The Glider
Stelio Frati
L'ALIANTE

ELEMENTI DI PROGETTO DEI MODERNI ALIANTI VELEGLIATORI - AERODINAMICA - INSEGNO CALCOLO STATICO - STRUTTURE

Con 250 illustrazioni, numerosi esempi di calcolo ed una ricetta di 36 fogli più note alinanti italiani e stranieri

EDITORE ULRICO HOEPLI MILANO
1946
Preface

At our Falco Builders Dinner at Oshkosh '89, Fernando Almeida mentioned “Mr. Frati’s book” in some context. This was the first I had heard of it, and Fernando explained that Mr. Frati had published a book years ago on aircraft design. Then and there, I decided I would have to get my hands on the book and get it translated into English.

Subsequently, Fernando mailed me his only copy of the book, *L’Aliante* (The Glider) which was a photocopy of the original. Since then, we have slowly worked our way through the book. The bulk of the work fell on Maurice Branzanti who translated the original text into English. I then edited and polished the words into the copy you see here, at times with the help of Steve Wilkinson, Jim Petty and Dave Thurston.

As you might imagine, the original 1946 book contained a lot of material that is hopelessly outdated now. The book contained many illustrative sketches of gliders circling clouds, launching by being towed by a car, and the like. There were many references to contemporary gliders and airfoils—indeed a large section of the book was simply a series of charts and tables of airfoils with the usual coordinate and aerodynamic data.

We have not included these outdated charts and decorative illustrations, and instead we have attempted to reproduce the original book in a form that covers the engineering and design principals in a way that doesn’t date the book in any obvious way. Thus we must apologize for a lack of strict fidelity to the original text, but we did this in the interest of producing a more immediate and interesting book.

Since Mr. Frati has no intention of reviving the book, we are happy to share it with everyone, first in installments of our Falco Builders Letter, and now in a book format that you can download from the Sequoia Aircraft web site at www.SeqAir.com. There are nine chapters in all, and this is our progress to date. We will be updating our web site as we make further progress.

Alfred P. Scott
Introduction

Among the many types of flying machines that helped conquer our airways, from the most modest and delicate to the huge, rugged Flying Fortress with thousands of horsepower, there is one category of aircraft that does entirely without engines: the gliders.

The glider was developed in Germany after the first world war, and it found particular acceptance among younger pilots. Even though many used it as a new form of sport and excitement, others employed experimental gliders to advance their studies in aerodynamics and to develop new methods of construction.

Today, aviation owes a great tribute to these last individuals. In fact, the glider has taught a great deal to designers, builders and pilots. To realize how much, we need only look at how many ways our armed forces have used these vehicles in the recent conflict.

To build a glider, one needs no huge industrial facilities, complex technical equipment or large financial backing—just pure creativity, a clear understanding of aerodynamic phenomena, and a patient pursuit of perfection in design and construction. So even our country, thanks to the efforts and merits of the “Centro Studi ed Esperienze per il Volo a Vela” at the Milan Polytechnic, was able to compete vigorously in this field.

The author of this book is, in fact, a young graduate of our Polytechnic who has already tested his theories and practical notions by building several successful gliders.

In this volume, you will find in simple terminology all the necessary advice and information you’ll need to begin the project, complete the construction and fly your glider.

Don’t be frightened if this book seems rather large for such a simple subject. It also includes the specifications of a variety of gliders, so in addition to being a textbook, it is also a reference manual.

To the new student generation, may this book be the incentive to further cultivate the passion of flight.

Prof. Ing. Silvio Bassi
Milan, Italy
March 1946
Chapter 1
Preliminary Considerations

1. Soaring
Soaring is the complex of activities that results in the flight of a glider. To be exact: (a) to design and construct a glider, (b) to study a specialized aspect of meteorology, (c) to study the techniques of flying, and (d) to organize proper ground support.

In this book, we will discuss mainly the design of pure sailplanes, and only passing reference will be made to low-performance gliders used for dual instruction.

2. Gliders: Training and Soaring
Official Italian regulations define gliders as aircraft that are heavier than air and have no means of self-propulsion. The use of gliders varies: for dual instruction; for more specialized training in soaring; for aerobatic flight; and for distance, endurance, and altitude flights. A strict subdivision according to the particular use is difficult to make. In fact, from the training vehicle to the record-setting vehicle, there is a complete gamut of medium-performance but still important gliders.

As a convention, we will consider two major classes: gliders and sailplanes. Gliders are defined as those unpowered aircraft that due to their basic construction and flight characteristics are used only for free gliding. In this category, we’ll find those gliders used for training. We consider sailplanes to be unpowered aircraft that due to their superior aerodynamics and construction have improved performance and can be used for true soaring.

To give an idea of the difference in performance, gliders generally have a minimum still-air sink rate of more than 2 m/sec, with a maximum glide ratio of approximately 10:1. Sailplanes, however, have a minimum sink rate less than 1 m/sec, and a glide ratio above 20:1. Under certain atmospheric conditions, admittedly, a glider can be made to soar, when the speed of the rising air is greater than the minimum sink rate of the glider. By the same token, even a high-performance sailplane can do no more than glide when rising air is absent.

In truth, even the most sophisticated sailplane is actually gliding—descending—in relation to the air mass within which it is operating. It will be soaring—gaining altitude—in reference to the earth’s surface, but the altitude reached will depend on the relationship between glider and surrounding air, and the relationship between the air and the earth’s surface.

Because of this anomaly, a glider “rises while descending.”

3. Aerodynamic Characteristics
The aerodynamic characteristics already mentioned are: efficiency, or glide ratio; and sink rate. Glide ratio is the ratio between the horizontal travel $D$ and loss of altitude $H$ in a given time. The value of this ratio,

$$ E = \frac{D}{H} $$

is an indication of the quality of the glider, since at an equal altitude loss $H$, the distance $D$ reached is proportional to the efficiency $E$, which can be expressed an efficiency value, say 20, or more commonly as a glide ratio, typically stated as 20:1.
The sink rate is the amount of altitude lost by the glider in the unit of time in relation to the surrounding air. This value is expressed in m/sec. Thus, from an altitude of 100 meters, a glider that has a minimum sink rate of 1 m/sec and a glide ratio of 20:1 will take 100 seconds to reach the ground after traveling a horizontal distance of 2000 meters. Modern competition sailplanes have achieved glide ratios of over 30:1, with minimum sink rates of .5 m/sec.

It is evident that the lower the sink rate, the longer the duration of any flight from a given altitude, and the higher the chance of being kept aloft by very light ascending air movements. At first glance, it would seem that obtaining the minimum possible sink rate would be of great importance for soaring. However there are two other factors of equal importance: the handling and the horizontal speed of the craft. To better understand this, let’s briefly explain how soaring is achieved.

4. Practicality of Soaring
We can consider two types of soaring: thermal soaring; and ridge, or wave, soaring.

Thermal soaring takes advantage of the vertical movement of air masses caused by temperature differences. The rise of an air mass occurs when a so-called “thermal bubble” detaches from unevenly heated ground formations. These thermal currents are generally of small dimension. Larger masses of ascending air occur under cumulus clouds, and air movements caused by storm fronts are of particularly high intensity.

In ridge soaring, pilots take advantage of the vertical component that results from a horizontal air movement encountering a mountain, hill or slope.

In thermal soaring, either for endurance or distance, we try to gain altitude by flying tight spirals in a favorable site while the conditions are good. When conditions deteriorate and we cease to gain altitude, we move in search of a new area. It is obvious than that when we are trying to gain altitude, the handling of sailplane is of great importance. The tighter the spiral flight, the greater the likelihood that we can stay within even the smallest thermals.

But during the straight-and-level flight from one rising mass to another, it is obviously important to do so as rapidly as possible to minimize the loss of altitude. In this case, it is important for the sailplane to be capable of the maximum possible horizontal speed and low vertical speed—i.e. high efficiency. Unfortunately, it is not possible to combine both pure speed and ultimate maneuverability, so a certain compromise between the two is necessary. Which preference is given to one over the other depends greatly on the intended use of the glider.

5. Launching Methods
Even though it is not directly related to a sailplane design project, it is important to know the launching methods used so we can study the airframe structure and the placement of the necessary hardware required for launching. Since the glider does not have an engine, it obviously needs some kind of external energy to get airborne. The launching methods most commonly used are: elastic cord, ground winch, automobile tow, and airplane tow.

Launch by Elastic Cord. This type of launching is the simplest and most economical, and it has been employed for several years by training schools in various countries.
An elastic cord is attached to the glider’s nose while its tail is securely anchored to the ground. The cord is then stretched like a slingshot by two groups of people spread out at an angle of approximately 50-60°—so they won’t be run over by the glider at the time of release. When the cord has reached the proper tension, the glider is freed. The slingshot action then catapults the glider into flight with an altitude gain proportional to the cord tensioning.

This system presents one major inconvenience: acceleration so high at the instant of launch that it can stun the pilot, with possible serious consequences. However, if the tension of the cord is reduced to diminish the acceleration effect, the glider will fail to gain sufficient altitude. For this reason, elastic-cord launching has been abandoned, except for launching from atop hills, where the acceleration can be reduced since only horizontal flight has to be sustained.

**Launch by Ground Winch.** This system has seen many modifications and improvements throughout the years. It is now the most practical and safest means of launching.

The system consists of a large rotating drum driven by a powerful motor. The glider is pulled by a steel cable, of approximately 1000 meters in length, that winds onto the drum. With this system, the speed of launching can be controlled, making a gradual and safe transition from ground to altitudes of 200-250 meters possible.

**Launch by Automobile Tow.** In the United States, it is common practice to tow a glider with an automobile. A cable of 1000 to 3000 meters in length is stretched between the automobile and the glider. This requires a paved runway or a well-maintained grass strip long enough so the automobile is able to reach the speed needed for the glider to fly.

Economically speaking, this system, is less efficient than a ground winch launch, which requires only enough power to pull the glider, while auto-tows need the extra power to run the automobile. As a bonus, however, altitude gain is far greater.

**Launch by Airplane Tow.** All the systems previously described are mainly used for launching of training gliders. For true sailplanes, it is essential to reach launch altitudes of between 500 and 1200 meters. The most practical way to accomplish this is a tow to altitude behind an airplane. A cable of 60 to 100 meters in length is stretched between the aircraft. When the desired altitude and conditions are reached, the cable is released by the sailplane.

This system has the advantage of not requiring a complex ground organization. The tow plane should be able to fly slowly, just over the cruising speed of the glider to avoid overstressing the glider and to allow it to maintain an altitude not too far above the towplane.
Chapter 2
General Characteristics of Gliders

6. Introduction
Because of their specialized use, gliders are quite different from powered airplanes. This is made obvious by several characteristics. One is the completely different arrangement of the landing gear, a result of the light weight of the aircraft and the absence of a propeller. Others are that the pilot’s seat is located toward the front for center-of-gravity reasons, the wing span is always considerable, and the fuselage and other components are well streamlined to obtain the maximum aerodynamic efficiency.

Wood has been almost universally accepted as the prime building material. It is fairly inexpensive, practical to use, and easy to repair, even with simple tools. In some cases, a fuselage of welded steel tubing with fabric covering has been adopted. This provides a light and simple structure, but it will never beat the rigidity and aerodynamic finesse of wood construction.

A few examples of all-metal gliders are available, but this method of construction requires a well-equipped shop and specialized, skilled labor. The high cost involved limits such construction to high-volume, production-series aircraft, seldom the case with gliders.

Let’s now consider the two major classes in which we categorize gliders and explain their characteristics in detail.

7. Training Gliders
This type of glider should be of simple construction, for low cost and easy maintenance. This is an important consideration, since a flight school often uses its own students to carry out small repairs, and the equipment at their disposal is usually not the best.

Gliders in this category should also be quite rugged, especially in the landing gear, since they often aren’t flown with great skill.

A certain uniformity of design is characteristic of this class of glider. The wingspan is usually 10 meters, the wing area is 15-17 square meters, and the glider has a high, strut-braced wing of rectangular planform and a low aspect ratio.

The fuselage may be only an open framework of wood or tubing with the cockpit completely open, or it can be a closed, plywood-skinned box section. The wing loading of these aircraft is always very low, usually around 12-14 kg/square meters, and with an empty weight of 90-120 kg.

The wood wing is a double-spar structure, the spars braced together for torsion strength and the whole covered with fabric. The control surfaces are driven by steel cables and bushed pulleys, and the landing skid is incorporated in the fuselage and can be shock-absorbed.

In this glider there is absolutely no instrumentation, since due to their use it would be meaningless. The use of a parachute is also senseless; because of the low altitude of flight, a parachute would be useless in case of emergency. The common cruise speed is on the order of 50 km/h.
8. Sailplanes

Training Sailplanes. The uniformity of design that we have seen in training gliders does not exist in this category. In general, these designs have strut-braced wings, box-section fuselages, and open cockpits. The wing span is between the 12 and 14 meters, wing loading 15-17 kg/sq m, and they all have basic instrumentation.

Competition Sailplanes. As mentioned before, there are many variations of sailplanes. One may have a simple high wing and V tail, another a gull midwing. The wingspan may reach over 20 meters with variable flaps and up to 33 meters in some cases.

Particular care is given to the cockpit area, in terms of both instrumentation and pilot position. Reclining seats, adjustable pedals, cockpit ventilation, and anything else that might provide the pilot with the greatest possible comfort are important in these gliders, since endurance flights have lasted longer than 50 hours, and distance flights have reached the 700-km mark.

Almost all these gliders are single seat, but two-seat sailplanes are increasing in popularity, especially for endurance and distance flights. In these cases, the sailplanes have dual controls. The seats can either be side-by-side or tandem.

In the case of a tandem configuration, the second seat coincides with the aircraft’s center of gravity, so the balance does not change whether flying with one or two persons. One advantage of the tandem configuration is to maintain the fuselage cross-section at a minimum, therefore increasing efficiency. While the aerodynamics of the side-by-side configuration aren’t as good, the pilot’s comfort and the copilot’s visibility are improved.

9. The Structure of Sailplanes

While today’s gliders may differ in design, they are all very similar in basic structure. Let’s quickly describe the principal structures, keeping in mind that we will be referring to wood construction.

Wing Structure. The wing structure that has been in use for a number of years is based on a single spar with a D-tube torsion box. This design was developed in order to obtain the necessary strength in the long wingspan with minimum weight—an important concept in gliders. This is achieved by placing one single spar in the area of maximum wing thickness, of roughly 30-35% of the wing chord.

In these wings, there is always a second smaller aft spar, between 60-70% of wing chord. Its purpose is not to increase the wing strength, but merely to supply a mounting surface for the aileron hinges and to maintain the wing ribs in the proper position; otherwise they would be distorted by the tensioning of the covering fabric.

Notwithstanding the actual shape of the wing, the spar can be of three classical types: (a) double-T frame with center web, (b) C-frame with one side web, (c) box spar with two webs, one on each side. In sailplane construction, the most-used method is the third one—the box spar.

The spar is the element that withstands the forces of bending and drag. The wing is also affected, especially at high speeds, by great torsion forces. In the single-spar structure, this torsion is resisted in part by the box-like structure that exists between the leading edge and the spar (an area covered by thin plywood) and in part by the spar web itself.
The torsion is then transferred to the fuselage by the wing attachments. The usual solution is to transfer the torsion through a properly placed aft diagonal member that extends from the spar back toward the fuselage.

The area between the spar and the diagonal member is also covered with plywood to produce a closed and torsion-resistant structure.

A much simpler and more rational system is to transfer the torsion by means of a small forward spar. This will not only improve the flight characteristics of the assembly, but it offers a gain in weight due to the elimination of the cover between the spar and the diagonal.

The reason that this system is little used is due to the difficulty encountered in the connection of the forward part of the wing with the fuselage, which at this point usually coincides with the cockpit, and which does not offer sufficient strength for the connection.

The other structural elements of particular importance, since they contribute to the wing’s shape, are the wing ribs. In most gliders, these ribs are of the truss style of design, and the members are glued in place and reinforced with gussets on each side. The truss may be made up of both vertical and diagonal members, or only diagonal members.

Sometimes, the ribs are completely covered with plywood on one surface, and in this case the diagonals members are omitted and only the vertical braces are used. This structure is much simpler than the truss, but it is slightly heavier and more costly.

The ribs are joined to the spar in two ways: full-chord ribs are slide over the spar, or partial ribs are glued to the spar faces and reinforced by gussets. The second method is more common because it allows for a thicker spar without any increase in weight.

**Fuselage Structure.** The fuselage is made up of wooden frames connected to each other by wooden stringers and finally covered with plywood. On tubular metal frames, a fabric covering is usually used. The fuselage frames are always of the truss type, with gusset connections like the ones we have seen in the rib construction. For the frames subjected to high stress, a full plywood face on one or both sides is used.

With a plywood skin covering, it is possible to obtain great torsional strength, while bending forces are resisted by the horizontal stringers and the portion of plywood covering glued to the same stringers.

The strongest frames should be the ones that attach to the wings, because they must support the plane’s full weight. The frames that support the landing gear should also be particularly strong.

A fixed single wheel is attached to the fuselage with two wooden members between frames. There is no need for shock absorption, since the cushioning of the tire itself is sufficient. In the case of retractable gear, various retraction systems are used, but they always have considerable complications.

For the wing/fuselage connection, as in the most common case where each wings is a separate piece, the system currently adopted is one in which the wings are first connected with metal fittings and then the wing, now as one unit, is connected to the fuselage by
less complicated attachments. This way, the fuselage is not affected by the considerable forces of wing bending and needs to support only the wing weight and the forces applied to it.

**Tail Section.** The structure of the tail section is similar to that of the wing: a spar of box or C shape, truss-style ribs, plywood covering for the fixed surfaces (stabilizer and fin), and fabric covering for the control surfaces (elevator and rudder).

