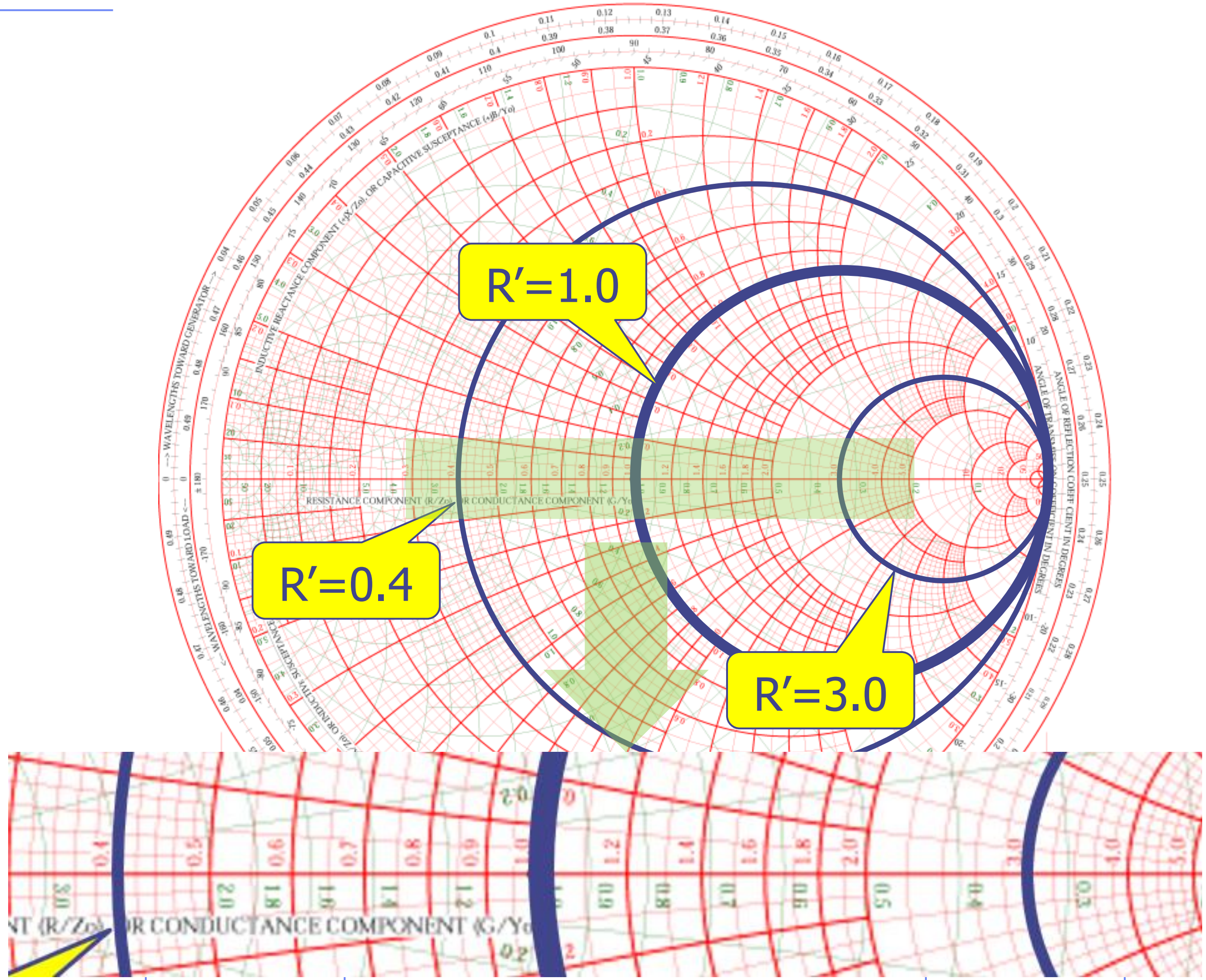
$R - jX$



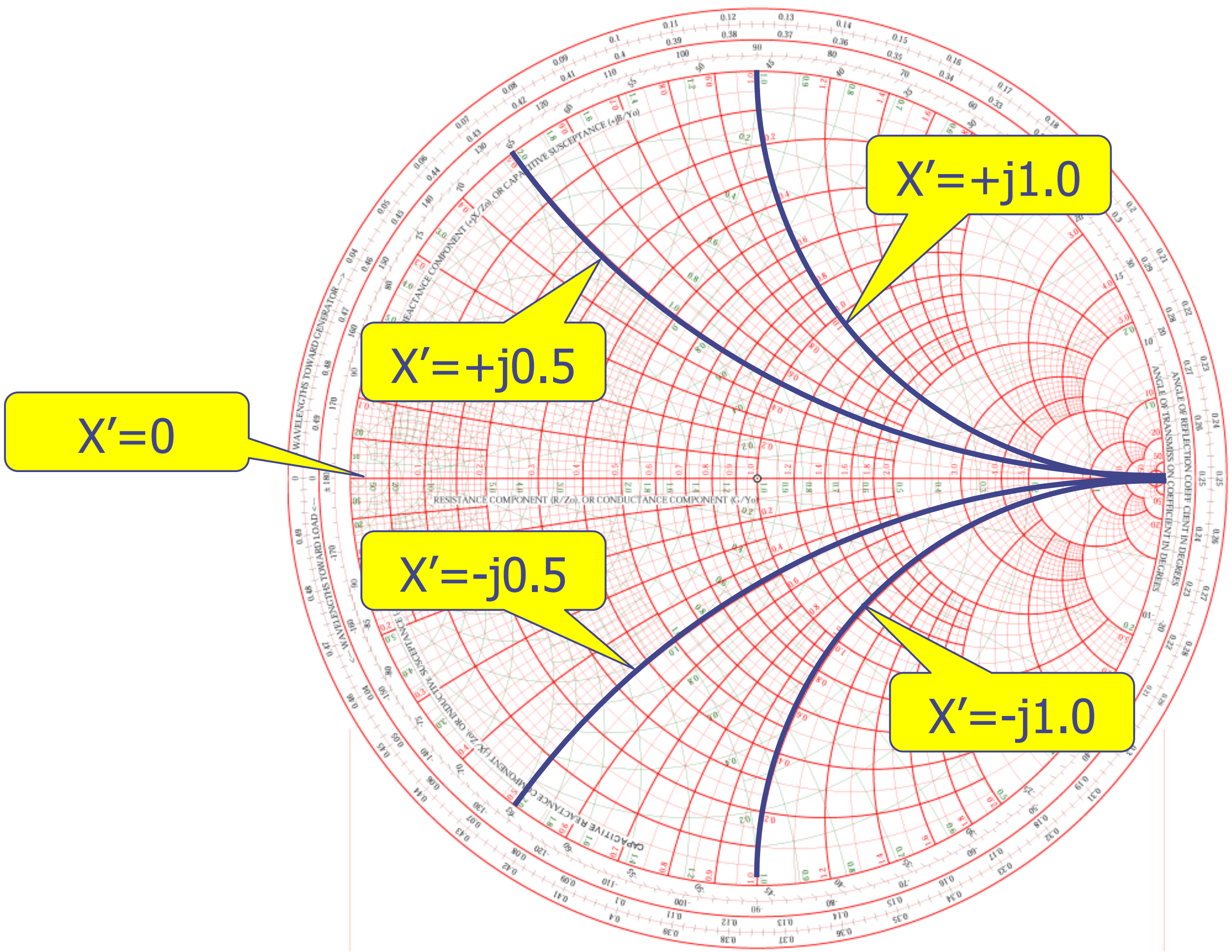
Key Values on the chart



Constant Resistance Circles

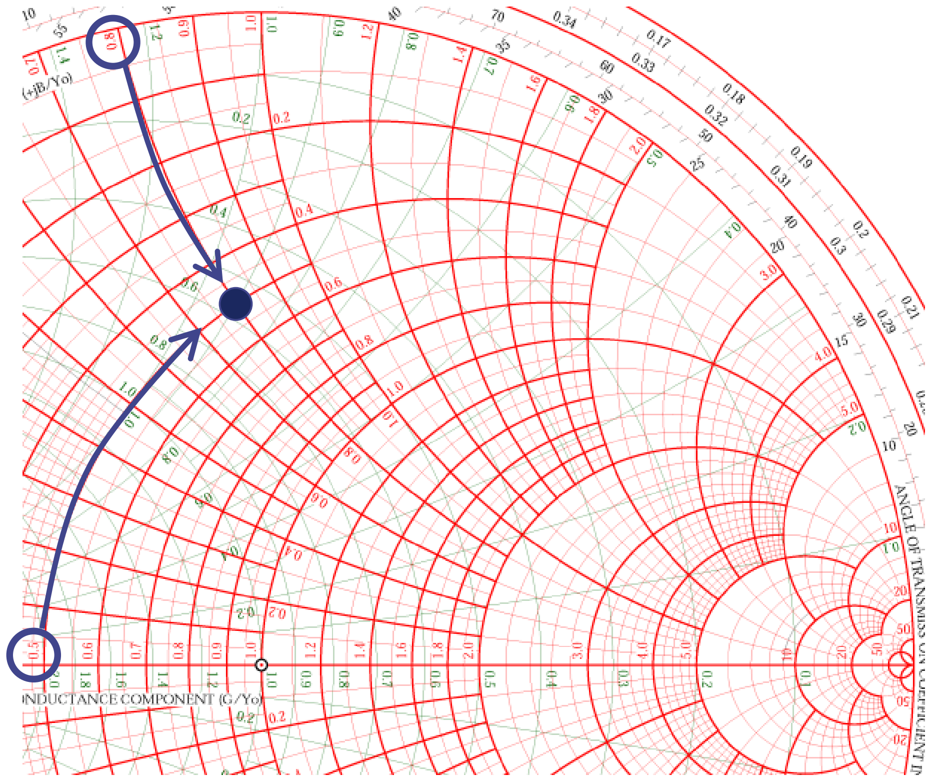


Constant Reactance 'Arcs'



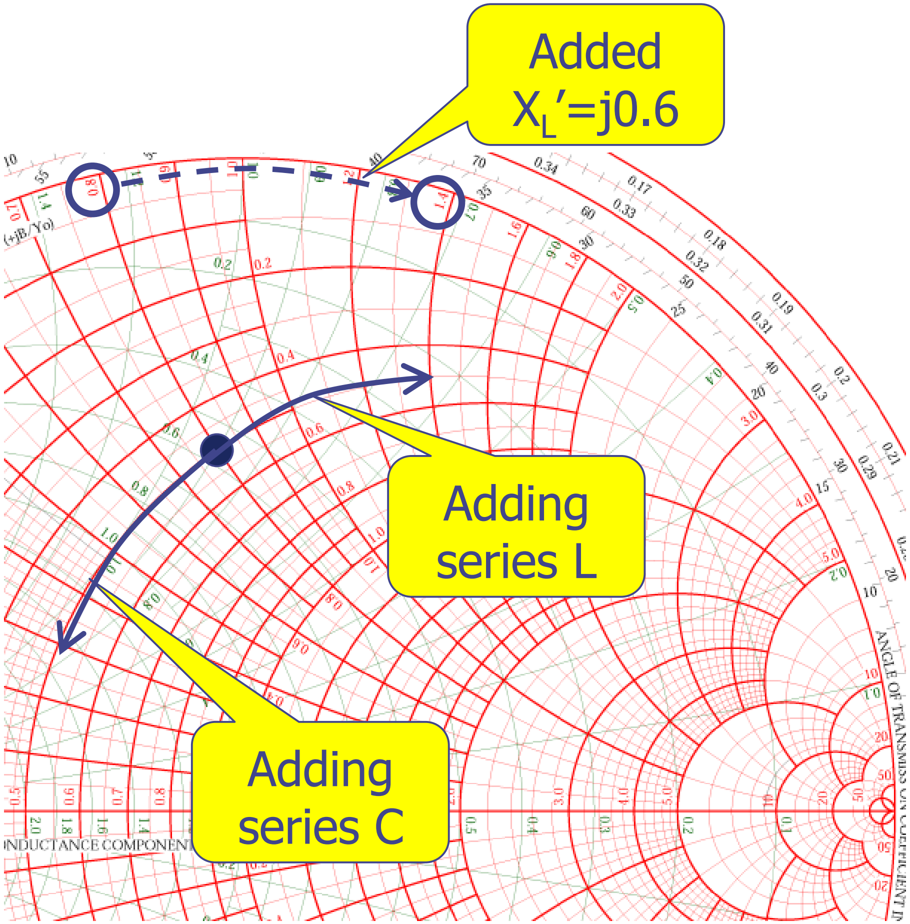
Plot a Complex Impedance

- $Z = 25 + j40$
- Divide by 50 to normalize…
- $Z' = 0.5 + j0.8$
- Find intersection of R′=0.5 circle and X′=0.8 arc



Adding Series Elements