Sometimes the stabilizer is of a twin-spar structure with plywood covering from leading edge to forward spar and fabric covering for the remainder. This solution is of limited value, though, since the weight saving obtained the reduction of the plywood covering is balanced by the extra weight of the double spar, and obviously also by the extra construction complication encountered.

The elevators and the rudder, like the ailerons, are fabric-covered to reduce the weight, and this is also necessary to keep the inertia of the moving mass small. The required torsional strength is achieved by diagonal members between ribs, while more sophisticated gliders have a semi-circular plywood section on the leading edge of the control surfaces.
Chapter 3  
Elements of Aerodynamics

11. Aerodynamic Force  
A stationary body immersed in a flow of air is subjected to a force that is the total of all forces that act upon it. This resultant force is called the aerodynamic force and is designated by the letter \( F \). Generally, the direction of this force is different from the air flow direction.

\[ V \quad F \]

*Figure 3-1*

If the body has a symmetrical shape relative to the air flow, the aerodynamic force is also in the same direction.

\[ V \quad F \]

*Figure 3-2*

However, if the same body is rotated in relation to the air flow at the angle \( \alpha \) ("alpha"), called the angle of incidence, the direction of the force \( F \) is no longer in the direction of the air flow and is usually at a different angle than the angle of incidence.

\[ V \quad \alpha \quad F \]

*Figure 3-3*

The reason the force \( F \) is not in the same direction as the air flow is due to the difference in velocity of the air particles between the upper and lower surfaces of the body. This phenomenon was studied by Magnus and is demonstrated by Flettner’s rotating cylinder.

**Rotating Cylinder.** Let’s immerse a cylinder in a flow of air. This flow will produce a force \( F \) on the cylinder in the same direction, because the cylinder is symmetric with respect to the flow.
Now, if we rotate the cylinder around its axis in the direction shown, the fluid particles in direct contact with the surface will be carried by friction. Notice that while the velocity of the particles over the upper surface will be added to the stream velocity, in the lower portion the velocity will subtract. The result is a higher stream velocity in the upper surface and a lower velocity in the lower surface.

Thus, the motion of the fluid particles around the cylinder is a combination of the effects of the direction of the stream and the rotation of the cylinder. The direction of the air downstream of the cylinder is now at the angle \(i\), called the induced air flow angle. The value of the aerodynamic force depends on various factors:

- air density \(\rho\) ("rho"—mass density of standard air)
- area of the body \(S\)
- relative velocity \(V\) (air flow velocity in relation to the body)
- shape and orientation of the body in relation of the direction of the stream, a factor we will call \(C\).

Analytically, the dependence of \(F\) is expressed by the following equation:

\[
F = C \cdot \rho \cdot S \cdot V^2 \quad [1]
\]
where the units of measurement are:

\[ F = \text{force in kg.} \]
\[ V = \text{velocity in m/sec.} \]
\[ S = \text{area in m}^2 \]
\[ \rho = \text{density in kg. sec}^{-2}/m^4 \]
\[ C = \text{nondimensional coefficient} \]

12. Airfoils
A solid section of particular importance is the airfoil. Its shape is such that the air flow around it generates a field of pressure that is a combination of fluid movements along and around it, as in the case of the rotating cylinder. In other words, a uniform air flow will undergo an increase in velocity over the upper surface of the airfoil and a decrease over the lower surface.

Due to the well-known Bernoulli theorem, we will have a decrease of pressure where the velocity increases and an increase of pressure where the velocity decreases. The aerodynamic force \( F \) therefore depends on positive pressure along the bottom and negative pressure—suction—on the top. The pressure and suction vary with the angle of incidence of the air flow.
As you can see, the suction is much greater than the pressure at normal flight conditions. This means that the lift of the wing is due more to a suction effect than a pressure effect, contrary to what it may seem at first sight. In short, we may say that an airplane flies not because it is sustained by the air underneath, but because is sucked by the air above it.

This experimental observation was of great importance in the understanding of many phenomena of flight. Moreover, this should be considered when designing the wing structure and skin covering, especially for very fast aircraft.

**Lift and Drag.** When we say “airfoil,” we are really talking about a section of a wing with its vertical plane parallel to the longitudinal axis of the aircraft. Let’s consider the force $F$ in this plane, and let’s split it in two directions, one perpendicular to the direction of the relative velocity, and one parallel.
Let’s call lift $L$ and drag $D$. Flight is possible when the lift $L$ is equal to the weight $W$. In the same manner as we have seen for the aerodynamic force $F$, lift and drag are expressed by the following equations:

\[
L = C_L \cdot \left( \frac{\rho}{2} \right) \cdot S \cdot V^2 \quad [2]
\]

\[
D = C_d \cdot \left( \frac{\rho}{2} \right) \cdot S \cdot V^2 \quad [3]
\]

where the non-dimensional coefficients $C_L$ and $C_d$ are called the coefficient of lift and coefficient of drag, respectively.

These coefficients are obtained in wind tunnels, which work on the principle of reciprocity. In other words, an air flow with velocity $V$ will impose a force on a stationary body equal to the force derived from the body moving with velocity $V$ in an atmosphere of stationary air.

The airfoil model under analysis is suspended from scales, which will register the forces that are caused by the wind. By changing the dimensions of the model and the velocity of the air, the forces on the airfoil will also change. The results are then reduced to standard units independent of the airfoil dimensions and the air velocity. The units measured are square meters for the surface area and meters per second for the velocity.

In reality, things are not as simple as this. The measurements given by the scales require a large number of corrections. These depend upon the characteristics of the wind tunnel and the Reynolds Number used in the experiment. However we will not elaborate on this, because the subject is too vast.

**Center of Pressure.** The intersection of the aerodynamic force $F$ with the wing chord is called the center of pressure. It is shown with the letters $C.P.$ in Figure 3-8.

As we have seen so far, the aerodynamic force $F$ is represented in magnitude and direction as a resultant of $L$ and $D$. But as far as its point of origin (center of pressure) is concerned, things are not that simple. In fact, the force $F$ for certain angles of incidence of lower lift will no longer cross the wing chord; therefore the $C.P.$ is no longer recognizable. We will see later how we can get around this.

**Angle of Incidence.** The pressure, suction, aerodynamic force, lift and drag will vary with the angle of the solid body form with the relative direction of the air flow. This angle of incidence is normally defined as the angle between the relative direction of the air flow and the chord line of the airfoil.

**Efficiency.** The ratio between lift and drag is very important in aerodynamics. This ratio is called efficiency, and it is indicated by the letter $E$.

\[
E = \frac{L}{D} = \frac{C_L}{C_d} \quad [4]
\]

Physically, efficiency represents the weight that can be lifted for a given amount of thrust. It is obvious, therefore, that is important to always obtain the maximum value of
$E$ by reducing drag to a minimum. The efficiency $E = \frac{C_L}{C_d}$ improves gradually by increasing the wing span, as we will see later. The experimental values of $C_L$, $C_d$, and $E$ of airfoils obtained in wind tunnels are generally for aspect ratios of 5 or 6.

13. Charts
To aid in the understanding of aerodynamics, it is helpful to show the characteristics of an airfoil in orthogonal or polar charts. Since the coefficients $C_L$ and $C_d$ are always less than one, their values are multiplied by 100 in these charts.

Orthogonal Charts. In this type of chart, the coefficients $C_L$, $C_d$ and $E$ are functions of the angle of incidence $\alpha$. On the vertical axis, we have the $C_L$, $C_d$ and $E$ coefficients, and the angle of incidence $\alpha$ is on the horizontal axis. Thus we have three curves relative to $C_L$, $C_d$, and $E$. To obtain the value of a coefficient at a certain angle of incidence, for instance $\alpha = 6$ degrees, you draw a vertical line from the incidence angle axis equal to the given value. And for all the points of intersection of this line with the three curves, you draw corresponding horizontal lines to determine the values for $C_L$, $C_d$ and $E$.

![Figure 3-9](image-url)

Polar Charts. In a polar chart, we have the value of $C_d$ on the horizontal axis, and the value of $C_L$ on the vertical axis. The values of $C_L$ and $C_d$ are given by a single curve called the polar profile, on which the angle of incidence alphas are marked.
To determine these values for a certain incidence, for example $\alpha = 6$ degrees, on the point on the curve corresponding to that incidence you draw two lines, one vertical and one horizontal. The value of $C_L$ and $C_d$ are read on the proper corresponding axis.

A feature of the polar profile is that the point of tangency with a line drawn from the origin of the axes represents the angle of incidence of maximum efficiency.

The curve of the efficiency $E$ relative to $C_L$ is also shown in the polar chart. At a given angle of incidence, its value is obtained by drawing a horizontal line that will intersect the $E$ curve. At this point of intersection a vertical line is drawn, and the value is read on the proper scale.

**14. Moment of an Airfoil**

To establish the position of the center of pressure, we first determine the moment of the aerodynamic force $F$ with respect to a point on the airfoil. By convention, the leading edge is used. The moment and the coefficient of moment $C_m$ are determined in a wind tunnel as was done for lift and drag.
The moment \( M \) is:

\[
M = C_m \cdot \rho \cdot S \cdot V^2 \cdot c \quad [5]
\]

where

\[
c = \text{chord of the airfoil} \\
C_m = \text{coefficient to be determined}
\]

Having found the value for \( M \) by various measurements in the wind tunnel, the coefficient \( C_m \) will be:

\[
C_m = \frac{M}{\rho \cdot S \cdot V^2 \cdot c} \quad [6]
\]

where \( M \) is measured in kgm and \( c \) in meters.

Having found the moment, we now establish the position of \( C.P. \).

Let’s consider the force \( F \) and its moment with respect to the leading edge. We can calculate the arm length \( x \) from \( F \) since

\[
M = F \cdot x
\]

then

\[
x = \frac{M}{F}
\]

The position of \( C.P. \) is given by \( x' \) which is equal to

\[
x' = \frac{x}{\cos \theta}
\]

For normal angles of incidence, angle \( \theta \) is very small so we can substitute \( L \) and \( F \), giving

\[
x' = \frac{M}{L}
\]
and substituting $M$ and $L$ we will have

$$x' = \frac{\rho \cdot S \cdot V^2 \cdot C_m \cdot c}{\rho \cdot S \cdot V^2 \cdot C_L} \cdot \frac{C_m \cdot c}{C_L}$$

If we would like to express the position of $C.P.$ in percent of the chord as it is usually expressed, then we have:

$$\frac{x'}{c} = \frac{C_m}{C_L} \quad [7]$$

In conclusion, we can say that the position of $C.P.$ in percent of the chord for an airfoil at a given angle of incidence is given by the ratio between the coefficient of the moment $C_m$ and the coefficient of lift $C_L$ at that angle of incidence.
15. Moment Equation and its Properties
The equation for the moment is represented by a polar chart as a function of the coefficient of lift. This curve is essentially a straight line until just before the maximum lift value is reached.

The value of the coefficient of moment in relation to zero lift, $C_L = 0$, is of particular importance in determining the airfoil’s stability. This intersection on the horizontal axis is called $C_{m0}$. The position of the center of pressure may be determined graphically in the polar chart by looking at the moment curve.
For a given value of $C_L$, a horizontal line is drawn with its origin on the vertical axis and its length equal to the value of $C_m$, i.e. $100 \ C_L = 30, \ 100 \ C_m = 30$. This line is called the reference chord.

To determine the position of C.P. at a certain $C_L$ value, a horizontal line is drawn through the $C_L$ value in consideration, so that it will intersect the $C_m$ curve at a point A. The line drawn from the axis origin O and the new-found point A or the extension of this line will intersect the reference chord at a point that represents the center of pressure.

**Grade of Stability of an Airfoil.** This graphic construction allows us to arrive at important conclusions about the stability of an airfoil. We can have three cases: (a) the moment curve intersects the horizontal axis to the right of the origin, (b) the curve coincides with the origin, or (c) the curve intersects the horizontal axis to the left of the origin.
Case A. In this case, the curve intersects the horizontal axis at a positive value of $C_{m0}$. Let’s determine, using the previous procedure, the position of the C.P. for a value of low lift, where A is the position of equilibrium. Let’s suppose that now we increase the incidence angle, thus increasing lift (point B on the moment curve). We’ll notice that the C.P. moves forward, toward the leading edge. On the other hand, if the incidence is reduced, the C.P. will move aft towards the trailing edge.

Therefore, in an airfoil where $C_{m0}$ is positive, when a variation occurs, the center of pressure will move in a direction that helps to increase the variation. We then deduce that an airfoil with such characteristics is instable because any variations will be accentuated and moved further away from the position of original equilibrium.
Case B. In this case, $C_L = 0$, $C_{m0} = 0$, and the curve goes through the origin. From the chart we note that for any variation the position of $C.P.$ does not move, and it coincides with the focus of the airfoil. An airfoil with this characteristic is said to have neutral stability.
Case C. Let’s now consider the third condition. For zero lift, $C_{m0}$ is negative. The effect of the center of pressure is therefore opposite the one noticed in Case A. For an increase in incidence, the $C.P.$ will move toward the trailing edge, and forward when the angle of incidence is reduced. In these conditions, the airfoil is stable.

All of the airfoils in use, however, are designed as in Case A—they are therefore instable. Airfoils that are unaffected by variations (Case B) are used in tail sections. Their profiles are biconvex and symmetric.

Surfaces that are flat are the one like in Case C, these are stable, but obviously they are not used in the wing construction, both because of the impossibility of obtaining structural strength and because of the low values of lift and efficiency. There are in existence some airfoils that follow the characteristics of these flat surfaces, and these are called autostable, but their use is limited to wing extremities.

The instability is at maximum in concave convex profiles with high degree of curvature, and it diminishes gradually through lesser degree of curvature in the biconvex asymmetric airfoils to, as we have seen, completely disappear in the symmetric biconvex profiles.
The measurement of instability of an airfoil is in conclusion dependent on the movement of the C.P. with variation of incidence. In the normal attitude of flight, the position of C.P. varies between 25-45% of the wing chord when normal wing airfoils are considered, while for biconvex symmetric profiles found in the tail sections, the variation is 25%.

By studying the moment curve we can thus rapidly establish the instability of a certain airfoil, and say that the closer to the origin the moment curve intersects the horizontal axis (small values of $C_{m0}$), the flatter the curve is, and the less the instability is.

**Moment Arm.** Let’s suppose we now would like to find the moment, not in relation to the leading edge as we did previously, but in relation to any point on the chord of the airfoil in question, let us say point $G$ for an attitude corresponding to the point $A$ for the moment curve in Fig. 3-17.

Joining points $G$ and $A$ with the origin $O$, the extension of the line $OA$ will determine on the reference line the center of pressure C.P., while the line $OG$ will intersect the horizontal line between $A$ and $B$. The line $AB$ represents, on the $C_{m}$ scale, the moment of the aerodynamic force for the attitude under consideration in relation to the point $G$. 

![Figure 3-17](image-url)
Thus, if we name $x_g$ the distance of the point $G$ from the leading edge, and $x_p$ the distance of $C.P.$, due to the similarity of the triangles $MOG$ and $NOB, MOP$ and $NOA$, we have:

$$\frac{x_p}{x_p - x_g} = \frac{NA}{BA}$$

In the chart, $NA$ is the moment $C_m$ in relation to the leading edge and $BA$ is the moment $C_{mg}$ in relation to the point $G$. If point $G$ happens to be the fulcrum of the aircraft, relative to which we need to determine the moments, these are then found simply by connecting the origin $O$ with the fulcrum $G$ on the reference chord; the horizontal segment found between the said lines and the moment curve will give us the moment fulcrum for that given attitude. This line, which starts at the origin and passes through the fulcrum $G$, is called the fulcrum line.

![Figure 3-18](image)

Following this we may establish, given the fulcrum $G$ on the reference chord, the equilibrium attitude, by drawing a horizontal line through the intersection of the fulcrum line and the moment curve. (Fig. 3-18) The $C.P.$ of this particular attitude coincides with the fulcrum $G$. These properties of the chart allow us to study the aircraft’s stability graphically, as we will see later on.
16. Wing Aspect Ratio

Thus far we have discussed $C_L$ and $C_d$ without considering one very important factor of the wing, the wing aspect ratio $AR$. This is the ratio between the wing span and the mean chord:

$$AR = \frac{b}{c_m} \quad [8]$$

where, $b$ is the wing span and $c_m$ is the mean chord, however the following expression is more widely used:

$$AR = \frac{b^2}{S_w}$$

where $S_w$ is the wing area.

To better understand the effect of the aspect ratio on the wing coefficients, let’s remember how the lift phenomenon works. We have seen that during normal flight conditions lift depends on pressure below and suction on top of the wing. Thus the air particles will have a tendency to move at the wing tips from the high pressure zones to the low pressure zones by revolving around the wing tips.

Since the air flows in direction $V$, the air particles at the wing tips will have a spiral motion. This is the so-call vortex, and it produces an increase in drag and a decrease in lift. The larger the wing chord at the tip, the larger are the produced vortexes. An increase in the aspect ratio causes a reduction in the wing chord, and thus a reduction of drag, which depends on two factors, profile drag ($C_{dp}$) and induced drag ($C_{di}$).

$$C_d = C_{dp} + C_{di} \quad [9]$$

The coefficient of induced drag is given by:

$$C_{di} = \frac{2(C_{dp})^2}{\pi} \cdot \frac{1}{AR} \quad [10]$$
This induced drag is, in fact, the one produced by the vortex at the wing tips.

For a wing with an infinite aspect ratio, $AR$ equals infinity, the induced drag $C_{di}$ is 0, and the drag is only the profile drag. From Formula 10, we notice how the induced drag $C_{di}$ depends on the lift $C_L$, and this is explainable by the lift phenomenon itself. The larger the $C_L$, the larger the difference between the pressure and suction, thus the larger the intensity of the vortexes. The aspect ratio therefore influences the induced drag while the profile drag remains the same.

The variation of $C_{di}$ with the variation of the aspect ratio is found in the following relationship:

$$
\Delta C_{di} = \frac{2(C_L)^2}{\pi} \cdot \left( \frac{1}{AR_1} - \frac{1}{AR_2} \right) \quad [11]
$$

where $AR_1$ and $AR_2$ are the two values of the aspect ratio. During practical calculations, $AR_1$ is the experimental value given by tables and generally is equal to 5, while $AR_2$ is the real one of the wing.

The coefficient $C_{d}'$ of a wing with aspect ratio $AR_2$ will be:

$$
C_{d}' = C_d - \frac{2(C_L)^2}{3.14} \cdot \left( \frac{1}{AR_1} - \frac{1}{AR_2} \right)
$$

Since the vortexes increase drag and destroy lift, an increase in aspect ratio will improve lift as a result. In practice though, these improvements are ignored because they are small values.
Influence of the Aspect Ratio on the Polar Curve. Let us examine the changes to the polar curve with an increase of the aspect ratio.

Let’s consider the polar curve relative to the aspect ratio, $AR_1$ (dashed line), and let’s increase the value to $AR_2$. Calculating the values for different attitudes, we establish the values of $C_{d}'$ relative to $AR_2$. This new polar curve (solid line) will intercept the horizontal axis at the point $M$, this being the same point as the original curve intercepted, since $C_L = 0$ and the variation $\Delta C_d = 0$. For increasing values of $C_L$, the variation $\Delta C_d$ is negative, and it will increase until it reaches its maximum value at the maximum value of lift, a value given by the line $C-C'$.

From this new curve we can see that the attitude of maximum efficiency has moved to greater angles of incidence and a greater minimum value for drag. Thus, increasing the aspect ratio gives a double advantage: (a) a reduction of drag, with subsequent increase in efficiency and (b) movement towards attitudes of greater lift with minimum drag. This very important for gliders which always operate at attitudes of high lift.
We should consider though that the aerodynamic coefficients are also influenced by the shape of the wing itself. The optimum shape would be of an elliptical form that resembles the distribution of lift. As a matter of fact, in fighter planes, where the aspect ratio is rather small, this type of shape is often used. These wings are very complicated to build, so for gliders where the aspect ratio is always high, a linear form with a slight curvature at the wing tips gives optimum results.

17. Wing with Varying Airfoils

It is often of more convenient to build a wing with varying airfoils. In modern planes, this is usually the case. A constant-airfoil wing is rarely used. For structural reasons, the wing is usually thick at the connection with the fuselage. It is here that the greatest forces of bending and shear are applied. As we move toward the wing tips, the airfoil is much thinner to reduce drag and to improve stability and efficiency. For these and other reasons, the wing is almost never of constant chord.

![Figure 3-21](image)

Let’s see how we can determine the wing characteristics when the airfoil is variable. Let’s consider a wing with a shape as shown above, where the airfoils are A at the wing root and B at the tip. If the variation between A and B is linear, as is usually the case, then we can accept that the airfoil M in the middle would have intermediate characteristics between A and B. This is not precisely correct due to induction phenomena between adjacent sections, but practical tests show that this hypothesis is close enough to be accepted for major calculations of wing characteristics.

With this hypothesis in mind, where the intermediate airfoil has intermediate characteristics, we can now consider the portion between A and M to have the characteristics of airfoil A, and the portion between M and B to have the characteristics of airfoil B.

The area $S_{w1}'$ of the half wing relative to A will be:

$$S_{w1}' = \frac{c_1 + c_m}{2} \cdot \frac{b}{4}$$

and the area relative to B:

$$S_{w2}' = \frac{c_m + c_2}{2} \cdot \frac{b}{4}$$

These areas will be doubled for the full wing, thus for the airfoil A it will be $S_{w1}$, for the airfoil B it will be $S_{w2}$ (\(S_{w1} = 2 \cdot S_{w1}'\) and \(S_{w2} = 2 \cdot S_{w2}'\)). The ratio between these areas,
The Glider


total wing area $S_w$ is called the coefficient of reduction. Thus we have:

$$ X_1 = \frac{S_{w1}}{S_w} \quad \text{for airfoil A} $$

$$ X_2 = \frac{S_{w2}}{S_w} \quad \text{for airfoil B} $$

These coefficient of reductions, $X_1$ and $X_2$, are less than 1, and their sum is obviously:

$$ X_1 + X_2 = 1 $$

The coefficients $C_L$, $C_d$, and $C_m$ of the airfoils $A$ and $B$ are multiplied by the respective coefficients of reduction $X_1$ and $X_2$. These new reduced values are then added together to the coefficients $C_L$, $C_d$, and $C_m$ of the wing. Summarizing, if we say that $C_{LA}$, $C_{dA}$, $C_{mA}$ are the coefficients of the airfoil $A$, and $C_{LB}$, $C_{dB}$, $C_{mB}$ are the coefficients of the airfoil $B$, then the ones for the complete wing, $C_L$, $C_d$, $C_m$ will be:

$$ C_L = (C_{LA} \cdot X_1) + (C_{LB} \cdot X_2) $$

$$ C_d = (C_{dA} \cdot X_1) + (C_{dB} \cdot X_2) $$

$$ C_m = (C_{mA} \cdot X_1) + (C_{mB} \cdot X_2) $$

As an example, let’s consider a wing with the following dimensions:

- Wing span ($b$) = 12 m
- Wing area ($S_w$) = 12 m$^2$
- Maximum chord ($c_1$) = 1.2 m
- Minimum chord ($c_2$) = 0.8 m
- Midpoint chord ($c_m$) = 1.0 m

![Figure 3-22](image-url)
Let’s suppose that airfoil $A$ is the maximum chord, and the minimum chord is airfoil $B$, and the variation between them is linear. The areas for the half wing $S_{w1}'$ and $S_{w2}'$ will be as we have seen:

$$S_{w1}' = \frac{c_1 + c_m \cdot b}{2} \cdot \frac{b}{4} = \frac{1.20 + 1}{2} \cdot \frac{12}{4} = 3.30 \text{m}^2$$

$$S_{w2}' = \frac{c_m + c_2 \cdot b}{2} \cdot \frac{b}{4} = \frac{1 + 0.80}{2} \cdot \frac{12}{4} = 2.70 \text{m}^2$$

and for the full wing,

$$S_1 = 2 \cdot 3.30 = 6.60 \text{m}^2$$

$$S_2 = 2 \cdot 2.70 = 5.40 \text{m}^2$$

the coefficients of reduction will be:

for airfoil $A$

$$X_1 = \frac{S_{w1}}{S_w} = \frac{6.60}{12} = 0.55$$

for airfoil $B$

$$X_2 = \frac{S_{w2}}{S_w} = \frac{5.40}{12} = 0.45$$

Let’s suppose now that for a particular attitude we have the following values for $C_L$, $C_d$, and $C_m$.

<table>
<thead>
<tr>
<th>Airfoil $A$</th>
<th>Airfoil $B$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$100 ; C_L = 50$</td>
<td>$100 ; C_L = 45$</td>
</tr>
<tr>
<td>$100 ; C_d = 3.5$</td>
<td>$100 ; C_d = 2.5$</td>
</tr>
<tr>
<td>$100 ; C_m = 15$</td>
<td>$100 ; C_m = 12$</td>
</tr>
</tbody>
</table>

Multiplying these values by the respective coefficients of reduction, $X_1$ and $X_2$, we will have the reduced coefficients as:

$$100 \; C_{LA} = 50 \cdot 0.55 = 27.5$$

$$100 \; C_{LB} = 45 \cdot 0.45 = 20.2$$

$$100 \; C_{dA} = 3.5 \cdot 0.55 = 1.92$$

$$100 \; C_{dB} = 2.5 \cdot 0.45 = 1.12$$

$$100 \; C_{mA} = 15 \cdot 0.55 = 7.5$$

$$100 \; C_{mb} = 12 \cdot 0.45 = 5.4$$
Therefore the wing coefficients at this attitude will be finally given by the following summation:

\[
\begin{align*}
100 \ C_L &= 100 \ C_{LA} + 100 \ C_{LB} = 27.5 + 20.2 = 47.7 \\
100 \ C_d &= 100 \ C_{dA} + 100 \ C_{dB} = 1.92 + 1.12 = 3.04 \\
100 \ C_m &= 100 \ C_{mA} + 100 \ C_{mB} = 7.5 + 5.4 = 12.9
\end{align*}
\]

By repeating the same operation for different attitudes, we may calculate the polar curve for a wing with varying airfoils.

**18. The Complete Airplane**

In the preceding paragraphs we have seen how aerodynamic coefficients of the wing are obtained as functions of the wing shape, airfoil and aspect ratio. To obtain the coefficients for the complete airplane, it will be necessary to determine the coefficients for the other parts of the plane, and then add them to those of the wing. Things are not so simple though; the phenomenon of aerodynamic interference comes into play. That is the disturbance that one body in an airstream is subjected to by the presence of another body.

However, due to the simple design of a glider, the coefficients may be derived with good approximation by analytic calculations, but particular care should be given to the intersection axis of the wing and the tail section with the fuselage. In the final calculation, the lift supplied by the fuselage, the tail section and other parts of the plane are never considered due to their small values relative to the lift supplied by the wing.

As far as fuselage drag is concerned, it is not easy to give exact values, since experimental data for gliders is nonexistent. A solution would be to go back and experiment in a wind tunnel, but due to their long wing span, the wing chord of the model would be so small that it would be impossible to make any precise calculation. In practice, for the calculation of the full glider coefficients, the drag from the fuselage, the tail section and other parts, is considered constant, and their lift is nil.

**Additional Coefficients.** The coefficients of drag of all other parts that are within the flow of air have to be taken in consideration, and these must to be added to that of the wing. To do this, this coefficient \( C_d \), is multiplied by the ratio of the area of the part in question and the area of the wing.

Note however that for the fuselage, tires, etc. the area considered is the largest area perpendicular to the airstream, while for the tail group it is the area in the same plane as the wing.
These ratios multiplied by the value of \( C_d \) will give additional coefficients of drag. Thus, for the fuselage

\[
100C_{df} = 100C_d \cdot \frac{S_f}{S_w}
\]

and for the tail section

\[
100C_{dt} = 100C_d \cdot \frac{S_t}{S_w}
\]

and so forth for the other elements.

The coefficient of total drag for the plane (\( C_{dTotal} \)) is then the sum of the wing coefficient (\( C_{dw} \)) with the ones for the other elements:

\[
100C_{dTotal} = 100C_{dw} + 100C_{df} + 100C_{dt}
\]
Since lift will not vary, the airplane’s efficiency is:

\[ E = \frac{L}{D_{\text{Total}}} = \frac{100C_L}{100C_{d_{\text{Total}}}} = \frac{100C_L}{100C_{d_{\text{w}}} + 100C_{d_{f}} + 100C_{d_{t}}} \]

The polar curve of the complete airplane is therefore equal to that of the wing, but it is slightly moved by a line equal to the value of the drag coefficient given by the other elements. (Fig. 3-25) As we have seen, the polar characteristics of the complete airplane has deteriorated, but the maximum efficiency has moved towards a larger incidence, something that could be useful in gliders.
Chapter 4
Flight Stability

19. Static and Dynamic Stability
An airplane has longitudinal, lateral, or directional stability if it will return to its original attitude when disturbed by external forces from its straight-and-level flight by newly generated involuntary forces without the intervention of the pilot. Static stability is when spontaneous forces acting on the airplane will re-establish the conditions that were originally upset by outside forces.

While returning to its original setting, it is possible that the point of equilibrium is passed, thus beginning a number of oscillations. These oscillations may decrease or increase in amplitude. If the oscillations decrease at a fast rate (i.e. are “damped”), it means that the plane possesses not only static stability but also dynamic stability. An airplane requires static stability and dynamic stability to quickly reduce any oscillations.

The components for stability and maneuvering are the entire tail section and the ailerons. The tail section is usually characterized by a fixed portion and by a movable one used for maneuvering, in other words, for changing the plane’s attitude or correcting accidental variations. The ailerons are used for lateral maneuvering or to re-establish lateral stability.

20. Longitudinal Stability
We have seen when discussing the various wing airfoils how these are by nature very instable. Their instability is due to the movement of the center of pressure with changes in the angle of incidence. If the lift $L$ is equal to the weight $W$, when both these forces are at the center of gravity $CG$, we will have equilibrium because the resolution of the forces is nil, as is the moment of these forces with respect to the $CG$ location.

![Figure 4-1](image.png)

Consider what happens if the angle of incidence is increased to $\alpha'$. The center of pressure will move forward from its original position to $C'P$. Lift $L$ now has a moment with respect to the point $CG$, which is:

$$M = L' \cdot b$$

This moment will have the tendency to increase the angle of incidence, thus moving farther away from a position of equilibrium.
An opposite moment will be necessary to re-establish equilibrium. This is achieved by means of the horizontal tail, whose moment with respect to the center of gravity is:

\[ M_t = L_t \cdot D_h \]

where

\[ L_t = \text{Total lift (or negative lift) of stabilizer} \]
\[ D_h = \text{Distance of horizontal tail center of pressure from center of gravity } CG \]

With respect to the individual location of the horizontal tail and the wing, the angle between the wing chord and the stabilizer is called the horizontal tail angle. In Figure 4-2, this angle \( i \) between the wing and the stabilizer is a negative value.

**Moment for the Complete Design.** Let us now examine the moment of the complete aircraft design where the horizontal stabilizer is at given angle \( i \). In the polar chart, the moment curve is still a straight line but with a steeper slope than the ones we have seen for the wing itself when only the partial aircraft was being considered—in other words for an aircraft design without considering the tail section.
By changing angle $i$, we generate different moment curves, but notice that these curves are essentially parallel to each other. This is because they benefit from the property that the incidence angles—which affect the aircraft attitude when changing angle $i$—will move on lines of equal slope, lines called isoslopes. The slope is given by the ratio $MAC/D_h$—the average wing chord over the horizontal tail distance. These isoslope lines are used to determine the moment curves for the complete aircraft design.

We will avoid using the analytical method of establishing these curves because of the many factors involved—factors that are, at times, not easily determined. Therefore we must use a wind tunnel to obtain acceptable results. You run tests by changing the horizontal tail angle and obtain the different moment curves needed for longitudinal stability studies.
**Centering.** After obtaining the moment curves analytically or by experiment, we can proceed to the study of longitudinal stability.

![Diagram of moment curves for partial and complete aircraft](image)

**Figure 4-4**

As you can see in Figure 4-4, we can establish that the position of the aircraft center of gravity cannot exceed the limits set by the points O₁ and O₂, where the center of gravity lines drawn are respectively tangent to the moment curve for the partial aircraft and parallel to the moment curve for the complete aircraft.

In fact, in the case where the center of gravity would be ahead of the point O₁, the center of pressure will result in a farther aft position since its maximum forward position cannot be past O₁ as we have seen when determined graphically. In this condition, we would have a case of auto-equilibrium only for an aircraft design without a tail, while under normal flight conditions the equilibrium would be lost—hence the requirement of a stabilizer anyway. Thus, in all flight attitudes, the tail section will not create lift.

It follows then that the airplane’s efficiency will be reduced due to the lower total lift and the increase in tail drag. From what we have seen, we deduce then that, as the center of gravity moves forward, the aircraft will become more stable, even with a small tail section. Its forwardmost position is however limited by the aerodynamic considerations just explained.
In the opposite case, where the center of gravity is aft of point O2, we will have instability even with larger tail section surfaces and length, and an attitude of equilibrium will not exist.

The range of the center of gravity will have to remain therefore between these two extremes which may vary between 25% to 45% respectively forward and aft. In reality, however, it is always best to have the center of gravity to the front, between 25-30% of the wing chord.

**Angle and Location of the Horizontal Tail Section.** To locate and orient the horizontal tail, after determining the center of gravity position, you must determine the attitude of equilibrium without the intervention of any control surfaces, in other words, the normal flight attitude. As in the case of the wing alone, this attitude is the one corresponding to the intersection between the center of gravity line and the moment curve.

![Diagram showing the relationship between lift coefficient (CL), drag coefficient (Cd), moment coefficient (Cm), and center of gravity (CG)].

Having established this attitude of equilibrium, for example with $C_L = 30$, we draw a horizontal line through this point on the ordinate axis until it intercepts the center of gravity line at point A. This is the point through which the moment curve of the complete aircraft design will have to pass. This curve will give us the angle of the horizontal tail for equilibrium at that particular attitude.

Since high lift is always part of the normal flight attitude of gliders, the angle of the horizontal tail is always negative. At an average equilibrium attitude, we may consider $C_L$ to be varying between...
These procedures are only possible when the moment curves are derived by wind tunnel experiments. Without these, we would have to accept results with a lesser degree of accuracy.

With a glider, you may use a horizontal tail angle between $-3^\circ$ and $-4^\circ$ with a good chance of success.

21. **Horizontal Tail Area**

In our discussions of the moment for the entire aircraft, we assumed that the area of the horizontal tail was already established, but let’s see now how we arrive at the proper dimensions practically. As we have seen, the purpose of the horizontal tail is to create an opposite moment from the one created by the wing in order to re-establish an equilibrium for a particular flight attitude.

The designer could ask questions like: How quick should the action of the horizontal section be to re-establish equilibrium? How large should the stabilizing moment of the tail be over the unstabilizing moment of the wing? These questions are of great importance, but they are difficult to answer with great certainty. This is because the dynamic stability and not just the static stability has to be known. For this reason, it is not sufficient to consider the design by geometric and aerodynamic characteristics alone. Weight and the distribution of masses have to be considered as well.

Also, let’s not forget to consider the type of aircraft we are dealing with. Since it exploits air movements for its flight, the glider constantly flies in moving air. Thus it is very important—and natural in a sense—to make sure the airplane has excellent dynamic stability so that the pilot will not become exhausted by making attitude corrections.