- Add components to move around the Smith Chart
- Series L & C move along constant-R circles
  - Series L moves CW
  - Series C moves CCW



What about Admittance?

- Admittance is handy when adding elements in parallel
- Converting Impedance to Admittance is easy with Smith Chart

$$Admittance: Y = \frac{1}{Z}$$

$$Conductance: G = \frac{1}{R}\ ^{*}$$

$$Susceptance: B = \frac{1}{X}\ ^{*}$$

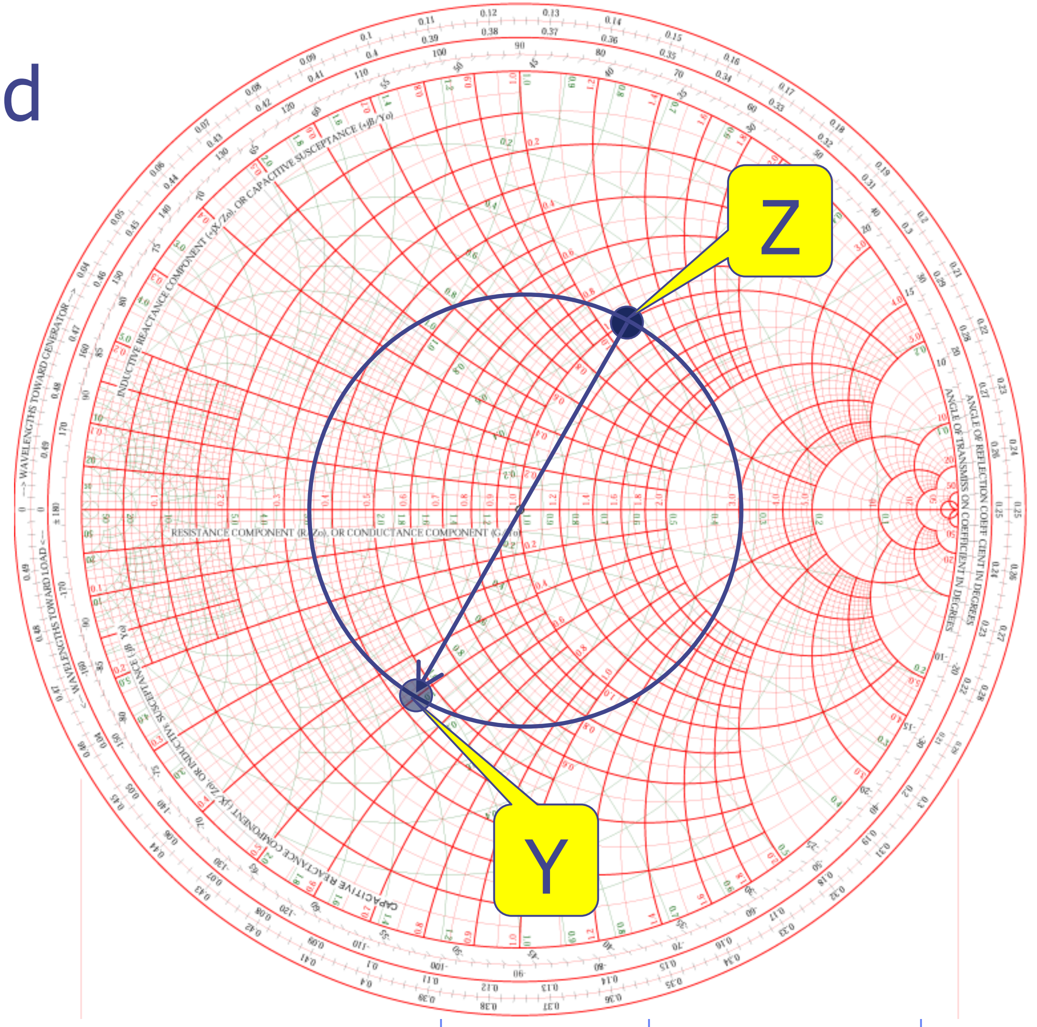
* (when "real" component = 0)