Now, let’s analyze the factors that influence the determination of the horizontal tail area. We know that its function is to offset the moment of the wing. This moment depends on the movement of the center of pressure along the wing chord. For a wing of given airfoil and area, the longer the span the less the average chord, and the less the total movement of the center of pressure—the destabilizing moment of the wing. Moreover, at equal average chords, the moment depends on the wing area.

The wing area is the main factor used to establish the horizontal tail area.

Finally the third element in the determination of this area is the distance of the horizontal tail from the airplane’s center of gravity. The greater this distance, the greater the moment of the tail.

**Tail Ratio.** We can say that the horizontal tail area $S_{ht}$ depends essentially on three factors: (a) the area of the wing $S_w$, (b) the wing span, or the wing mean aerodynamic chord $MAC$, and (c) the distance $D_h$ of the center of pressure of the horizontal tail from the center of gravity of the aircraft. The relationship that ties these factors is the tail ratio $K$ (also called tail volumetric ratio), the ratio between the moments of the wing area and the horizontal tail area.

\[
K = \frac{S_w \cdot MAC}{S_t \cdot D_h} \quad [13]
\]
This is a constant characteristic for every aircraft, and accounts for factors that come into play in dynamic stability. Having $K$, we now can determine from the relationship the value for the tail area $S_t$:

$$S_t = \frac{S_w \cdot MAC}{K \cdot D_h} \quad [14]$$

Based on analysis of various gliders that have excellent stability, the value of $K$ can be set at 1.8 for small gliders with short fuselages and 2.2 for large gliders with long fuselages. As an average value, we can use a value of $K = 2$.

**Horizontal Tail Characteristics.** A symmetrical airfoil is always used for the horizontal tail. In its normal position, the horizontal tail establishes the airplane’s design attitude. A variation in the horizontal tail incidence will fix the airplane’s equilibrium at a different attitude. This change in incidence, or tail lift, is obtained by rotating the aft portion of the tail section up or down. The forward, fixed section is called the horizontal stabilizer; the rear movable section is called the elevator. The angle between the stabilizer and the elevator is the elevator angle. For gliders, the elevator angle is kept between $30^\circ$ for either climb or dive positions.

![Figure 4-6](image)

The rotational axis of the elevator is called the hinge axis. The hinge moment is the one generated by the aerodynamic reaction on the elevator in respect to the rotational axis. The pilot has to apply a force on the control stick, known at the *stick force*, in order to offset this moment.

![Figure 4-7](image)

To assist the pilot in such task, controls are sometimes aerodynamically balanced, or *compensated*. This is achieved by having some of the control surface in front of the hinge to create a hinge moment opposite to the one generated by the aft section.

However due to the low speed of gliders, the force at the stick is generally very small, therefore a compensated elevator is not required. On the contrary, at times the stick force is artificially increased by means of springs that tend to return the elevator to its normal neutral position. This is
done so the pilot’s sensations of control are not lost.

22. Lateral Stability
We must first understand that static lateral stability actually does not exist. After a rotation around the longitudinal axis, lift is always relative to the symmetrical plane, therefore no counteracting forces are present. A difference of lift between the wings is created only by the ailerons, but this is a pilot-generated action, and therefore we may not treat this as stability. We know for a fact however that a plane will have the tendency to automatically return to level flight following a change in attitude, but this because a sideslip motion is generated as an effect of the roll.

![Figure 4-8](image)

Let’s suppose for a moment that the center of lift and the center of gravity \( CG \) coincide in vertical location, and that a rotation around the longitudinal axis has taken place. Lift \( L \) is always on the longitudinal plane of symmetry but now does not coincide with the vertical plane through which \( CG \) and the weight force \( W \) are found. If we take the components of \( W, W' \) and \( W'' \)—\( W' \) being on the same plane as \( L \), and \( W'' \) perpendicular to it—we see that the effect of \( W'' \) is to give the aircraft a sideways movement, or slip. If the center of lift and the center of gravity coincide, then there will not be any forces able to straighten the aircraft.

![Figure 4-9](image)

If the wings are angled in respect to the horizontal (the *dihedral angle*), we will have a center of lift that is higher than the center of gravity, thus causing a moment that will have the tendency to level the aircraft. Moreover, due to the slip movement, the direction of the relative wind will no longer be parallel to the longitudinal axis, the down-going wing, due to the dihedral, will strike a flow of air at a greater angle of attack than the upper wing. The greater lift produced by the lower wing will roll the airplane back to his original position.

We have to keep in mind that these stabilizing effects are created only by the slippage movement which follows the initial roll movement.
Even without dihedral, a wing will have a dampening effect to the roll movement. In fact, when the aircraft rotates around the longitudinal axis, there is a second air velocity that affects the wing, the rotational velocity $V$. For the upper wing there is a decrease in incidence of the relative air flow, while for the lower wing there is an increase. Consequently we have an increasing lift in the lower wing (B) and a decreasing lift in the upper wing (A). An opposite moment to the original roll is therefore originated that will have the tendency to dampened the starting roll. Notice that as the original roll stops, so does the opposing roll because its origin was dynamic and due to the rotational velocity $V$. Together with all the factors we have seen that affect lateral stability, inertia due to forces of mass will enter into play as well. It is easy to understand how the analytical study of lateral stability could be a complex one. In practical terms however, to obtain a good lateral stability without exceeding to levels that may hinder handling capabilities, the dihedral may be 2°-4° for gliders with straight wings and gliders with average taper, the dihedral may be 4°-8° for the center section and 0°-1° for the outer panels.

23. Lateral Control Surfaces
To change the airplane’s equilibrium in the longitudinal axis, or to return the plane in the original position of equilibrium when the built-in stability is not sufficient, we have control surfaces that move in opposite directions on the outboard wing trailing edge. These are the ailerons, and their rotational movement changes the curvature of the wing and therefore the lift.
The down-aileron will increase lift while the raised one will decrease it, and this produces a rolling movement. However, the down-aileron will produce more drag than the up-aileron, which results in a yaw movement opposite to the one desired. This negative reaction is very perceptible in gliders due to their long wing span and low weight.

![Diagram of aileron action](image)

**Figure 4-12**

To eliminate this, the best method is to increase the drag of the up-aileron to compensate for the additional drag of the down-aileron. This is accomplished by extending the leading edge of the aileron so that it will extend below the surface of the wing when the aileron is up, but which will be inside the wing when the aileron is down. Ailerons on gliders are generally not aerodynamically compensated for the same reasons explained for the elevator.

**Wing Twist.** As we have seen, the lowering of the aileron will increase wing lift, but this is only true if the flight conditions are for less than maximum lift. If the aircraft is in flight conditions where the wings are producing maximum lift, as it is often the case in gliding, the lowering of an aileron will not increase wing lift. On the contrary, this could cause a sudden wing stall, possibly resulting in an entry into a spiral dive.

![Diagram of wing twist](image)

**Figure 4-13**

It is possible to eliminate such problems by twisting the wing negatively, in other words by building the wing so its extremities have a lower angle of attack than the wing center section. With this design, the ailerons will be more effective, even at a high angle of incidence.

With such a wing, the center portion will stall before the extremities. Because the ailerons are still very effective, there will still be sufficient lateral stability to prevent a spiral dive, even in the critical condition of an imminent stall.

Together with the wing twist, changes in the chord and thickness towards the wing tips are made to increase the overall stability and efficiency. In practice, the aerodynamic twist (relative to the incidence for maximum lift) is kept between 4 and 6 degrees in gliders. The geometric twist (relative to the airfoil chord line) turns out to be between 2 and 4 degrees, since the airfoils adopted for the wing tips generally have a higher incidence relative to the maximum lift than the airfoils used at the wing root.
Aileron Differential Ratio. By increasing the drag of the up-aileron in compensating for the negative moments, we would also worsen the aerodynamic characteristics of the wing. Therefore the idea is to reduce the increased drag of the down-aileron by reducing its angular travel when it is lowered. This is accomplished by designing a differential control system that causes the down-aileron to rotate at a lesser angle than the up-aileron.

This will not necessarily diminish the moment of roll. On the contrary, practice has shown that the up-aileron is more effective than the down-aileron, especially when reaching the conditions of maximum lift as we have previously mentioned. This differential control will give us a double advantage: a full, or nearly full, cancelling of the negative yaw moments, since the drag of the down-aileron with respect to the up-aileron is diminished, and an improvement in the lateral stability, especially at higher incidence, since reducing the movement of the down-aileron also reduces the chance to incurring a loss of wing lift.

In modern gliders, this differential is quite high, 1:3 in the case of one sailplane. For an average value, we can adopt a ratio of 1:2. The maximum rotational angles are 30 degrees for the up-aileron, and they vary between 10 and 15 degrees for the down-aileron.

24. Directional Stability
Directional stability is accomplished by installing a vertical tail surface, or fin and rudder, at the aft end of the fuselage. This location puts the resulting center of side-force lift behind the center of gravity, thus if the aircraft is turned about its vertical axis, a resulting stabilizing force will be generated that will return the aircraft to its original position.

We have to keep in mind, however, that a center of side-force lift that is too far behind the center of gravity is detrimental to the lateral stability, since a drop of the aft fuselage will result and a corrective action will be required, like increasing tail lift. But in such conditions an increased dihedral will be required also to prevent aircraft slip. Lateral and directional stabilities are therefore related to each other, and each has an effect on the other. Thus a large dihedral requires a larger vertical surface and vice versa.

The dimensions of the vertical surface are also dependent on the shape of the fuselage. The larger the keel effect of the fuselage, the smaller the required size of the vertical surface. On this subject we should remember that a fuselage of circular, or nearly circular, cross-section will have a rather a
low keel effect. It is not convenient for the fuselage to have a small circular section, and it is better to have a taller and flatter section for structural reasons. For the correct size of the vertical surfaces that insures static stability, you must rely on wind tunnel experiments for the particular model in question, try different sections and choose the most appropriate one. These results will not enough to guarantee stability; our concerns are with dynamic as well as static stability.

Since wind tunnel tests are not very practical for these kind of aircraft, the only avenue left is a comparison with similar existing aircraft that are known to have good flight characteristics.

25. Vertical Empennage
From the examination of various gliders, we have obtained an empirical formula for the determination of the area of the vertical tail that may be used as a first approximation. This formula takes in account the wing span, the distance of the surface hinge from the center of gravity and the total weight of the aircraft.

\[ S_{vt} = K \frac{W \cdot b}{D_h^2} \]  

[15]

where \( S_{vt} \) is the area of vertical tail in square meters, \( b \) is the wing span in meters, \( W \) is the total aircraft weight in kg, and \( d_h \) is the distance of rudder hinge line from the center of gravity. The coefficient \( K \) may have the following values: 0.0035 for small gliders with short wing spans, 0.004 for medium-size gliders, and 0.0045 for large gliders with long wings.

**Vertical Tail Features.** As in the case of the horizontal tail, symmetrical airfoils are always used to produce the same aerodynamic reaction on both sides of the aircraft from the same amount of angular movement. In the vertical empennage, the fin is a fixed forward part, and the rudder is a moveable surface.

**Rudder Area.** In gliders, the area of the rudder is always a large percentage of the vertical tail area, generally between 60%-75%, and the rudder is normally the only control surface that is aerodynamically compensated. The percent of compensating area is normally between 15%-20% of the rudder. The angle of movement is generally 30 degrees to either side.
Chapter 5
Mechanics of Flight

26. Glide Angle and Glide Ratio
To understand the flight of a glider, we will set up a simplified situation. Let’s stipulate that the flight is performed in calm air, in a straight line, and at a constant velocity. In these conditions, we have a flight path that follows a linear slope at angle $\varphi$, called the glide angle.

The forces that act on the airplane are the weight $W$ and the aerodynamic force $F$. For any attitude, we will have equilibrium when these forces are on the same vertical line ($W$ is always vertical), intersect the center of gravity $CG$, are opposite, and have the same magnitude. Consequently, the moment of these two forces in relation to any point in space will be nil. For simplicity, we will further suppose that the point where force $F$ is applied is also the center of gravity $CG$.

Let’s consider the components of the forces $F$ and $W$ in relation to two directions, one vertical and one parallel to the flight direction. The $F$ components are the lift $L$ and the drag $D$. The components for $W$ are $W'$ and thrust $T$, and they will be opposite to $L$ and $D$. The thrust $T$ determines the motion along the trajectory and depends on the glide angle $\varphi$ and the weight $W$. In the diagram, we can see how the triangles $F-CG-L$ and $W-CG-W'$ are equal and similar to the triangle $ABC$. Consequently,

$$\frac{L}{D} = \frac{d}{h}$$
knowing that

\[ \frac{L}{D} = \frac{C_L}{C_D} = E \]

we also know that

\[ \frac{d}{h} = E \quad [16] \]

The ratio \( d/h \) is called glide ratio, and its value represents the aerodynamic efficiency \( E \) as well. Its reciprocal, \( h/d \), represents the trajectory slope \( p \).

\[ p = \frac{h}{d} = \frac{1}{E} \quad [17] \]

which is trigonometrically expressed as

\[ p = \frac{h}{d} = \tan \phi \quad [17'] \]

To summarize, the greater the efficiency \( E \), the smaller the trajectory slope. Therefore, for a given altitude loss, the distance travelled \( d \) is proportional to the efficiency \( E \).

### 27. Horizontal and Vertical Speeds

Velocity \( V \) on the trajectory is due to the thrust \( T \), a component of the weight \( W \), in the direction of motion. In equilibrium conditions, \( T = D \), thus

\[ T = D = C_d \cdot \rho \cdot S_w \cdot V^2 \]

from which we have

\[ V = \sqrt{\frac{T}{C_d \cdot \rho \cdot S_w}} \]

which can be calculated from the other equation as

\[ L = C_L \cdot \rho \cdot S_w \cdot V^2 \]

therefore

\[ V = \sqrt{\frac{L}{C_L \cdot \rho \cdot S_w}} \]

Since \( L = W \cos \phi \), we have the more practical equation that will give us the velocity as a function of the wing loading \( W/S_w \).
The Glider

Figure 5-3

\[ V = \sqrt{\frac{W}{S_w} \cdot \cos \varphi \cdot \frac{1}{\rho \cdot C_L}} \]  \[18\]

From the velocities triangle we can see that the horizontal and vertical velocities are

\[ V_x = V \cdot \cos \varphi \]
\[ V_y = V \cdot \sin \varphi \]

therefore, from formula 18 we know that the horizontal velocity \(V_x\) is

\[ V_x = V \cdot \cos \varphi = \cos \varphi \cdot \sqrt{\frac{W}{S_w} \cdot \cos \varphi \cdot \frac{1}{\rho \cdot C_L}} \]  \[18'\]

and \(V_y\), the vertical component of \(V\), is

\[ V_y = V \cdot \sin \varphi = \sin \varphi \cdot \sqrt{\frac{W}{S_w} \cdot \cos \varphi \cdot \frac{1}{\rho \cdot C_L}} \]  \[18''\]

or

\[ V_y = \frac{V_x}{E} = \frac{1}{E} \cdot \sqrt{\frac{W}{S_w} \cdot \cos \varphi \cdot \frac{1}{\rho \cdot C_L}} \]  \[18'''\]

On normal flight attitudes though, angle \(\varphi\) is very small. For an example, given a standard value of efficiency for a glider of \(E = 20\), we know that \(1/E = \tan \varphi\) or \(\tan \varphi = 1/20 = 0.05\). From trigonometric tables, we find the value of angle \(\varphi = 2^\circ 50'\), which corresponds to a value of \(\cos \varphi = 0.99878\). For normal flight attitudes, we can use a value of 1 for \(\cos \varphi\) without introducing too much of an error. The equations will then be

\[ V_x = \sqrt{\frac{W}{S_w} \cdot \frac{1}{\rho \cdot C_L}} \]  \[19\]

\[ V_y = \frac{1}{E} \sqrt{\frac{W}{S_w} \cdot \frac{1}{\rho \cdot C_L}} \]  \[20\]

These are the formulas of current use for the calculation of both the horizontal and vertical speeds of a glider in a linear and uniform flight.

Stelio Frati  
5-3  
Mechanics of Flight
From the previous relation, for the wing loading $W/S_w$ and the air density at a constant altitude, at any given value of attitude $C_L$, we have velocities $V_x$ and $V_y$. Of all these values, the only ones of interest in the case of the glider are the minimum horizontal speed, the minimum vertical speed, and the top speed in a dive. The minimum horizontal speed can be easily calculated from formula 19 with the maximum coefficient of lift $C_{L_{\text{max}}}$.

$$V_{x_{\text{min}}} = \frac{W}{S_w} \cdot \frac{1}{\rho} \cdot \frac{1}{C_{L_{\text{max}}}}$$

[21]

To determine the minimum speed of descent, formula 20 is written

$$V_{y_{\text{min}}} = \left( \frac{W}{S_w} \cdot \frac{1}{\rho} \right) \cdot \frac{1}{E \cdot \sqrt{C_L}}$$

In this equation, we know that the factor that is rooted is constant for a certain altitude. It follows that velocity $V_y$ is dependent on the factor $E \cdot \sqrt{C_L}$.