Converting to Admittance

- Draw circle centered on Z_0 that crosses through Z point
- Bisect circle thru Z and Z_0
- Y is 180° away on circle

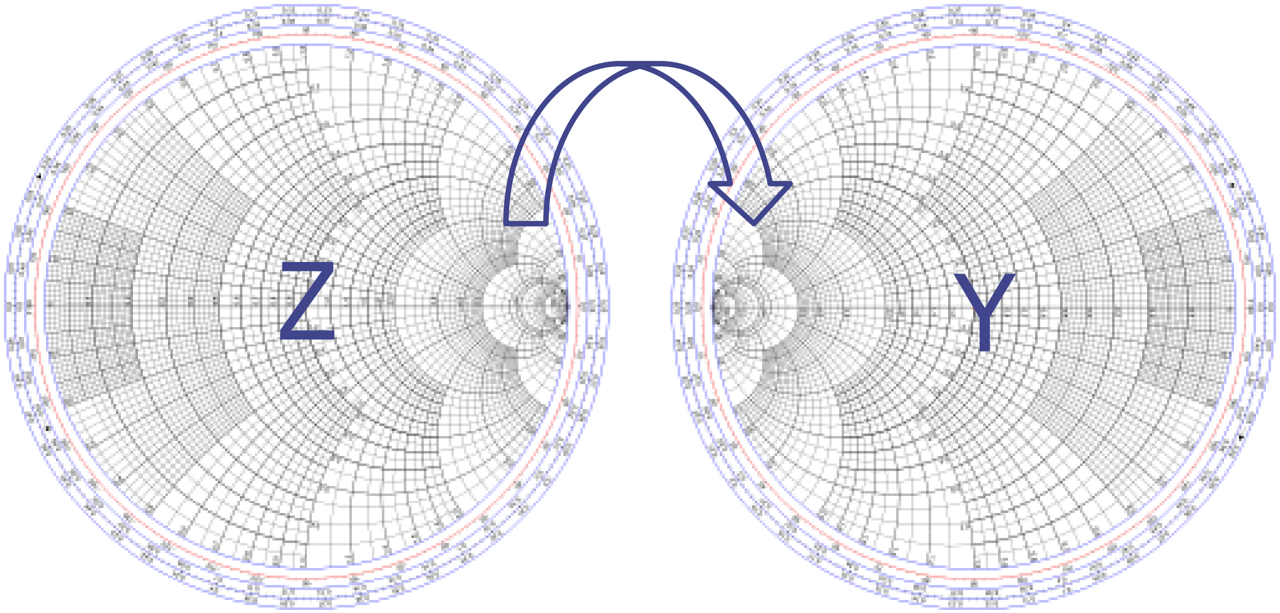
$$Z' = 1 + j1.1$$

$$Y' = 0.45 - j0.5$$



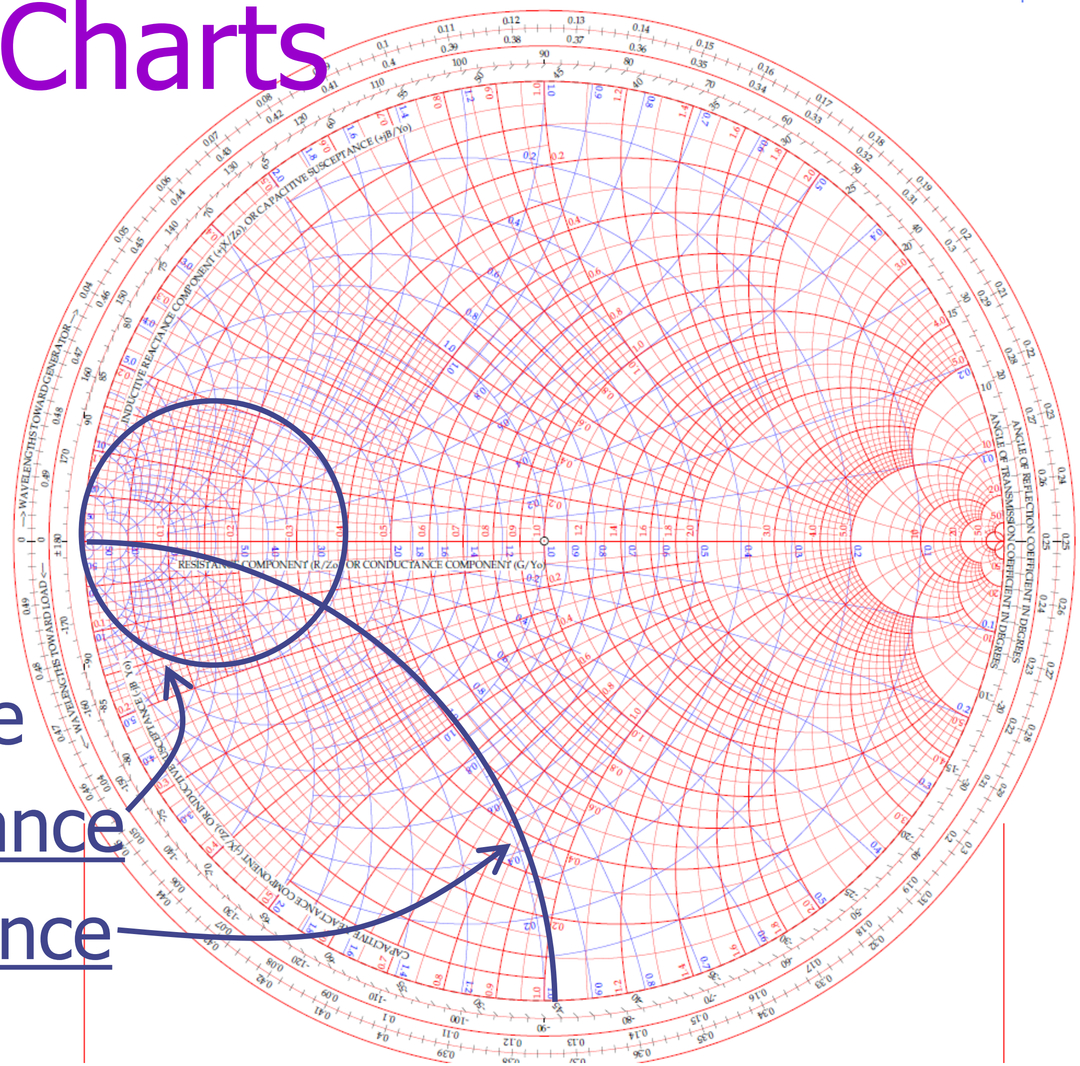
Admittance Curves

Admittance Curves are obtained by simply rotating the Smith Chart by 180°



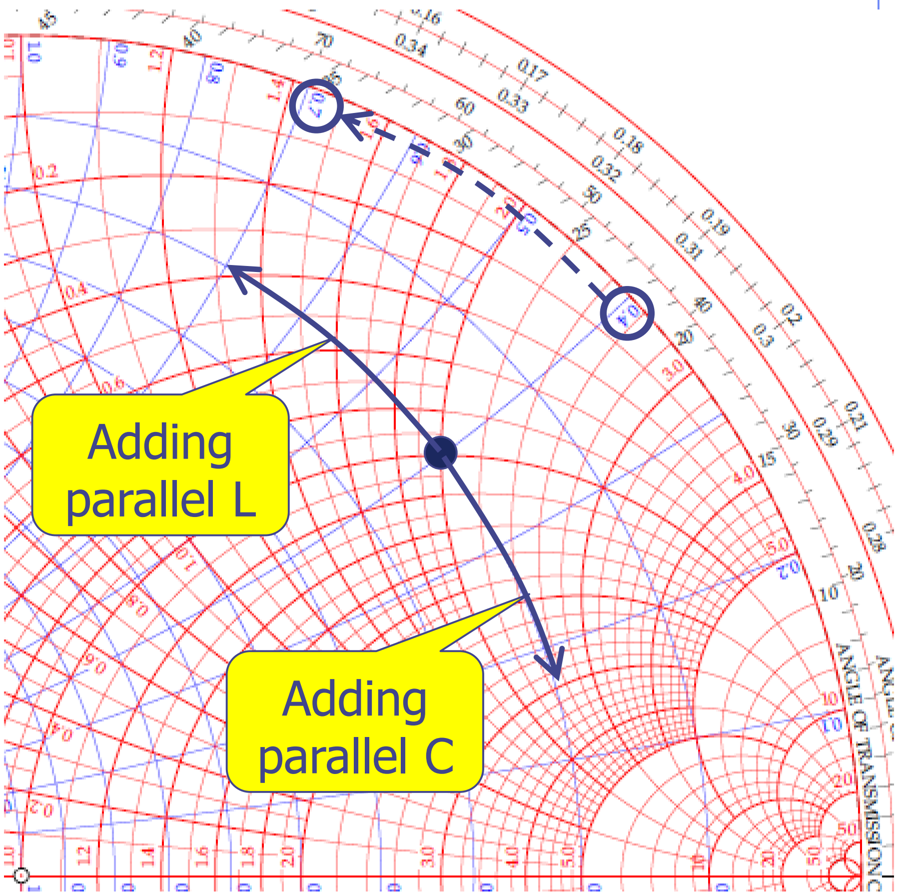
Combination Charts

- Look carefully – Admittance curves are here!
- Both **Z-only** and **combo** charts are available
- Constant <u>Conductance</u>
- Constant <u>Susceptance</u>



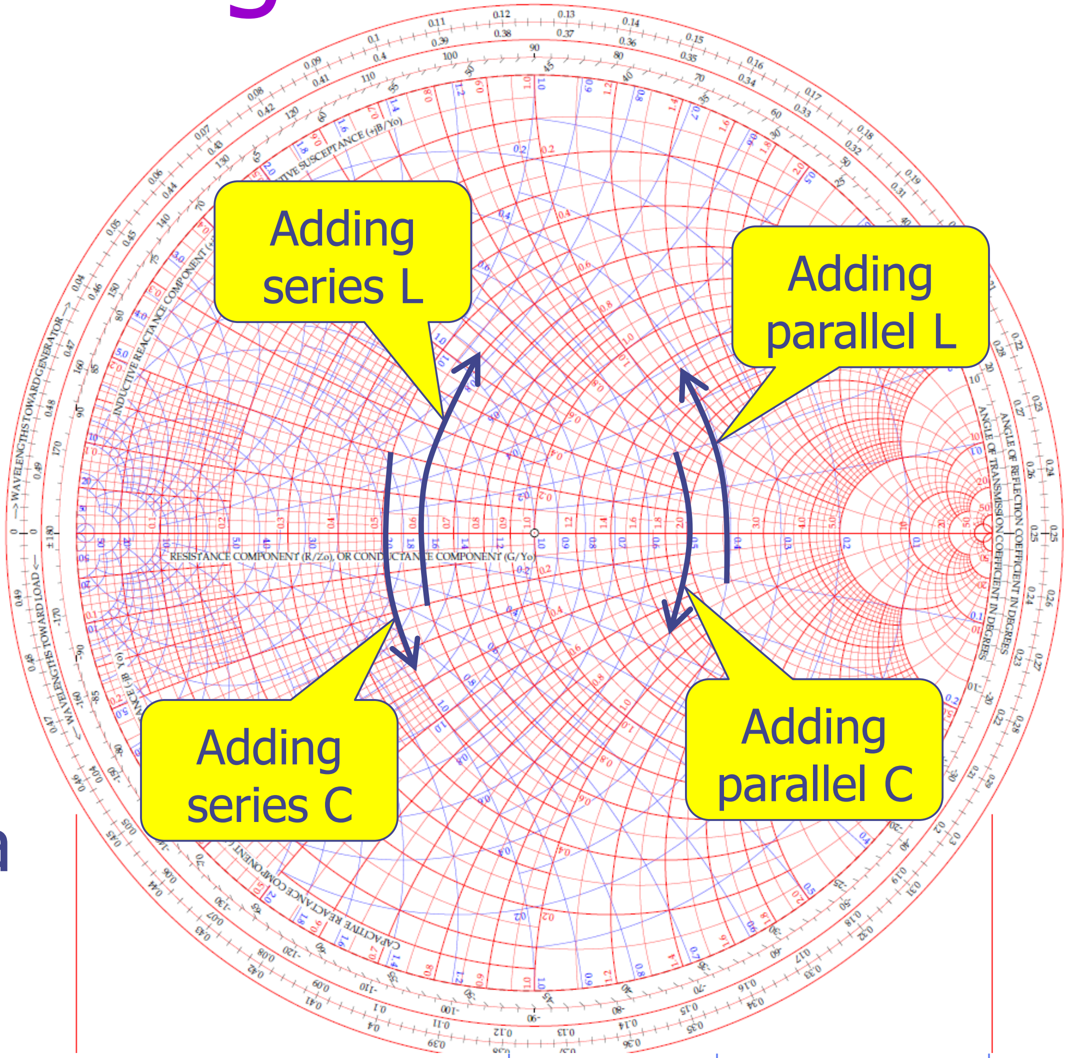
Adding elements in parallel

- Adding parallel or shunt L & C moves along constant conductance circles
- Easiest to do with "combo" Smith Chart
  - Shunt L with $B'_L = j0.3$ is shown