The Power Factor
The velocity of descent $V_y$ will be lowest at an attitude where the factor $E \cdot \sqrt{C_L}$ is at a maximum value. This is because

$$E = \frac{C_L}{C_d}$$

thus

$$E \cdot \sqrt{C_L} = \frac{C_L}{C_d} \cdot \sqrt{C_L} = \frac{C_L^{\frac{3}{2}}}{C_d}$$

In other words, the velocity of descent will be at its lowest when the factor $C_L^{\frac{3}{2}}/C_d$ is at its maximum. This is called the power factor, since the power required to maintain horizontal flight at any given attitude is inversely proportional to it.
29. Top Speed in a Dive

![Figure 5-4](image)

In the flight attitude shown above, the aerodynamic force $F$ is in the direction of the trajectory since $C_L = 0$. Thus $F$ is directly in line with $D$ and equals the weight $W$. The equations are $W = D$ and $L = 0$, thus

$$W = C_d \cdot \rho \cdot S_w \cdot V^2$$

The velocity on the trajectory coincides with the velocity of descent $V_y$, so $\varphi = 90^\circ$, $\cos \varphi = 0$, and $\sin \varphi = 1$, therefore

$$V_y = V \cdot \sin \varphi = V = \sqrt{\frac{W}{S_w} \cdot \frac{1}{\rho} \cdot \frac{1}{C_{do}}} \quad [22]$$

where $C_{do}$ is the coefficient of drag at zero lift.

This top speed is important for safety considerations of the airplane’s structure. Aerodynamic brakes have been used, if the top speed reaches a value that can compromise the glider’s structural strength.
Chapter 6
Applied Aerodynamics

Wing airfoils can be classified in three categories from the geometric point of view: thick airfoils with relative thickness greater than 15%, medium airfoils with relative thickness between 12% to 15%, and thin airfoils with relative thickness less than 12%.

When choosing an airfoil, we should not consider the aerodynamics characteristics alone. We also have to take into account the requirements of the construction.

In the case of gliders, the wing span is always considerable, thus the selection would be made from medium, or even thick, airfoils. It is important that the airfoil be of sufficient thickness so that the strength-to-weight ratio of the spar is not compromised—particularly at the point where the wing meets the fuselage.

The airfoil’s thickness is therefore established by considering both the aerodynamics as well as the construction.

Among these, we particularly take into consideration the following:

1. Maximum value of the lift coefficient $C_{L_{\text{max}}}$ This is the factor that directly influences the minimum velocity.
2. Maximum value of efficiency $E = C_l / C_d$. As we have previously seen, this is of utmost importance, especially for gliders.
3. Maximum value of the power factor. $C_t^{3/2} / C_d$ This index measures the quality of climb and the velocity of sink. The higher the value, the lower the power required to maintain flight. Therefore, the higher the value the lower the sink velocity $V_s$.
4. Minimum value of the moment's coefficient for zero lift $C_{M_0}$. This factor is the index of stability of the airfoil, and it gives the movement of the center of pressure. If its value is negative, it means that the airfoil is stable.

It is not necessary to find an airfoil that simultaneously satisfies all these requirements, and some of them offset each other. For example, airfoils with a high value of $C_{L_{\text{max}}}$ have generally a high value of $C_{M_0}$, that is they have a considerable movement of the center of pressure.

Therefore to obtain the best compromise between the various characteristics we turn to a combination of different airfoils. The wing is seldom of constant airfoil, particularly in gliders. At the fuselage as we have seen, even for construction reasons, a thick airfoil with high lift will be convenient. At the tips, however, a thinner and more stable airfoil, with low drag and small pitching moment, will be necessary to reduce losses and increase stability and handling qualities.

Let’s understand that, if there is doubt in selecting a single airfoil for the wing, the doubt will be greater when selecting more than one airfoil. For this reason it is not possible to tell which will be the best airfoil for a glider. To all these factors that may influence the selection, such as the particular type and use of a glider, we have to add the designer’s own preferences.
As we saw in Chapter 1 when considering the characteristics of the various gliders, there is a great variety in the design of the wing airfoils. We go from the concave convex airfoil to the biconvex asymmetric airfoil for gliders with same architecture and same use. Until ten years ago the most common design were the concave convex airfoil, which presented optimum characteristics of efficiency and minimum sink speed, but lower horizontal speed and little longitudinal stability. On the contrary, today we see the use of airfoils with little curvature or even biconvex asymmetric. In concluding, we can say generally that thick, curved airfoils constant throughout the full wing span, are the most convenient for recreational gliders.

For training gliders, the curved airfoils but with varying extremities to the biconvex asymmetric or symmetric, are still preferred. For competition gliders, the preference goes to the semi-thick, and much faster, airfoils. For the tail section, there is not much doubt, since the biconvex symmetric design is always used with thicknesses ranging from 10% to 12%.

31. Airframe Components and Drag.
We will now discuss the coefficients of drag of some of the airframe components. As stated earlier, these coefficients are based on the largest cross section perpendicular to the flight direction.

Flat Rectangular Sections. The drag coefficient $C_d$ of a flat surface is a function of its length and Reynolds number. For isolated flat surfaces, $C_d = 0.65$. For flat controlling surfaces, (considering the wing interference), $C_d = 0.85$ as an average value for normal Reynolds numbers found in such aircraft.

Wires, Cables and Extrusions. For round wire normal to the wind, the drag coefficient is $C_d = 0.60$. For cables of non-regular section, $C_d = 0.72$. Due to the high drag generated by wires and cables, they are often substituted with extrusions, generally with lenticular section, which is a good aerodynamic shape and also rather easy to fabricate. The coefficient for such an extrusion is $C_d = 0.20$.

Shaped Supports. In gliders, all of the supports could be made of round steel tubes, but generally in order to reduce the drag, an extrusion or a wood shape with a metal core is used. We will show the drag coefficients for various cross sectional shapes.

As we can see, if the length of the section is increased in relation to its thickness, the drag coefficient also increases. The optimum value for the section’s length is three times its thickness. In the following table, the values for sections with their major axis at incidence angles of $0^\circ$, $5^\circ$ and $10^\circ$ are shown. As you can see, the drag increases with the incidence angle.
The Fuselage. Due to the large number of possible fuselage designs, it is very difficult to establish the drag of a new design without conducting wind tunnel tests, however as a rough approximation, you can establish the drag coefficient of a fuselage by comparing it to a similar one with known characteristics.

The shape of the fuselage is rather simple from the standpoint of construction, but experimental results are lacking. The drag coefficients that we show here do not pertain to any particular glider, but they could be used as a reference to understand the magnitude of these values.
In these three shapes, note that there is little difference in the minimum drag. You could assume that the section design has no bearing on the outcome. But let’s notice the importance the shape of section assumes once the angle of incidence is increased—with an angle of 10° in respect to the fuselage axis, there is an increase of the minimal drag of 230% if the section is square, while it will not reach 33% if the section is circular. Drag coefficients values for fuselage with open cockpit can vary from 0.09 to 0.18.

Two types of fuselage with open cockpits are shown above, one with a rectangular section, the second with a circular section. For a fuselage with a closed cockpit, drag coefficients can be achieved from 0.045 to 0.050.

For the fuselage here above, the following drag coefficients were found: 0.044 at 0° incidence, 0.071 at 10° incidence, and 0.1545 at 20° incidence. As you can see, the drag increases considerably with an increase of the angle of incidence, especially with a fuselage of square or polygonal shape.

As an approximation, we can establish the coefficients of drag of 0.08 to 0.10 for a polygonal shape fuselage with open cockpit, 0.07 to 0.08 for the same but with a closed cockpit and 0.04 to 0.05 for a curved, plywood-skinned fuselage.

Wheels. For drag coefficient for low pressure wheels that are usually used in gliders, we can use \( C_d = 0.15 \) where the section considered is obtained by multiplying the wheel diameter by the largest wheel width. In gliders, the wheels—normally one—are always
partly masked by the fuselage, but we can assume the drag for the wheel in its entirety considering the interference with the fuselage.

32. Summary

Sample of an Aerodynamic Calculation for a glider. Let us try a simple example of the aerodynamic calculation of the flight characteristics of a glider. The aircraft will be a glider with a 15 meter wing span. The basic data is:

<table>
<thead>
<tr>
<th>Component</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wing Span</td>
<td>15 m</td>
</tr>
<tr>
<td>Area</td>
<td>15 m²</td>
</tr>
<tr>
<td>Aspect ratio</td>
<td>15</td>
</tr>
<tr>
<td>Chord, root</td>
<td>1.4 m</td>
</tr>
<tr>
<td>Chord, tip</td>
<td>0.6 m</td>
</tr>
<tr>
<td>Airfoil, root</td>
<td>NACA 4415</td>
</tr>
<tr>
<td>Airfoil, tip</td>
<td>NACA 2R₁₁₂</td>
</tr>
<tr>
<td>Angle of incidence</td>
<td>Root 0°, Tip –3°</td>
</tr>
<tr>
<td>Tail Horizontal area</td>
<td>2.1 m²</td>
</tr>
<tr>
<td>Vertical area</td>
<td>0.9 m²</td>
</tr>
<tr>
<td>Airfoil</td>
<td>NACA M3</td>
</tr>
<tr>
<td>Fuselage Max cross-section</td>
<td>0.48 m²</td>
</tr>
<tr>
<td>Total weight</td>
<td>250 kg.</td>
</tr>
<tr>
<td>Wing loading</td>
<td>16.7 kg/m²</td>
</tr>
</tbody>
</table>

The architecture is for a glider with high wing with trapezoidal shape, and a monocoque fuselage with plywood skin. The cockpit is closed, well-streamlined and faired to the fuselage. The glider has a ski and a wheel that is partially protruding.

Aerodynamic Characteristic of the Wing. Let us start our calculation with the most important component both aerodynamically and by construction, the wing. From the data we see that the airfoil is the NACA 4415 at the wing root and NACA 2R₁₁₂ at the tip with a 3° twist. The wing has, in other words, a negative twist of 3°. The airfoil variation from the fuselage to the tips is linear. From the airfoil tables, we get the values of the aerodynamic characteristics $C_L$, $C_d$, $C_m$ for an aspect ratio of 5.

![Figure 6-5](image-url)
Let’s consider the wing by disregarding any tip radiuses. Let’s obtain the reduced coefficients for the two airfoils. The partial areas $S_1'$ and $S_2'$ are:

\[
S_1' = \frac{1.40 + \left( \frac{1.40 + 0.60}{2} \right)}{2} \cdot 3.75 = 4.5 \text{ m}^2
\]
\[
S_2' = \frac{\left( \frac{1.40 + 0.60}{2} \right) + 0.60}{2} \cdot 3.75 = 3 \text{ m}^2
\]

The wing area is:

\[S = 15 \text{ m}^2\]

Therefore the reduced coefficients are, for NACA 4415:

\[
\frac{2 \cdot S_1'}{S} = \frac{9}{15} = 0.60
\]

and for NACA 2R12

\[
\frac{2 \cdot S_2'}{S} = \frac{6}{15} = 0.40
\]

For clarity, let’s make a table with the values of $C_L$ and $C_d$ for an aspect ratio of 5 for the two airfoils and include the new calculated values with reduced coefficients.

<table>
<thead>
<tr>
<th>$\alpha^\circ$</th>
<th>$C_L$</th>
<th>$C_d$</th>
<th>$0.6 C_L$</th>
<th>$0.6 C_d$</th>
</tr>
</thead>
<tbody>
<tr>
<td>-3</td>
<td>0.55</td>
<td>0.0055</td>
<td>0.033</td>
<td>0.0033</td>
</tr>
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<td>0.0390</td>
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<td>0.0855</td>
<td>0.445</td>
<td>0.0513</td>
</tr>
<tr>
<td>20</td>
<td>0.785</td>
<td>0.1096</td>
<td>0.472</td>
<td>0.0657</td>
</tr>
</tbody>
</table>

NACA 4415
We now know the reduced coefficients $C_L$ and $C_d$. To obtain the coefficient for the complete wing, all we have to do is add these together taking into account that the airfoil at the tip, NACA 2R112, is twisted at $-3^\circ$ in relation to the airfoil at the wing root, NACA 4415. For example, at $0^\circ$ we have

$$C_L = 0.082 + (-0.024) = 0.058$$
$$C_d = 0.045 + 0.018 = 0.063$$

The values obtained and the one for efficiency $E = C_L/C_d$ are shown in the following table

<table>
<thead>
<tr>
<th>$\alpha^\circ$</th>
<th>$C_L$</th>
<th>$C_d$</th>
<th>$E$</th>
</tr>
</thead>
<tbody>
<tr>
<td>-3</td>
<td>0.058</td>
<td>0.0063</td>
<td>9.2</td>
</tr>
<tr>
<td>0</td>
<td>0.163</td>
<td>0.0095</td>
<td>17.2</td>
</tr>
<tr>
<td>6</td>
<td>0.262</td>
<td>0.0156</td>
<td>16.8</td>
</tr>
<tr>
<td>9</td>
<td>0.389</td>
<td>0.0254</td>
<td>15.3</td>
</tr>
<tr>
<td>12</td>
<td>0.495</td>
<td>0.0395</td>
<td>12.5</td>
</tr>
<tr>
<td>15</td>
<td>0.589</td>
<td>0.0535</td>
<td>11.0</td>
</tr>
<tr>
<td>18</td>
<td>0.681</td>
<td>0.0727</td>
<td>9.3</td>
</tr>
<tr>
<td>21</td>
<td>0.746</td>
<td>0.0947</td>
<td>7.9</td>
</tr>
</tbody>
</table>

In these calculations, great precision is not important. Calculating to the third or fourth decimal place is useless if you think of the number of unknowns caused by the interference of various elements, all of which would be impossible to take into account. For example, establishing that the plane’s minimum sink rate is of 0.6784 m/s or of 0.68 m/s is exactly the same thing. Therefore has you have probably already noticed, the values are rounded off.

We have calculated the values for $C_L$, $C_d$ and $E$ for an aspect ratio of 5.

We must now calculate the change in these values for the aspect ratio of our example. We’ll disregard the variation relative to $C_L$, because it’s too small be of consequence. But let’s calculate the change in the drag

$$\Delta C_d = \frac{2C_L^2}{\pi} \left( \frac{1}{AR_1} - \frac{1}{AR_2} \right)$$
where AR₁ and AR₂ are the values of the aspect ratio between which the variation exists. In our case, AR₁ = 5 and AR₂ = 15, we have

$$\Delta C_d = \frac{2C_L^2}{3.14} \left( \frac{1}{5} - \frac{1}{15} \right) = 0.085C_L^2$$

at each value of $\alpha$, thus for $C_L$, we have the value of correction for drag.

For example at $\alpha = 0$, $C_L = 0.058$ so we have:

$$\Delta C_d = 0.085 \cdot 0.058^2 = 0.0003$$

and the value for $C_d'$ for $AR = 15$ is:

$$C_d' = C_d - \Delta C_d = 0.0063 - 0.0003 = 0.006$$

All the $\Delta C_d$ are therefore calculated for all the values of $C_L$.

In the following table we see the coefficients $C_d$ for $AR = 5$, the change $\Delta C_d$, and the resultant values $C_d'$.

<table>
<thead>
<tr>
<th>$\alpha^\circ$</th>
<th>$C_d$ $\text{AR = 5}$</th>
<th>$\Delta C_d$ $\text{AR = 15}$</th>
<th>$C_d'$ $\text{AR = 15}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>–3</td>
<td>.0067</td>
<td>.0001</td>
<td>.0066</td>
</tr>
<tr>
<td>0</td>
<td>.0063</td>
<td>.0003</td>
<td>.0060</td>
</tr>
<tr>
<td>3</td>
<td>.0095</td>
<td>.0022</td>
<td>.0073</td>
</tr>
<tr>
<td>6</td>
<td>.0156</td>
<td>.0058</td>
<td>.0098</td>
</tr>
<tr>
<td>9</td>
<td>.0254</td>
<td>.0118</td>
<td>.0136</td>
</tr>
<tr>
<td>12</td>
<td>.0395</td>
<td>.0208</td>
<td>.0187</td>
</tr>
<tr>
<td>15</td>
<td>.0535</td>
<td>.0295</td>
<td>.0240</td>
</tr>
<tr>
<td>18</td>
<td>.0727</td>
<td>.0395</td>
<td>.0332</td>
</tr>
<tr>
<td>21</td>
<td>.0947</td>
<td>.0472</td>
<td>.0475</td>
</tr>
</tbody>
</table>

As a result we may now have the characteristics $C_L$, $C_d'$, and $E$ for the complete wing for an aspect ratio of 15.

<table>
<thead>
<tr>
<th>$\alpha^\circ$</th>
<th>$C_L$</th>
<th>$C_d$</th>
<th>$E$</th>
</tr>
</thead>
<tbody>
<tr>
<td>–3</td>
<td>.025</td>
<td>.0066</td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>.058</td>
<td>.0060</td>
<td>9.7</td>
</tr>
<tr>
<td>3</td>
<td>.163</td>
<td>.0073</td>
<td>22.3</td>
</tr>
<tr>
<td>6</td>
<td>.262</td>
<td>.0098</td>
<td>26.7</td>
</tr>
<tr>
<td>9</td>
<td>.389</td>
<td>.0136</td>
<td>28.6</td>
</tr>
<tr>
<td>12</td>
<td>.495</td>
<td>.0187</td>
<td>26.5</td>
</tr>
<tr>
<td>15</td>
<td>.589</td>
<td>.0240</td>
<td>24.5</td>
</tr>
<tr>
<td>18</td>
<td>.681</td>
<td>.0332</td>
<td>20.5</td>
</tr>
<tr>
<td>21</td>
<td>.746</td>
<td>.0475</td>
<td>15.7</td>
</tr>
</tbody>
</table>
**Characteristics of the Complete Glider.** To obtain the aerodynamic characteristics of the complete aircraft, you must add to the wing's lift and drag values those of the various other elements that make up the glider, such as the fuselage, empennage, landing gear, bracing struts, etc. In our example, we will ignore the lift components of these elements.

**Additional Coefficients.** To determine the additional coefficients of drag, let the fuselage with skid be $C_d = 0.05$ and since the fuselage cross-section $s$ is $0.48 \text{m}^2$, its coefficient to be added will be

$$C_{df} = C_d \cdot \frac{s}{S} = 0.05 \cdot \frac{0.48}{15} = 0.0016$$

where the wing area $S = 15 \text{m}^2$.

The minimum drag coefficient of the empennage airfoil NACA M.3 is $C_d = 0.004$ and since the empennage surface $S_t$ is $2.10 + 0.9 = 3 \text{m}^2$, the additional $C_{dt}$ will be

$$C_{dt} = 0.004 \cdot \frac{3}{15} = 0.0008$$

And for the wheel, let its dimension be $300 \times 100$ and the drag coefficient = 0.15. Since its calculated cross-sectional area is $0.03 \text{m}^2$, the additional $C_{dlg}$ is

$$C_{dlg} = 0.15 \cdot \frac{0.03}{15} = 0.0003$$

that we will use in its entirety even through the wheel is only protruding half way. This is to take into consideration the interference drag with the fuselage.

The additional total coefficient $C_{dT}$ will then be $C_{df} + C_{dt} + C_{dlg}$

$$C_{dT} = C_{df} + C_{dt} + C_{dlg}$$

$$C_{dT} = 0.0016 + 0.0008 + 0.0003 = 0.0027$$

that we will slightly increase to allow for interferences and set it at

$$C_{dT} = 0.003$$

By adding this constant value to the value of $C_d$ of the wing in the various configurations we are left with the coefficient of drag for the total aircraft.

As we have previously mentioned this procedure is not exact, since it does not take into account for the additional changes in drag caused by interference.

These changes, while almost negligible at small angles of incidence, will increase at higher angles of incidence and may even double at angles of incidence over $15^\circ$. Since you cannot obtain exact data on fuselages, it is simpler to proceed in this manner, even if it is not precise and add a constant value for additional drag.
The characteristics of the complete aircraft are thus

<table>
<thead>
<tr>
<th>$\alpha^2$</th>
<th>$C_L$</th>
<th>$C_d$</th>
<th>$E$</th>
</tr>
</thead>
<tbody>
<tr>
<td>-3</td>
<td>-0.025</td>
<td>0.0096</td>
<td>—</td>
</tr>
<tr>
<td>0</td>
<td>0.058</td>
<td>0.0090</td>
<td>6.4</td>
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<tr>
<td>3</td>
<td>0.163</td>
<td>0.0103</td>
<td>15.8</td>
</tr>
<tr>
<td>6</td>
<td>0.262</td>
<td>0.0128</td>
<td>20.5</td>
</tr>
<tr>
<td>9</td>
<td>0.389</td>
<td>0.0166</td>
<td>23.6</td>
</tr>
<tr>
<td>12</td>
<td>0.485</td>
<td>0.0217</td>
<td>22.8</td>
</tr>
<tr>
<td>15</td>
<td>0.589</td>
<td>0.0270</td>
<td>21.9</td>
</tr>
<tr>
<td>18</td>
<td>0.681</td>
<td>0.0362</td>
<td>18.8</td>
</tr>
<tr>
<td>21</td>
<td>0.746</td>
<td>0.0505</td>
<td>14.8</td>
</tr>
</tbody>
</table>

We can observe how the value 23.6 for maximum efficiency $E$ is similar to the total efficiency of other gliders of this category, which average around the 24 mark.

**Flight Characteristics Determination.** Let us now calculate the horizontal and vertical velocity, $V_x$ and $V_y$, at different aspect ratios at sea level. These velocities are given by the following relations:

$$V_x = \sqrt{\frac{W}{S} \cdot \frac{1}{\rho} \cdot \frac{1}{C_L}} \text{ m/sec}$$

$$V_y = \frac{1}{E} \sqrt{\frac{W}{S} \cdot \frac{1}{\rho} \cdot \frac{1}{C_L}} \text{ m/sec}$$

where:

- $W/S = $ wing loading = 16.7 Kg/m$^2$
- $\rho = $ air density = 0.125 at sea level

therefore the horizontal velocity will be:

$$V_x = \sqrt{16.7 \cdot \frac{1}{0.125} \cdot \frac{1}{C_L}}$$

where

$$V_x = 11.5 \cdot \frac{1}{\sqrt{C_L}} \text{ m/sec}$$

then in Km/h

$$V_x = 11.5 \cdot 3.6 \cdot \frac{1}{\sqrt{C_L}}$$
or

\[ V_x = 41.4 \cdot \frac{1}{\sqrt{C_L}} \]

For instance for \( \alpha = 3^\circ \), the \( C_L = 0.163 \), therefore

\[ V_x = 41.4 \cdot \frac{1}{\sqrt{0.163}} = 102 \text{ Km} / \text{h} \]

In this manner, you calculate all of the horizontal speeds for the various angles of incidences and put them in a table.

Then to obtain the sink rate \( V_y \), all you have to do is to divide the horizontal speed by the respective efficiencies \( E \). However, since the sink rate is expressed in m/sec, and the horizontal speed is in Km/h, we will have to divide by 3.6. We’ll then have:

\[ V_y = \frac{V_x}{E \cdot 3.6} \]

for the previous example of \( \alpha = 3^\circ \), we have \( V_x = 102 \text{ Km/h} \) and \( E = 15.8 \), thus

\[ V_y = \frac{102}{15.8 \cdot 3.6} = 1.89 \text{ m/sec} \]

The results are tabulated together with the horizontal velocities.

<table>
<thead>
<tr>
<th>( \alpha^\circ )</th>
<th>( E )</th>
<th>( V_x )</th>
<th>( V_y )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>6.4</td>
<td>172</td>
<td>7.5</td>
</tr>
<tr>
<td>3</td>
<td>15.8</td>
<td>102</td>
<td>1.80</td>
</tr>
<tr>
<td>6</td>
<td>20.5</td>
<td>81</td>
<td>1.10</td>
</tr>
<tr>
<td>9</td>
<td>23.6</td>
<td>66.5</td>
<td>0.78</td>
</tr>
<tr>
<td>12</td>
<td>22.8</td>
<td>59</td>
<td>0.72</td>
</tr>
<tr>
<td>15</td>
<td>21.9</td>
<td>54</td>
<td>0.68</td>
</tr>
<tr>
<td>18</td>
<td>18.8</td>
<td>50.5</td>
<td>0.74</td>
</tr>
<tr>
<td>21</td>
<td>14.8</td>
<td>48</td>
<td>0.90</td>
</tr>
</tbody>
</table>

The characteristics of \( E \) and \( V_y \) for our glider are reasonably good; not because of their absolute values, but because of their relation to the horizontal speeds. For example, at a velocity of 81 Km/h, the efficiency is 20.5 and the sink rate is is 1.10 m/sec. These are good for the gliding distance. At the efficiency’s maximum value, \( E = 23.6 \) we still have a substantial horizontal velocity and a low sink rate; while at the minimum sink velocity, \( V_y = 0.68 \) we still have an optimum efficiency value.

To get a quick view of the glider’s characteristics the results are plotted in the diagrams shown in Figures 6-6 and 6-7.
Figure 6-6

Figure 6-7
Maximum Speed in a Dive. Let us calculate now the maximum speed that the glider will reach in a prolonged dive. As we have seen this is given by the equation:

\[ V_{y_{\text{max}}} = \sqrt{\frac{W}{S}} \cdot \frac{1}{\rho} \cdot \frac{1}{C_{do}} \]

expressed in m/sec, where \( C_{do} \) is the coefficient of drag at zero lift. From the chart, at \( C_L = 0 \), \( C_{do} = .0096 \), where

\[ V_{y_{\text{max}}} = 11.5 \cdot \frac{1}{\sqrt{0.0096}} \cdot 3.6 \]

expressed in Km/h, therefore:

\[ V_{y_{\text{max}}} = 425 \text{Km/h} \]

which is a very dangerous high speed if reached in actual flight.

Sizing of Wing Spoilers. From an aerodynamic point of view, the proper sizing of the spoilers is very important, since the spoilers are used as brakes to limit the speed in a dive. In our previous calculation, we have determined the maximum speed in a dive, and we can see that this speed is very high for this type of aircraft, and if it is reached in actual flight, the overall structural integrity of the glider would be compromised. Therefore we must be able to limit this speed, which at times might be reached inadvertently or unavoidably. In normal gliders, the speed is kept to around 200-220 Km/h for safety reasons, and spoilers are used as brakes.

To calculate the size of the spoilers, we return to the equation given for the maximum speed:

\[ V_{y_{\text{max}}} = \sqrt{\frac{W}{S}} \cdot \frac{1}{\rho} \cdot \frac{1}{C_{dt}} \]

where \( C_{dt} \) is the total drag of the aircraft plus the spoiler’s drag, which is yet to be calculated, while \( V_{y_{\text{max}}} \) is the never-exceed speed set by the designer. Since the aircraft’s drag at zero lift, \( C_{L0} \) is known, from the previous equation we can calculate the total drag. The difference between the values will be the spoiler’s drag. Then knowing the drag coefficient for the spoilers, their surface area can be calculated.

Let’s calculate the size of the spoilers for the glider in our example, keeping in mind that we want to limit its speed in a dive to 200 Km/h. We have

\[ \frac{1}{\sqrt{C_{dt}}} = V_{y_{\text{max}}} \cdot \frac{1}{\sqrt{\frac{W}{S}}} \cdot \frac{1}{\rho} \]
or

\[ \sqrt{C_{dt}} = \sqrt{\frac{W \cdot 1}{S \cdot \rho \cdot V_{y_{\text{max}}}}} \cdot 3.6 \]

epressed in Km/h. Substituting with numeric values:

\[ \sqrt{C_{dt}} = \frac{11.5 \cdot 3.6}{200} = 0.207 \]

squaring this we find that \( C_{dt} = 0.0429 \). Since we know that the drag coefficient of the aircraft at zero lift is 0.0096, the drag for the spoilers will be \( C_{ds} = 0.0429 - 0.0096 = 0.0333 \). This coefficient of drag is additional and is a coefficient of the wing area therefore:

\[ C_{ds} = C_d \cdot \frac{s}{S} \]

where:

- \( S = 15 \text{ m}^2 \) = Wing area
- \( s = \) unknown area of the spoilers
- \( C_d = 0.0085 \) = drag coefficient of a rectangular plate

The total area \( s \) for the spoilers is then:

\[ s = \frac{C_{ds} \cdot S}{C_d} = \frac{0.0333 \cdot 15}{0.0085} = 0.59 \text{ m}^2 \]

With a spoiler surface on the top and bottom of each wing, we’ll have four elements, therefore the area of each spoiler will be 0.59/4 or 0.148m², so we can use spoilers measuring 165 x 900mm. We can see how the effect of these surfaces as true brakes is remarkable, and the design of the controls for such spoilers is also very important in order to prevent excessive loading on their deployment.
33. General Considerations
In the design process, it is extremely important to know in advance where the machine is going to be used. Poorly defined plans will always bring mediocre solutions.

Therefore in designing a glider, we should have a precise understanding of its use, and thus the desired aerodynamic characteristics and construction features. When defining these, the designer’s biases are naturally present, and it is in this phase of the design that it is preferable that common sense be combined with lots of experience. A mistake at this stage will hurt the quality of flight or the overall production cost.

When the designer has little experience, it’s a good idea to follow the example of existing designs and learn from the experience of others in this phase of the project. It is not a good idea to attempt something new if you have little experience. The ‘new’ always brings unknowns, even with expert designers.

And you should consider the practicalities of construction. It is better to build a well-constructed basic design than a poorly-constructed competition sailplane, which would be totally useless and would cost at least three times as much.

34. Wing Span
We have seen how the wing span is an index of the classification of gliders, which may be put into the following categories: (a) basic low-performance gliders with a wing span of 10 meters, (b) medium-performance gliders with a wing span of 15 meters, and (c) high-performance sailplanes with a wing span of 18 to 20 meters and above.

Another very important factor in classifying a glider is the wing aspect ratio.

The total weight of the proposed glider should be established using similar existing gliders that have good performance.

Knowing the wing span and the aspect ratio, we can then determine the wing area $S$ and the wing loading $W/S$. We see therefore how the preparation of the design depends almost exclusively on the determination of the wing span and aspect ratio.

Practical considerations and economics also come into play at this point. You can achieve high performance with a long wing span, however this comes at the expense of ease of handling due to the inertia of the wings. Moreover, large dimensions are less practical when it comes to construction, transport, assembly, and especially with the difficulties that come with off-field landings.

And finally, any aircraft with larger dimensions will cost more to build, because of the size itself and also because of all the extra requirements a high-caliber machine requires, like retractable gear, special instrumentation, etc.

Thus we can say that various factors come into play when making the choice of the wing span, and the economics are determined by the conditions that the aircraft will be subjected to. For example, when designing a competition sailplane, greater importance should be given to the aerodynamic performance. A long wing span will certainly be called for, as this offers a large wing area with improved efficiency and sink rate due to...
the reduction in the ratio between passive area and wing area, as we have seen in the
determination of the characteristics for the complete aircraft.

Thus, in a competition sailplane more importance is given to the aerodynamic
characteristics, even if this results in increased costs, higher probabilities of damage
while attempting an off-field landing, and handling difficulties. These
inconveniences—excluding cost naturally—will be compensated for by the pilot’s
expertise, since this type of aircraft will not be entrusted to beginners.

In any case, a compromise has to be reached between the various factors that will
determine the aircraft’s characteristics, giving preference to one or the other depending
on the requirements. A good rule therefore is not to push oneself towards extreme
solutions. The middle road is always the best. Only in experimental designs can you try
extreme solutions, with the understanding that it requires thorough knowledge. This was
the case with the famous glider of the Center of Polytechnics at Darmstadt, 30 Cirrus,
with an aspect ratio of 33. The aerodynamic characteristics are without a doubt very
high, but so was its cost.

Considering the cost, which is the determining factor of the construction for aircraft to be
purchased by individuals, we can say that as a general rule, the aircraft with larger wing
spans (18 to 20 m) are three to four times more expensive than the one with shorter span
(10 to 12 m). It is clear that the cost factor is a decisive importance at the start of the
project.

35. Aspect Ratio and Wing Loading

Having established the wing span, we can now consider the other factor that determines
the aircraft’s performance—the wing aspect ratio. We know that increasing the aspect
ratio diminishes the induced drag, therefore we increase efficiency. However, with equal
wing spans, when we increase the aspect ratio, the wing area is reduced and wing loading
is increased.

But the wing span $L$, the aspect ratio $AR$, and the wing area $S$, are bound by the relation:

$$AR = \frac{L^2}{S}$$

Having determined $L$ and $AR$, $S$ is also determined and so is the wing loading $W/S$, which
is always referred to as the total weight, pilot included. Pilot weight may vary within
restricted set limits.

Going to the actual practice, we can give approximate values to these factors for the
gliders of the category we have discussed:

- Low performance gliders: $L = 10$ to 12 m.
  - Wing loading ...........15 to 17 kg/m$^2$
  - Aspect ratio...............8 to 12
  - Wing area..................10 to 15 m$^2$

- Medium performance gliders: $L = 13$ to 15 m.
  - Wing loading ...........16 to 18 kg/m$^2$
  - Aspect ratio...............13 to 16
Wing area.....................14 to 16 m²

High performance sailplanes: \( L = 17 \) to 20 m.
Wing loading .................16 to 22 kg/m²
Aspect ratio..................18 to 22
Wing area.....................18 to 20 m²

This are nominal values for standard gliders. Of course, there are gliders with greater
aspect ratios and modest wing spans, and others with modest aspect ratios and longer
spans, but these are special cases for particular conditions.

The limits that the wing loading varies between is fairly restricted—on an average
between 15 and 18 kg/m²—and this is restricts the sink rate and landing velocity. But
since the wing loading does not influence the glide ratio, water tanks are added to serve
as ballast on gliders designed for long-distance flights to increase the horizontal velocity,
and the water dumped in flight once the higher speed is no longer required and a low sink
rate is desired to exploit slowly rising thermals, or to obtain a slow speed for landing.

36. Fuselage

The most important factor that defines the fuselage of a glider is its length, with
consideration given to the aircraft’s stability and handling ease, however many factors
influence its dimensioning.

We can achieve the same static stability with a short fuselage and larger empennage, or
with long fuselage and smaller empennage. The wing aspect ratio also influences the
longitudinal stability.

In the case of a long fuselage, we have a smaller empennage area, and thus a lower
weight and drag, but this is offset by the larger weight of the fuselage and the higher drag
due to the increase surface friction. Under this condition there wouldn’t be much
difference between longer or shorter fuselages.

However, if we consider the dynamic stability, we conclude that a longer fuselage is
preferable since the longitudinal inertia moments are increased and the empennage is less
influenced by the wing turbulence because the wing is much farther away, and thus is
more effective. However the fuselage cannot be excessively lengthened, or the glider
will be sluggish.

As a good approximation, we can set the fuselage length with the formula based on the
wing span \( L \):

\[
f = \left( 0.30 \cdot L \right) + 2.5
\]

This is the total length from the nose to the tail in meters.
37. Empennage
In dimensioning the empennage, it is important first to determine the area necessary to maintain good stability. The area of the horizontal tail $S_{ht}$ can be established using the formula in Chapter 4 (§ 21), as a function of the wing area $S$ for the average wing chord, and the distance $a$ of the airfoil from the aircraft’s center of gravity.

We have:

$$S_{ht} = \frac{S \cdot L}{K \cdot a}$$

where the coefficient $K$ may vary between 1.8 and 2.2. Also for the vertical tail we have seen in Chapter 4 how its surface can be dimensioned (§ 25).

38. Basic Three-View Drawings
Having established with approximation the overall required elements, we follow with the preparation of the general schematic design of the plane, thus drawing in the appropriate scale the three basics views, making provision for the loads and their required space.

First we draw the side view in 1/10 scale, drawing the fuselage shape, providing for the various loads allocation but also considering aerodynamics and aesthetics.

In this phase, we can take care of the so-called aesthetic aspect, in such a way that the design and the relationship between the various components results in a shape that is pleasant to the eye. Nature itself teaches us that generally designs that are aesthetically pleasing are also aerodynamically shaped.