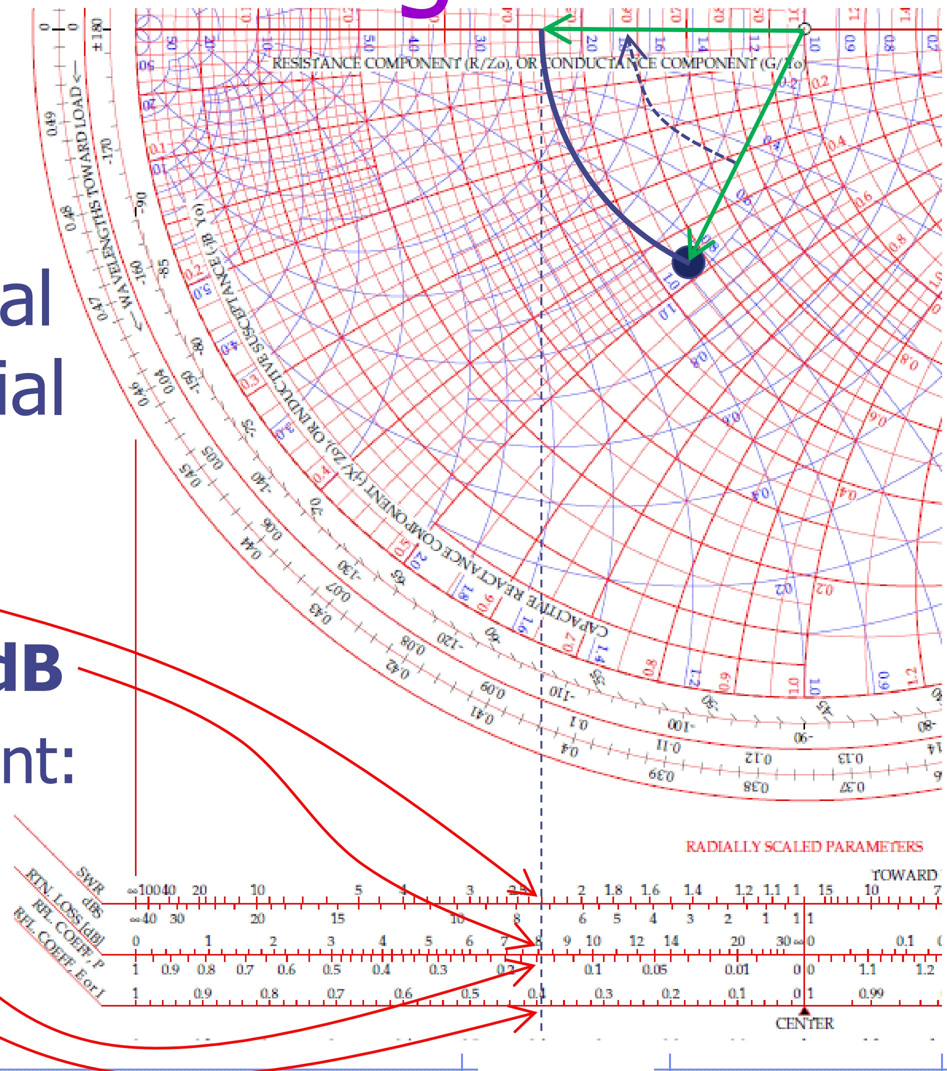
Quick tip – adding elements

- Adding inductors "eLevate" thru real axis
- Adding capacitors "Crash" down thru real axis
- Remember this when we design a matching circuit!



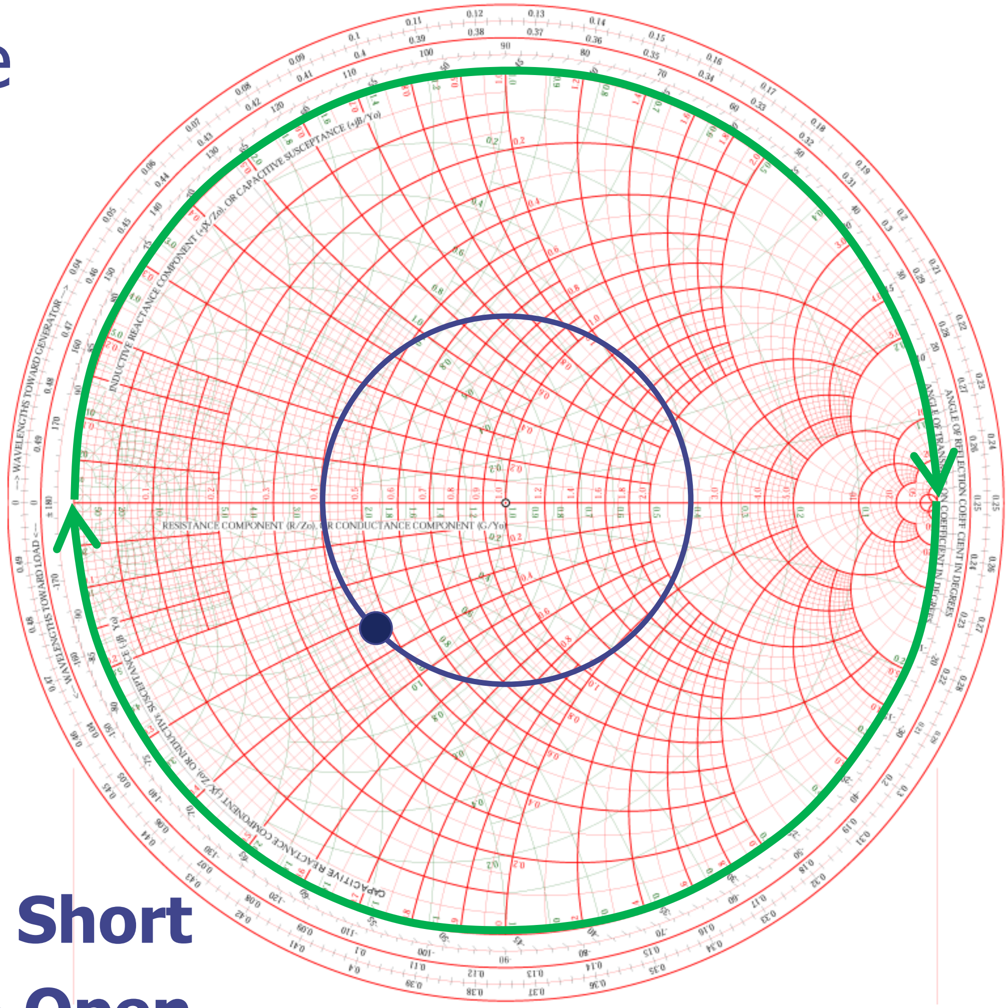
More Smith Chart Magic

- **Radially Scaled Parameters**
- Rotate vector to real axis, extend to radial scales:
  - VSWR: **2.3:1**
  - Return Loss: **8.10dB**
  - Reflection Coefficient: Power: **0.155** V or I: **0.39**



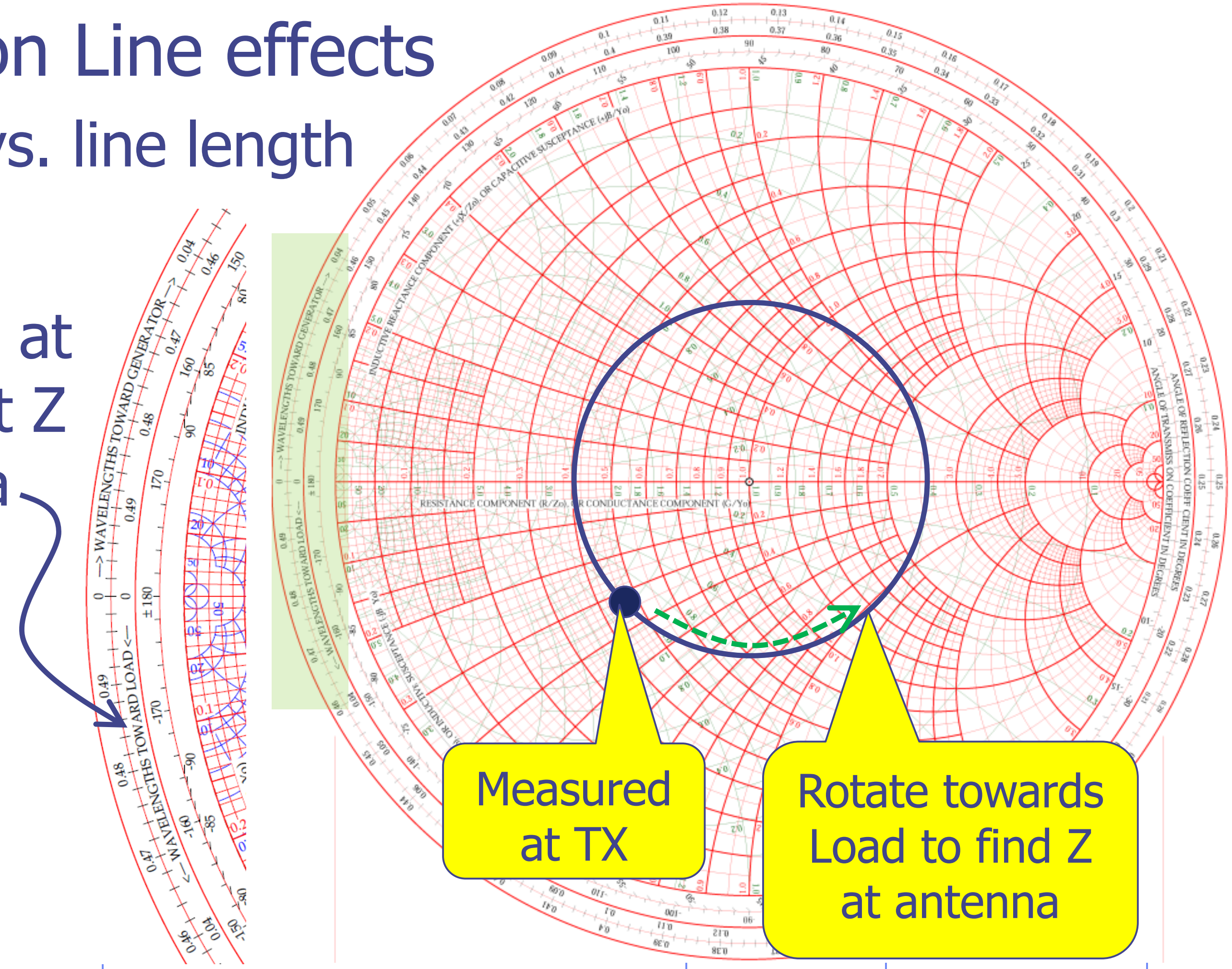
VSWR and Transmission Lines

- Constant VSWR circle
  - Impedance varies
  - VSWR stays same
- One trip around Smith chart is ½ wavelength
  - Impedance **repeats**
- Half-way around is ¼ wavelength:
  - **Open** transformed to **Short**
  - **Short** transformed to **Open**