Obviously, however, judgment should be left to the expert who knows and understands the nature of the phenomena associated with flight. At all the times, keep in mind the structural and aerodynamic requirements and reach a compromise to obtain the best of all factors.

The design of the fuselage is influenced almost entirely by the arrangement of the cockpit. Indeed, we can say that the fuselage of a glider is tailored around the pilot, with the need to reduce the cross-section to a minimum.

In a single-seat design or with two seats in tandem, the maximum width of the flight deck can be 60 cm on the outside. The interior dimension should not be less than 54 cm. The same can be said for the height, which may vary from 100 to 110 cm as a minimum. We have therefore established the preliminary requirements of the fuselage as a starting point.

We will sort out later the location of the wings, the horizontal empennage, the forward skid and eventually the landing gear.

39. Centering
Having established the location of the various elements and that of the loads, before we continue to define the aircraft’s design, we have to verify its centering. That is, we must make sure that the total of all the aircraft’s weights, fixed and moveable, will fall within 25-30% of the mean aerodynamic chord of the wing. This location for the center of gravity of the aircraft is essential for good stability.
Remember that the mean aerodynamic chord is the wing chord at the geometrical center of the wing.

In gliders, there is no variation in the load during flight therefore centering is a singular operation. It is obvious that the determination of the center of gravity does not require the pilot’s presence. However in a two-seat side-by-side configuration, it is necessary to determine the centering with one and two people to check if the center of gravity fluctuation falls within the allowable limits (25-30% of the wing chord for longitudinal stability).

The determination of the center of gravity location can be found either analytically or graphically.

In both cases, we first design the longitudinal section and the location of the various loads are established. The determination of the location and values of the various loads is not a simple matter at this stage since it’s not always possible to know in advance the weight distribution of the aircraft’s structure.

It is essential that the estimates of the weight of the components be made with great care, because the accuracy of these estimates will determine whether there will be a good or bad outcome in the design.

This analysis will be easier for the experienced designer who may use data from previous projects. It is very difficult to obtain detailed data on weight from aircraft built by others.

**Analysis of Partial Weights.** To help you with this difficult task, we will give you some average values of structural weights for various components for gliders.

**Wing.** For wings with a single spar and a torsion box at the leading edge, fully covered and complete with aileron controls and with wing root fittings, we have the following weights per m² of wing surface: for a wing of small aspect ratio (8-10), with external bracing: 4.5-5 Kg/m², cantilever: 5-5.5 Kg/m²; for a cantilevered wing of medium aspect ratio (12-15): 5.5 to 6.5 Kg./m²; for a cantilevered wing with high aspect ratio (18-20): 6.5 to 8 Kg./m².

**Empennage.** For the horizontal empennage with plywood-covered stabilizer and fabric-covered elevator, complete with all the attachments and controls, the weight varies from
3 to 4 Kg/m² respectively for aspect ratios of 3.5 to 4.5. The position of the center of gravity for monospar wings can be placed at about 30% the wing chord. In the horizontal empennage instead the position is 40% of the chord.

**Fuselage.** The determination of the fuselage weight by empirical methods is more difficult. We can give some values relative to the total weight $W$ (in Kg.) of the fuselage in relation to its length $L$, measured in meters; but as far as the longitudinal distribution of weights, it will have to be considered according to the internal arrangements and will vary from type to type.

For a single-seat and polygonal truss type fuselage without landing wheel, or for monocoque fuselage with landing wheel and plywood covering, complete with vertical empennage and canopy, we have

$$W = 6L + 20$$

For a two-seat design (side-by-side or tandem) with dual controls and complete as described above:

$$W = 6L + 50$$

The pilot with parachute is considered to be 80 Kg.

**Center of Gravity Determined Analytically.** Based on the partial weights, let’s now proceed to determine the location of the center of gravity.

![Figure 7-2](image.png)

The longitudinal section of the glider is subdivided in stations, and to each we fix its weight and the position of its center of gravity.

We select two reference points on the two axes of coordinates. Typically, we will select the tip of the nose as the ‘zero point’ in the horizontal (X axis), and this is usually called the ‘datum’. We’ll use the bottom of the skin or wheel as the ‘zero point’ in vertical (Y axis), often designated ‘W.L. O’ for ‘water line zero’.

Let’s call $x$ the distance from the datum, and $y$ the distance from W.L. O. Multiplying this distance by the weight gives us the static moment of the station relative to each axis and referred to as index $M_x$ and $M_y$ respectively for the X and Y axes:

$$M_x = W \cdot y \quad M_y = W \cdot x$$

All the moments for each axis are the summed and there are referred to as $\Sigma$ (sum).
Dividing then the summation of the static moments, $\Sigma M_x$ and $\Sigma M_y$ by the summation of the weights, $\Sigma W$, which is the total aircraft weight, we get the respective distances $x_{cg}$ and $y_{cg}$ from the X and Y axis for the center of gravity $CG$.

This distances are expressed by the following relationships:

$$x_{cg} = \frac{\Sigma M_y}{\Sigma W} = \frac{\Sigma (W \cdot x)}{\Sigma W} \quad [24]$$

$$y_{cg} = \frac{\Sigma M_x}{\Sigma W} = \frac{\Sigma (W \cdot y)}{\Sigma W} \quad [25]$$

For convenience the values of the individual operations are summarized in a table. We show as an example the calculation to determine the center of gravity for a glider in the 15 m. category.

![Figure 7-3](image-url)

**Figure 7-3**

<table>
<thead>
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<th>Sta.</th>
<th>W(Kg)</th>
<th>x (m)</th>
<th>$M_y$</th>
<th>y (m)</th>
<th>$M_x$</th>
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<td>23.40</td>
<td>1.23</td>
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</tr>
</tbody>
</table>

$\Sigma W = 250 \quad \Sigma M_y = 446.65 \quad \Sigma M_x = 135.16$

$$x_{cg} = \frac{\Sigma M_y}{\Sigma W} = \frac{446.65}{250} = 1.787m$$

$$y_{cg} = \frac{\Sigma M_x}{\Sigma W} = \frac{135.16}{250} = 0.54m$$
Center of Gravity Determined by Graphical Means. In order to determine the location of the center of gravity graphically, the polygon method is used. Using the side view of the aircraft, we draw vertical lines through the already pre-established partial center of gravities. These lines represent the direction of the weight-forces applied to them.

On one side, the polygon of the forces is constructed. All the individual weights are reported according to a selected scale and drawn one after the other in a continuous line. The ends of each segment are then connected to a randomly chosen point. These connecting lines are indicated as s1, s2, etc. The parallels of these lines, s1, s2, etc. are reported and intersected with the previously drawn vertical lines.

On the resulting vertical line R drawn from the intersection of the extension of the first and the last of the polygon lines, will be the location of the center of gravity $CG$ longitudinally. Repeating the operation but now using the horizontal lines, line R' will be determined. The intersection of this line with line R will be the location of the center of gravity, now established in height as well.

Normally, knowing the location of the center of gravity $CG$ in height is not necessary, therefore only the location of the line R is sufficient. The determination of the horizontal line R' graphically is not very precise—all the lines constructed horizontally are very close to each other making the process very confusing.
Once the center of gravity has been found, its position may not be what one would have expected. In this case a relocation of weights may be necessary. In our sample case, it is necessary to vary the position of the pilot in relation to the wing. After few changes and with the center of gravity location fixed in the desired location, the project may proceed with the determination of the aircraft shape, dimensions and general arrangements.

40. Side View

**Cockpit.** The first consideration is the location of the cockpit. For stability and optimal visibility, the cockpit is located as forward as possible.

For an average pilot (1.70 m), the cockpit will have the following dimensions: From the edge of the seat’s shoulder rest to the pedals’ rotational: 98-100 cm. Internal minimum width: 54-56 cm. From the edge of the seat to the control column: 45 cm.

In gliders, the seat is ergonomically shaped in order to offer maximum support to the body all the way past the pilot’s knees. This is done to diminish leg fatigue, since in most gliders the control pedals are set very high, almost at the same level of the seat.
In the canopy, it is best if the windshield and the side windows are at a small inclination from the vertical axis, otherwise even a light mist may produce a mirroring effect that will reduce visibility. Canopies that are flared to the fuselage with a high degree of inclination are better aerodynamically but offer poor visibility—and are therefore not recommended.

The windshield also should not be close to the pilot’s eyes: the optimum distance is approximately 60 cm, which is well over the minimum human focusing distance.

The instrument panel should be at a distance of 60-70 cm from the pilot and lightly inclined forward. Attention should be given to avoid having the panel located too low to prevent interference with the pilot’s legs. The seat should be elevated 8-10 cm from the bottom of the fuselage to allow proper clearance for the ailerons and elevator control cables that run under it. The rudder bar cables are run instead in the inner side walls so not to disturb the pilot. The following sketch shows the cockpit arrangements in a standard glider.

There is a space allocated for the parachute, usually 15 cm in thickness and placed behind the headrest. When designing a completely new glider, it is a good practice to first build a prototype of the cockpit. For this a forward section of the fuselage is built, then in it are placed the seat, the control stick, the rudder bar and all the various components. Finally the pilot with parachute will take a seat inside and check for possible interferences, practicality and comfort. If necessary, changes are made until you are satisfied with the design, recorded and transferred to the actual project.

The prototype is constructed with available materials. It does not require an outside aerodynamic shape or need a skinned fuselage. Its function is only to determine the location of the various controls and to finalize the shape and form of the seat for comfort and practical purposes.

**Fuselage Shape.** Once the various arrangements are established, and it comes the time to design the fuselage shape, there are no specific rules or formulas to allow the designer to get the best fuselage design. It is obvious that from the aerodynamics stand point, curved shapes are more efficient, but they are also more complicated and expensive to build.
As we mentioned before, at this stage in the project the personality of the designer has a lot to do with it. It will be up to him to find the best compromise between the aerodynamic requirements and the available resources.

Only a few general considerations are mentioned here. It will be up to the designer to decide which will be the best solution. For the forward fuselage section in the cockpit area, it is best to use a uniform width all the way from the shoulder height to the bottom of the seat. If the cross-section is a polygon, it is best if the sides are kept parallel or slightly inclined. If the cross-section is curved, it should be flattened at the bottom.

This is done in order to locate the seat position as low as possible in the fuselage, therefore reducing the fuselage’s overall height. Towards the rear, it is necessary to flatten the fuselage on the sides and create a sharp edge at the bottom. This helps the aircraft’s lateral stability since a sharp keel retards and actually opposes lateral slippage.

On occasion, we find that a sharp edge even in the upper portion of the fuselage and the dorsal area, further increases the lateral stability, particularly in flight conditions of high angles of incidence. This design also facilitate the application of plywood skin to the fuselage.

In the side view, we have to take into account the planing angle, which is the angle formed by the tangent to the landing carriage when the glider is in flying configuration and the ground. Due to their lower landing speed, the value of the planing angle is not as
important for gliders as it would be for powered airplanes, but it is recommended for this angle not to be less than 6 to 8°.

In the side view, the wing chord angle and the stabilizer angle should be defined. The horizontal empennage is usually set at 0° to the horizontal plane of the fuselage; for the wing chord that angle is set between 3 and 5°.

**Wing to Fuselage Connection.** The relative position of the wing in respect to the fuselage takes quite an importance in gliders. An interference between these two very important components may increase the total drag up to 15-20% if a bad design choice is made.

An analytical study of the wing-fuselage relationship is not possible. The only way to obtain proper data would be from wind-tunnel testing. But this is always a very laborious and difficult undertaking, especially when dealing with gliders.

The wing position may be: (a) middle wing, (b) high dorsal wing, or (c) high elevated wing (above the fuselage).

In the wing-fuselage connection, the following conditions should be adopted: The angle formed between the wing’s upper surface and the fuselage’s tangent at the point of intersection should be 90° or higher. The distance between the intersection lines should be constant all the way from the wing leading edge to trailing edge. Understandably, these conditions are difficult to maintain, especially for the middle wing configuration.
The use of a fairing helps the condition by filling those locations where the increased area would reduce the laminar layer’s speed. This reduction in speed induces eddies and therefore increases drag. The fairing also assures that the intersection line be in areas of relatively high pressure if at all possible.

It is important to mention that if the wing airfoil is bi-convex or plano-convex (flat bottomed), the connection to the fuselage is quite easy, while in cases of a wing airfoil having deep camber and high lift, it is difficult to obtain a good connection, both constructively and aerodynamically. This is because in a fairly short distance, all the high lift has to be eliminated and reduced to zero at the connection of the wing to the fuselage. It is common to gradually vary the airfoil and reduce the lift as it approaches the fuselage thus facilitating the fairing.

When the wing is high on the fuselage, or above and connected by a dorsal fin (as was often done in the past), the airfoil is left unchanged even if heavily cambered. It is important to note that the fairings used for gliders are different from the ones for powered planes. This is because gliders usually fly in heavy lift conditions, contrary to what happens in regular airplanes.
From all this, you may conclude that the high-wing configuration is the best solution for wing-fuselage coupling in gliders. The fairing in this case is simple both in design and in construction, consisting generally of a fin with vertical walls that attached at the cockpit.

**41. Frontal View**

There is little to say in regards to the frontal view design. In a mid-wing design, it is convenient to make it as a M-configuration. This is to raise the wing tips as far as possible from the ground and to increase lateral stability by increasing the aircraft’s keel effect. In this type of wing the dihedral is between 4 to 8° for the central section and of 0 or 1° from the formed elbow to the tips.

In the case of the high wing, the M shape is not necessary, and a dihedral of 2 to 3° is sufficient to give good spiral stability.
Having so determined the position and shape of the wing from the frontal view, it’s now important to check the position in height of the horizontal empennage. With the aircraft in a rest condition, that is with the wing and both landing skids on the ground, the horizontal empennage should not touch the ground, or even worst, it should not touch before the wing. In such case the empennage would have to support portion of the aircraft weight. It’s desirable that at rest, the horizontal empennage be at least 8 to 10 cm. from the ground.

42. Top View
In the top view, we are going to define the shape of the wing, the fuselage and the horizontal tail. For the wing we had already established, at the beginning, the opening, and the surface, therefore the mean chord and the span. What is required now is to establish the actual shape. In gliders, the wing could be tapered, rectangular, or a combination of both, rectangular for a central portion and then tapered.
For wings of greater span, the first design is preferable, since a greater chord is possible at the fuselage thus allowing for a thicker spar. The tapering ratio, the ratio between the maximum and minimum chord, may vary between 2.5 and 3.5, with greater ratio for longer span.

The rectangular wing is more suitable for smaller gliders with a short wing span, mostly used in trainer gliders, due to the relative simple construction. Furthermore the rectangular wing presents troublesome design characteristics in regard to sturdiness, in fact, at equal span and surface to a tapered wing, the chord and therefore the spar thickness at the fuselage connection is much smaller. Also the maximum bending moment is much greater in the rectangular wing due to its geometrical center being much further away from the fuselage junction than the one in the tapered wing. This type of wing is therefore not suitable for serious gliders or gliders with longer wing spans.

The third design in Figure 7-15 shows a compromise between the trapezoid wing and the rectangular, a square wing up to the center portion and tapered from there to the tip. This shape is suitable in the case of wings with external strut supports, since the maximum bending strain is not longer at the fuselage, but it coincides with the strut mountings. In the center portion the wing airfoils remains constant, while in the tapered portion the airfoil varies.

The fuselage top view should offer the largest width corresponding to the pilot seating area and have a minimum width of 60 cm. The width of the fuselage at the tail should be at least 15-18 cm to offer sufficient support and attachment for the tail itself.

43. Control Surfaces
Having designed the plane in its complexity, it is now necessary to determine the dimensions of the control surfaces, such as ailerons, elevators and rudder. In gliders, these surfaces have to be fairly large due to the aircraft’s low speeds.

For the ailerons, based on numerous practical experiences, it has been found that their maximum efficiency is reached when their chord is approximately 25-30% of the corresponding wing. Practically though, the chord is kept constant with the wing span and with little tapering, but at its extremities should never be more than 40-45% of the corresponding wing. The length of the aileron may vary between 45% to 70% the length of the half wing span, while its surface may vary between 18% to 22% the one of the half wing.

The ratio between the ailerons and the wing span is greater in gliders with longer wing span.

The elevators area is kept at 45% to 50% the area of the horizontal stabilizer. The area of the rudder is kept between 60% to 75% the area of the vertical fin.

44. Landing Apparatus
There is a great difference between gliders and motorized aircraft in their landing gear designs.

In gliders, due to the lack of a propeller, the low wing loading, therefore low landing speed, the landing gear may be just a simple ski or sliding block that may or may not be
shock-absorbed. The application of a small wheel with low pressure tire is very common and its location is just aft the center of gravity. Lateral stability when the craft is stationary is not there. As it’s commonly known, at the beginning of the takeoff run a person runs along side, holding one wing until enough velocity is reached and stability from aerodynamic forces through aileron control is obtained.

It was mentioned that the ski may or may not have shock absorbers. In training gliders, the ski is a wooden rail, rigidly attached to the fuselage. Generally though, the ski is attached by interposing rubber pads, tennis balls, or even metal springs.

The use of a wheel, does not mean that it replaces the ski, it is only an aid. It reduces friction at the start and facilitates the takeoff, and also it’s very useful for ground maneuverings. Generally it is placed just aft the center of gravity, and it should protrude at least 5 cm.

![Figure 7-16](image)

This is a preferable location because it gives the pilot some freedom in choosing landing rolls, long or short as required. With elevator control, at touch down, one could ride on the wheel for a lengthy and smooth landing, or vice versa, drive the ski to the ground in order to brake the run.

In better gliders, the wheel is completely retractable. In this case, its position is slightly ahead of the center of gravity and is equipped with a brake. The ski in this case is nonexistent. This solution, brings some complications to the construction design and adds weight, but also makes the fuselage more aerodynamic, not having protruding parts, such as the ski and the fixed wheel, which add drag and deteriorate flight efficiency.