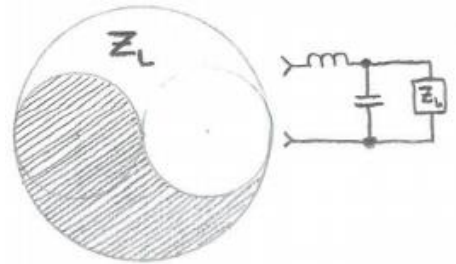
VSWR and Transmission Lines

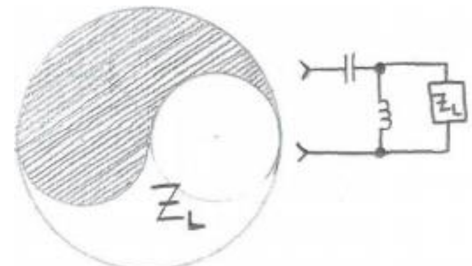
- Transmission Line effects
  - Predict Z vs. line length
- Example:
  - Measure Z at TX, predict Z at antenna

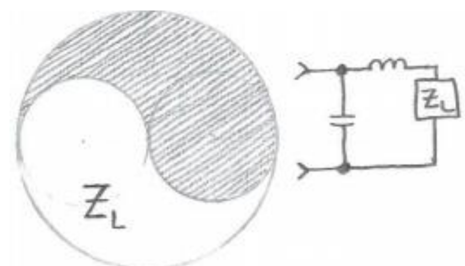


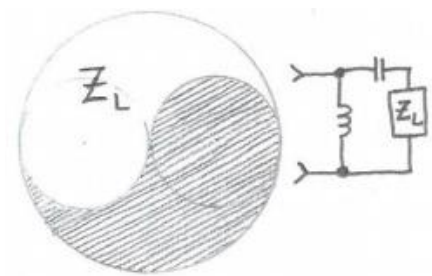
Impedance Matching: L-Network

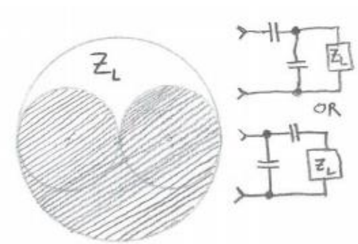
- Add series/parallel inductor/capacitor to move Z_L to Z_0
- L-Network topology based on where Z_L is on the Smith Chart
- Sometimes more than one network topology works

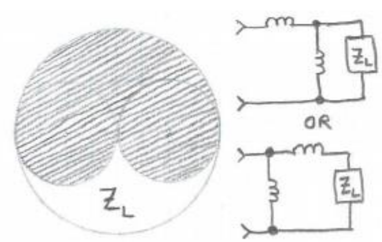






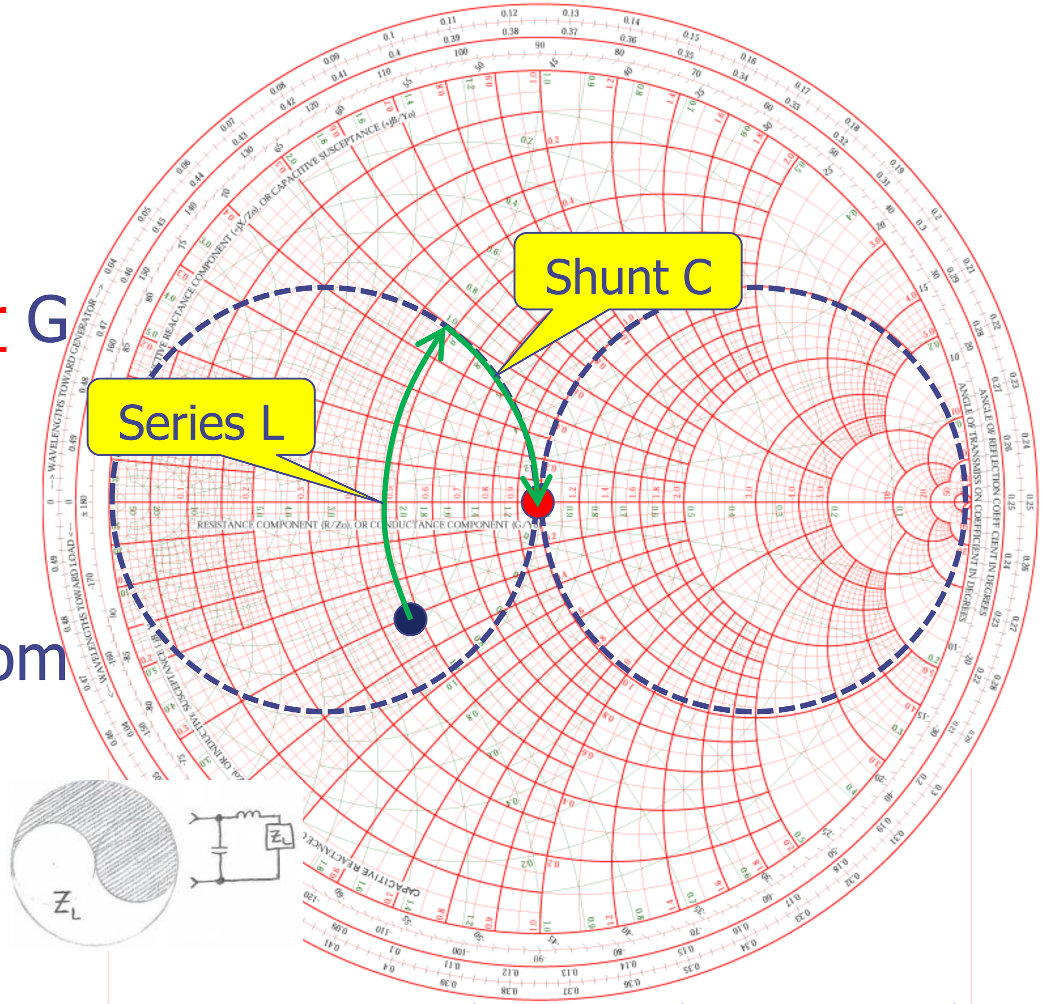






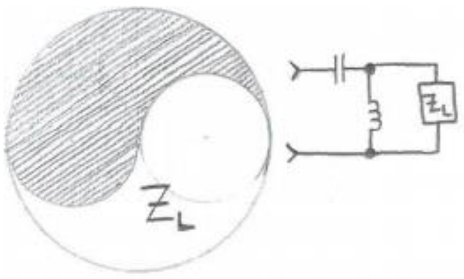
L-Network Design Process

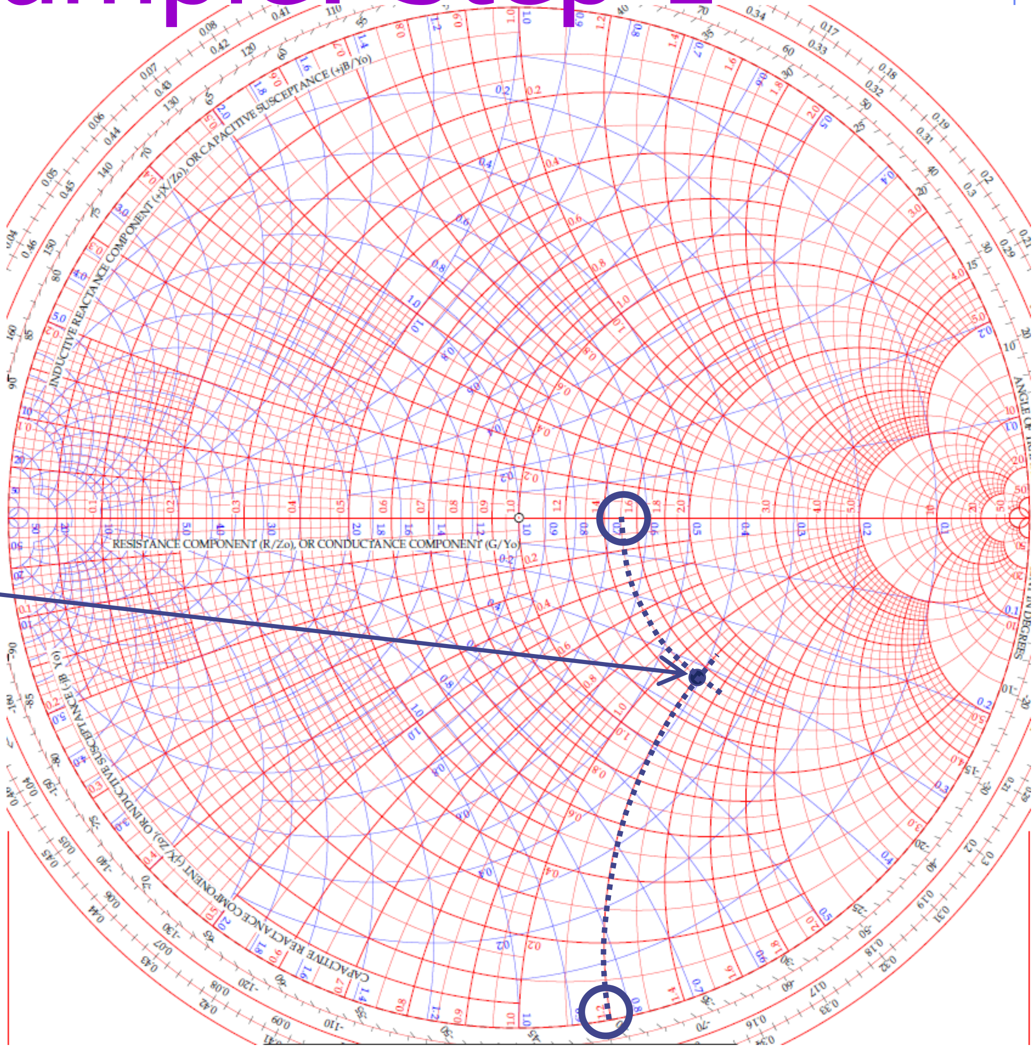
- Pick a topology
- Process:
  - Add ser/par L/C to rotate to unity R or G circle
  - Add ser/par L/C to rotate to Z_0
  - Compute values from $\Delta X'$ and $\Delta B'$
- Example:
  - Series L, shunt C



L-Network Example: Step 1

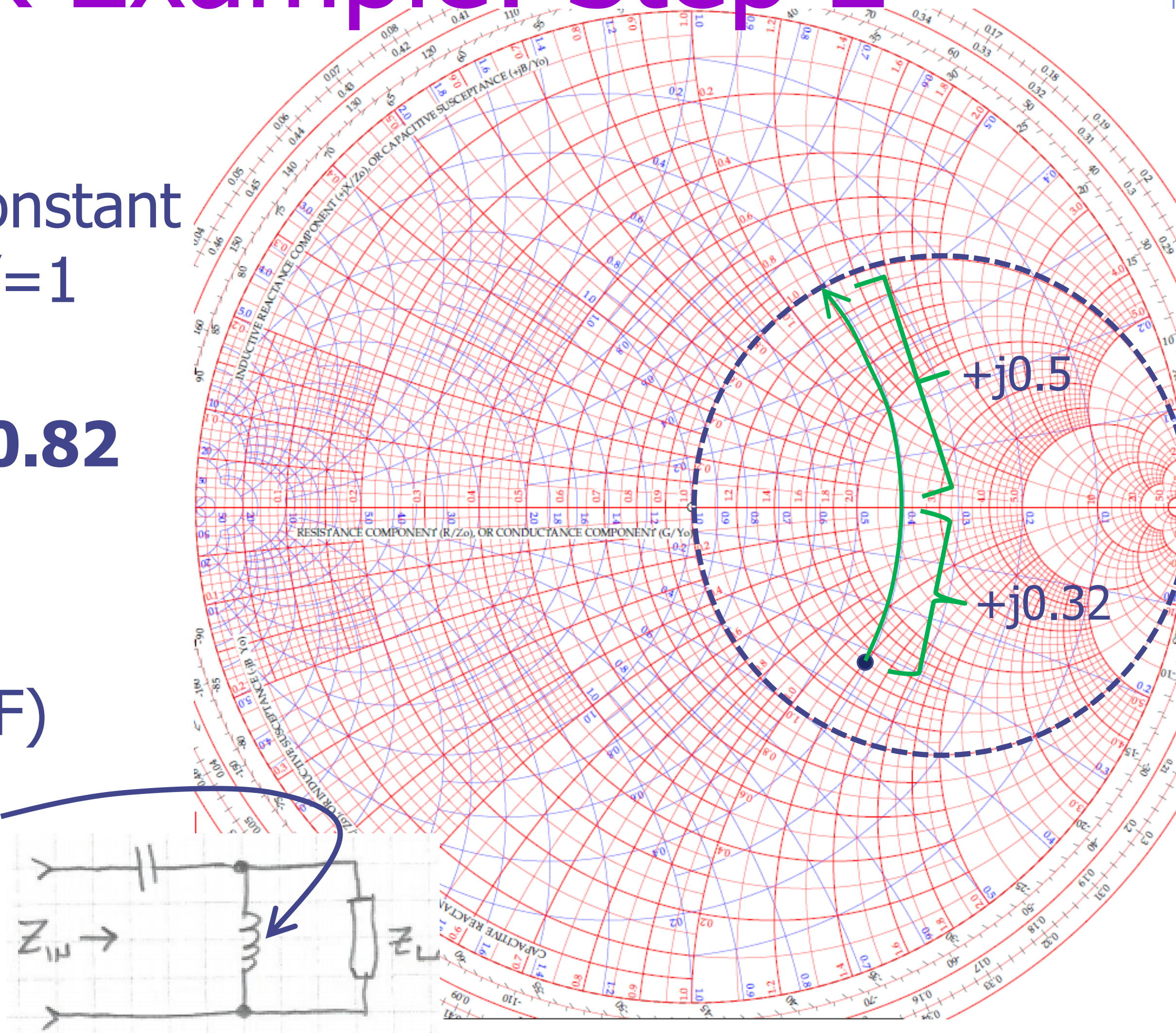
- Freq = 432.1MHz
- $Z_L = 75 - j60$
- Normalize…
- $Z_L' = 1.5 - j1.2$
- Plot it
- Pick a topology:





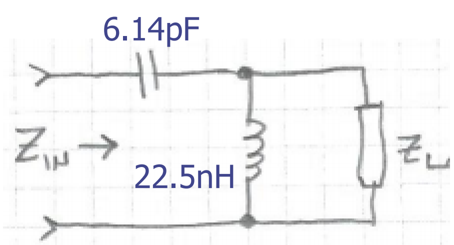
L-Network Example: Step 2

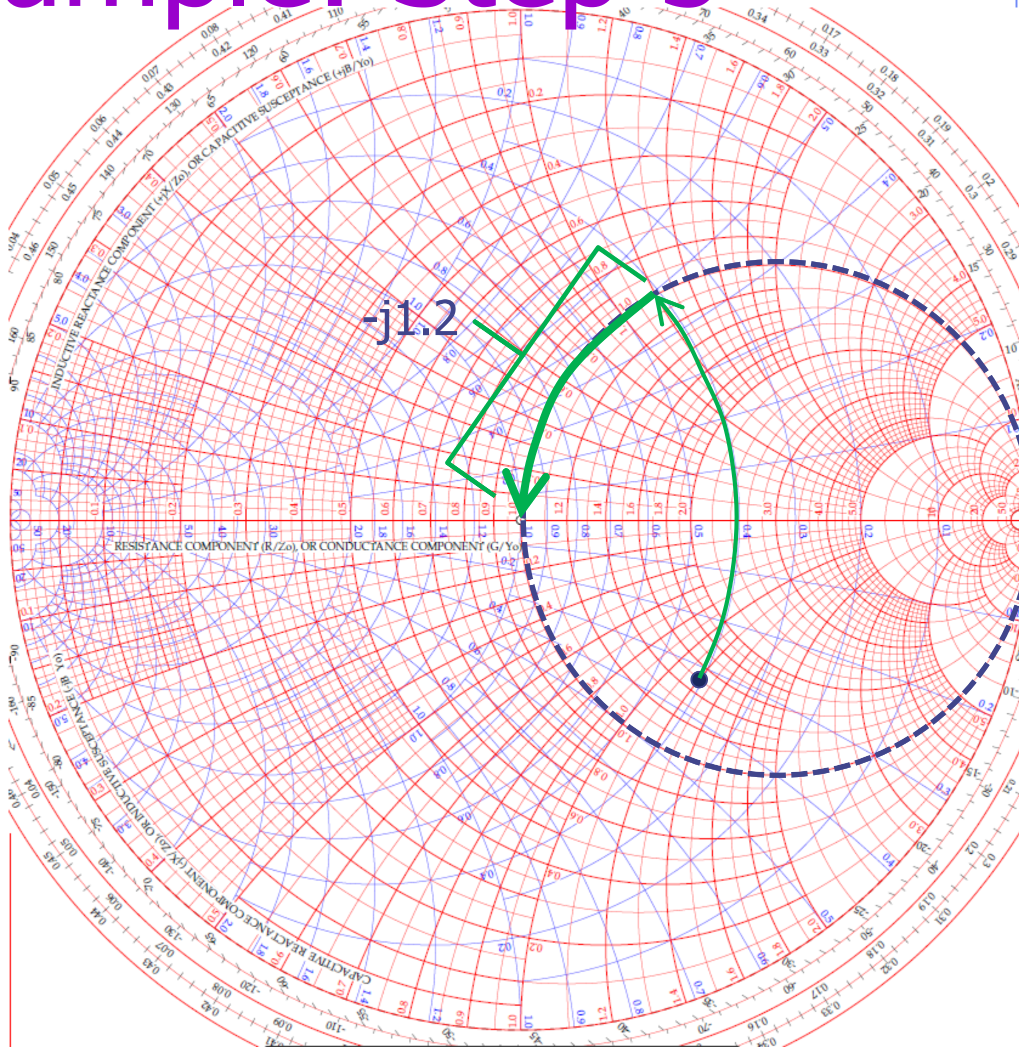
- Add Shunt L
  - Rotate on constant G until hit R′=1
  - Added B'_L is 0.32+0.5=**j0.82**
  - X'_L=j1.22
  - X_L=j61
  - $L=X_L/(2*pi*F)$
  - **L=22.5nH**



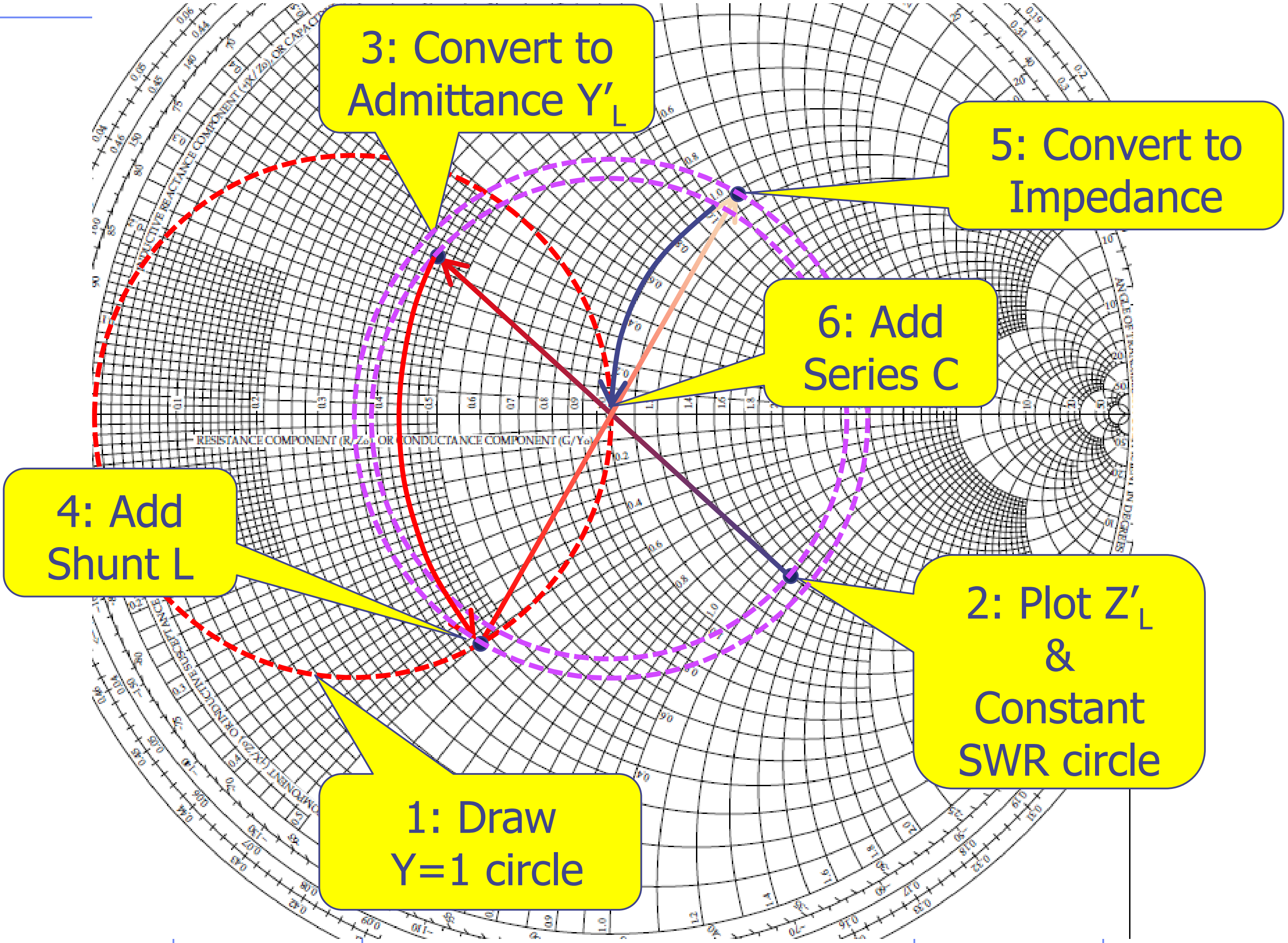
L-Network Example: Step 3

- Add Series C
  - Rotate on R'=1 until hit Z_0
  - Added X'_C = **-j1.2**
  - X_C=-j60
  - $C=1/(X_C*2*pi*F)$
  - **C=6.14pF**





Extra Credit: Z-only chart



Summary

- The Smith Chart is a highly useful tool:
  - Complex Impedance Transformations
  - Determining VSWR, RL, and much more
  - Transmission Line impedance transformations
  - Matching Network Design
  - …and a lot more that we haven't touched on
- Check out SimSmith – PC based tool
  - http://www.ae6ty.com/Smith_Charts.html
  - http://www.w0qe.com/SimSmith.html