The disadvantage of not having a front ski is appreciable when having to perform forced landings; plowed fields, river beds, or any other uneven field can easily damage the fuselage undercarriage.

To determine the type of the landing gear to be used, it is necessary to pre-determine the use of the aircraft and the type of person that will be flying it.

Such daring construction designs as retractable gear, are then only used in high performance gliders, used by experienced pilots, where the risks of sustaining possible damage are offset by the possibilities of winning races or establishing new records.

45. Control of Maneuvering Surfaces

The development and design of these controls is very important on any type of aircraft, but more so on gliders. Their controls have to be “very sweet”. Because of the light
aerodynamic loads exerted to the control surfaces, due to low speeds encountered in this type of flying, and the modest wing loading on these aircraft, the mechanical resistance found in the transmission’s linkages should not mask the reactions to the controls and prevent the pilot from “feeling” the aircraft at all times. Since the various linkages must be mechanically sound, it is necessary to reduce to the minimum all the possible friction causing apparatus such as pulleys, levers and elbows.

The simpler the transmission the better it works. The development of the aircraft’s structure and the development of its various controls should be carried out simultaneously, and if necessary, adapt the aircraft’s design to the design of the controls, not the other way around. If it’s necessary, in the end, it may be more convenient to design a more complex fuselage section, in order to facilitate the implementation of the control assemblies, rather than doing it the other way around.

Let us briefly point out the most common methods in use to control the movable surfaces. The ailerons, elevators, and rudder, are controlled by the pilot via linkages that may be made up of cables, rods or a combination of both.

**The Control Stick.** The ailerons are activated with a lateral movement of the control stick, while a longitudinal movement controls the elevators. The rudder is controlled with the pedals. In most gliders and powered aircraft, the stick movements are transmitted to the control surfaces with steel cables.

In high-performance gliders, the use of solid rods is becoming acceptable, these give a better feel to the pilot because of the low friction. These types of controls, though, are expensive and present fussier tune-ups. For these reasons, the cable method is more popular. The diagram on Figure 7-17, shows the most common method used for the transmission of movements by cables.
The control stick $A$ is hinged at $F$ on a supporting bracket $S$ which in turn is fixed to rod $B$ that liberally rotates on bearings $C-C$. The control stick rotates at $F$ in a longitudinal plane, and it extends beneath as a lever to which at point $B$ the control cable for the stabilizer is connected. From here, one end of the cable (1), goes directly to the upper stabilizer lever, the other end (2) through a pulley situated in front of the control stick, returns and is attached to the lower stabilizer lever.

Pulling the bar backwards, the connection $E$ moves to $E'$ pulling on the control cable (1) and the stabilizer moves up. The aircraft pitches up. On the contrary, if the control stick is pushed forward, the pull is now on the cable (2), the stabilizer moves down and the aircraft pitches down.

![Figure 7-19](image)

The control to the ailerons is obtained through a lateral movement of the control stick, which in turn rotates rod $B$. On rod $B$ there are attached two levers $L$, and attached to them there are two rods $T$ that transmit the movement via a three-arm lever to a cabling system connected to the ailerons.

![Figure 7-20](image)

The three-arm lever is fixed to a wing longeron. By disconnecting the lever $T$ from it, it allows the disassembling of the wings. In standard gliders the radius of the lever is kept between 80-120 mm. If space is not a concern, it is better to adopt the larger radius in order to reduce the system resistance.

**Pedals.** The pedal system in gliders is different from the ones used in powered aircraft. In powered aircraft, the rudder movement is achieved by the longitudinal movement of the pilot’s leg. This rotates a bar around a vertical support or the footboard moves entirely forward.
In gliders, in order to diminish pilot fatigue, due to occasionally lengthy flights, and also because the forces required in the controls are not that big, the command is achieved by the rotation of the pilot’s foot by pressing the pedal with the toes; the pedal is pivoted at the bottom, and the foot rests on it.

![Figure 7-21](image1)

On the pedal above the rotational axis are attached the control cables that run to two levers connected to the rudder. Behind the pedal there are springs for proper tensioning of the cables.

The diagram on Figure 7-22 shows the location of the controls, the levers, and the distribution of cables as generally used in gliders.

![Figure 7-22](image2)
46. Options

Spoilers. For years now, the use of spoilers has become essential. By design, they are generally flat surfaces, that when deployed by the pilot they open in a position perpendicular to the wing’s surface.

Their purpose is that of disturbing or spoiling the airflow over the wings surface, thus their name. This causes a loss of lift, therefore a decrease in efficiency and speed. This is a must for landing to reduce the landing roll especially in forced landings, situations that are very frequent in soaring. Spoilers are always placed on the dorsal side of the wing to get the maximum disturbance effect.

It is obvious that their size is related to the characteristics of the glider they are installed on. It is recommended, though, not to oversize them in order to increase their efficiency, because their deployment would require too much force. Their location should be such that once deployed their effect does not pose interference with other control surfaces and cause unwanted vibration, that, even if not dangerous definitely not welcomed.

With the increased popularity of the sport and its extreme ranges, such as flying into thunderstorms as well as into clouds, it has become necessary to be able to reduce the maximum achievable speed when in a dive. One may find himself in a situation, sometimes unavoidable, or without knowledge, where dangerous speeds are reached that could even compromise the integrity of the aircraft.

The thinking of limiting the maximum speed in a dive, increasing the aerodynamic drag, by designing oversized spoilers was entertained. (We have shown previously by a numeric example how to calculate the surface size of such air brakes.)

But in order not to exert an excessive strain when deploying such a large surface, designers have decided on dividing the calculated surface in two, locating one on the upper side of the wing and one on the lower side. The two sections are connected in such a way that the deployment of one is aerodynamically compensated by the other. In fact, the resistance encountered on the deployment of the upper spoiler is balanced by the wind assisted opening of the lower spoiler.
The use of a double spoiler systems has become widespread in the soaring. Their duty is twofold: Lessen the aircraft efficiency and descending speed, and bring the maximum speed attainable within the safety values of the aircraft structure. The speed with the double spoiler deployed in modern gliders is within the 200 and 250 km/h.

**Towing hooks.** In the first chapter, we discussed the various methods used in the towing gliders. These methods may be divided in two distinct categories: ground tow (elastic cable, winch, towing car) and towing in flight by aircraft.

The hooks, and their location on the aircraft, have to be consistent with the particular method used in towing. In the ground tow, the aircraft trajectory is sloped upwards in order to reach elevation quickly. In this condition it is necessary to place the hook much lower than the center of gravity and not too much forward of it.

Also the release has to happen automatically at the very end of the pull. For these reasons the hook employed in such systems has to be located under the front ski and has to be of the open type.

To prevent premature cable release, due to the higher inclination the glider presents in relation to the pulling cable, it is necessary for the hook to have an angle of approximately 25° from its vertical when the glider is in straight attitude.

For flight towing, the glider is usually slightly higher than the towing plane: therefore the hook should be just a little lower than the center of gravity but as forward as possible.

It is important to note that when towing this way, the towing cable is not always under tension. At times, due to different flight conditions between the two aircrafts, some caused by external effects, or caused by pilot’s inexperience, it may happen that the cable slackens. It is understandable then, that, to prevent premature release, the hook cannot be of the open type, but closed with pilot control on its opening.
The two type of hooks are shown in Figure 7-25. In most gliders both types of hooks are installed in order to accommodate the use of either system.
Chapter 8  
Aircraft Design

In this chapter we will try to offer some comments about the design of the aircraft and its components, and in particular the geometric section of these elements. And in the design process, we have to constantly be aware of the construction demands. For instance, when designing the wings and fuselage, it is done in such a way that the various components may be developed into surfaces that are straight and flat. Since these will be covered with plywood, we know that plywood does not adapt well to shapes that have double curvature. Only a slight amount of shaping is permissible, but even this requires very specialized work.

47. Wing Design

For simplicity of construction, it is preferable that the design be made with straight outlines except for the tip. Here, for aerodynamic reasons as well as for aesthetics, the contours will be curved. To lay out these wing tip curves, which are also used in the tail section, the most practical method is to draw a parabola by using tangent lines.

Generally the curves of the wing tips and tail section are drawn on paper to scale and free-handed. The difficulties arise when the same curves have been reproduced in the construction stage. Even in the case of a simple curve like a circular arc, drawn simply with a compass at the design stage, we realize the task may well be difficult, not to mention the difficulties encountered when trying to use other irregular curves. Laying out of parabolic lines by tangent lines is, however, practical and the reproduction at any scale is feasible, therefore it is possible to get harmonious and very pleasing curves.

Let’s look at, for example, the outline of a wing tip. The first step is to design a square wing, like the line $AB$ in Figure 8-1. On the leading edge, a point $C$ is selected at a distance of about one half the length of $AB$. On the trailing edge, a point $D$ is selected at a distance of about 1.2 times the length of $AB$. A third point $E$ is chosen at the intersection of the line $AB$ with the spar axis. Points $C$, $E$, and $D$ are the tangent points of the curve that will be drawn from the leading edge, to the wing tip, and to the trailing edge.
To draw the curve, we must first divide the segments $CA$ and $AE$ into equal parts, in our example six, and these points are then joined as we can clearly see in Figure 8-2. If we draw a curve tangent to all of these lines, these will result in a parabolic arc. The operation is repeated for points $E$, $B$, and $D$. For design simplicity, points $C$ and $D$ are made to correspond to the wing ribs, or at a distance from $A$ and $B$ of an integer value. Point $E$, as we mentioned, can be on the axis of the spar. It is possible that the points $C$, $E$, and $D$, following the first design, may be adjusted in order to give a more pleasing curve to the eye. It may take a few attempts to find the right location that gives the best results. The tail section and even the fuselage may be drawn using the same methods.

48. Design of Wing Airfoil
In the design of the wing, the airfoil is of fundamental importance.

Wing with constant chord. In a wing where the airfoil is kept constant throughout the full span, the design of the various airfoil sections is relatively simple. A section of Chapter 6 Applied Aerodynamics is dedicated to the design of the proper airfoils. [The tables of the 1946-era airfoils are omitted here.] In each table, there are three columns of numbers: $X$, $Y_s$ and $Y_i$, and these values relate to a unit length of the airfoil. In other words, they are percent values of the airfoil length.

The $X$-values are the horizontal distance (abscissa) and the $Y$-values are the vertical distances (ordinate). The length of the airfoil is subdivided into ten parts, and the first part is again subdivided into five to six parts in order to obtain greater precision near the leading edge. We have, therefore, values of $X$ at 1.25% to 2.5%...10% to 20%...100%. From these points we draw perpendicular lines, and on these we trace the values for $Y_s$ and $Y_i$, (Figure 8-3). By connecting the newly found points, we obtain the shape of the airfoil. To determine the values for $X$, $Y_s$ and $Y_i$ for a particular length, all we have to do...
is multiply the values found on the table by the desired length and divide by 100. This way we can obtain the proper airfoils in relation to their length.

**Wing with varying airfoil and angle of incidence.** As we have seen, the wings of gliders rarely are of constant airfoils, and they vary from section to section. At the fuselage, for reason of construction, the airfoils are thick and designed for greater lift, while at the tips, for increased efficiency and stability, the airfoils are much thinner and may even be at a negative incidence angle in respect to the sections near the fuselage.

If we are given the two fundamental airfoils, we can design the intermediate ones. Only wings with a linear sweep will be considered, this way, the airfoil variation will be linear, and this linear variation can be determined either analytically or graphically.

**Graphic Method.** On an horizontal reference line $T$, we trace the location of the ribs in a selected scale (1:10, 1:5). If $A$ and $B$ are the location of the ribs at the extremes, which have a known airfoil, we mark on them the upper, $Y_s$, and lower $Y_i$, values for a chosen percentage of the chord, let’s say 30%. We connect these points with a line.

The intersection of this line with the previously traced lines representing the ribs location, will give the upper and lower values of all the intermediate ribs at that particular percentage of chord. The schematic seen on Figure 8-5 show this type of construction. Repeating this operation for all the percentage on $X$, we’ll have all the required values for all the intermediate ribs.

Since the process has to be repeated a number of times, (usually 14), if we continue the use of the same line $T$ to generate the expected values, a lot of these will be too close together and even coincide, making the operation very difficult and cumbersome.
In order to eliminate this, and the possibility of errors, the design will have to be repeated separately for every percentage value. We understand how long and laborious the operation will become.

For this reason and also for the poor precision expected from the graphic method, it is preferable to calculate the required values by means of the analytical method.

**Analytical Method.** Let us consider again the airfoils A and B and the intermediate airfoils 2-3-4. At each percentage value of X, (30% for instance), we find the difference between the value of A and the value of B. Dividing this difference by the number of ribs less one, which is the same as the number of spaces between the ribs, we find the difference in value that exists between adjacent ribs. This is only true if the distance between the ribs remains constant, if not a difference may be calculated proportionally. Adding this difference to the value of rib B, or subtracting this difference from the value of rib A, the same amount of times that there are spaces, we obtain the value for each intermediate rib.

**Example.** Let’s use a practical example to better understand the principle. Let us consider the upper value Ys at 20% of the chord. For A, Ys = 40mm. For B, Ys = 20mm. The difference between the two is 40 – 20 = 20mm.

This divided by the number of spaces, four in our case, gives us the increment between two adjacent ribs:

\[
\frac{20}{4} = 5\text{mm}
\]

Adding to the value B or subtracting from the value A we have the values for ribs 2-3-4:

- Ys for B = 20 mm
- Ys for 4 = 25 mm
- Ys for 3 = 30 mm
- Ys for 2 = 35 mm
- Ys for A = 40 mm

To verify we see that the value of Ys for A = 40mm. With the same procedure we obtain all the other required value at all the percentages of the chord.

**49. Wing Twist and the Wing Reference Plane**
We have seen how to obtain the various airfoils of the intermediate ribs between the root and tip ribs, but we have done this without consideration of their relative orientation to each other, created by the twist in the wing.
For the proper wing construction, we need to have the exact orientation of each airfoil in relation to the other. It is useful therefore to refer to each airfoil, not to its chord, but to a common plane that we call the wing reference plane.

This arbitrary selected plane is chosen outside the wing. This is done in order to keep all the dimensions of the various airfoils positive, and thus to simplify the calculations.

To obtain the desired twist, generally, the airfoil sections are rotated around their leading edge so the leading edge remains straight.

The wing reference plane is generally fixed at a distance of 15-20 cm below the leading edge.

The airfoils for the wing root and tip are drawn in reference to their chord or tangent depending on the type of airfoil table used.

It is now necessary to refer to the angle of incidence of the wing in relation to the fuselage axis.
For this we draw a horizontal reference line at a distance from the leading edge by the same amount of the earlier chosen distance to the wing reference plane, and at an angle equal to the angle of incidence.

To clarify this let’s use an example.

Let the wing reference plane be parallel and at a distance of 150 mm from the leading edge. Let the wing twist be –5 degrees, and the angle of incidence of the wing in relation to the fuselage be 3 degrees. The airfoil at the wing tip will then be –2 degrees in relation to the fuselage.

Having drawn the basic airfoil in relation to its chord, we trace a horizontal reference line at a distance from the leading edge of 150mm and having an inclination of 3 degrees at the fuselage and –2 degrees at the wing tip.

We reference all of the airfoil data to this line.

We then trace from each point of division of the chord lines perpendicular to the horizontal reference line. On this line, we read the $Y_s$ and $Y_i$ values of the airfoil in relation to the horizontal reference line.

The basic airfoils are therefore then defined by the exact points.

For the basic linear variation between them we proceed as we seen earlier. The intermediate airfoils will all be referred to the wing reference plane with an angle of incidence based on the wing twist.

**Virtual and Real Airfoil for the Wing Tip.** Up to now we have only considered a straight wing all the way to its tip. We know that the wing tips are rounded for aerodynamic reasons as well as for aesthetic design, and we have already seen how these curves are designed.
We will now look at how the airfoils in this region have to be modified.

The values $Y_s$ and $Y_i$ of these airfoils need to be multiplied by the ratio of the real and virtual chords. This ratio that will diminish towards the tip, and it will always be less than one.

We thus obtain airfoils with the chord, thickness and angle of incidence desired, but closer to the wing reference plane. The leading edge therefore in this region is no longer straight. We need to adjust this distance back to the original distance. To do this all that is required is to add to the values $Y_s$ and $Y_i$ the difference $h$ found between the leading edges of the virtual and real airfoils.

50. Fuselage Design
Having approximately designed both the top and side views of the fuselage at the beginning of the project, we should now sort out the shape of the various sections required for construction. Having fixed the fundamental shape, considering all the space needed by accessories, it is now the time to proceed with the streamlining of the fuselage, in other words to design a fuselage that is aerodynamic and still compatible with the construction requirements.

We should first explain the process of streamlining. If we consider a body of revolution—a body obtained by rotating a curved line around an axis—its sections will
be circles. In a case like this, it will be sufficient for the single generating line to be streamlined in order for the entire body to be streamlined.

Similarly, a body whose sections are of any shape but similar to each other, and aligned on a common straight axis passing through a fixed point in each section, the body will be streamlined if any of the generating lines are streamlined.

Therefore a fuselage of an elliptic shape, where the ratio of the axis of the ellipses of the various sections is constant, and these ellipses are aligned on an axis drawn through a characteristic point to them (for example one of the foci, or its center) will be streamlined as long as any of the parameters, such as one axis, is streamlined. The same stands true for a fuselage of rectangular shape, where there is a constant ratio between the two sides and where the sections are aligned at the intersection of the diagonals.

Generally though, the various sections are not similar and the ratio of the axis of the ellipses or the sides of the rectangular are not constant. Also the line to which the sections are referred to is not linear, but curved downwards, like in the front part of the fuselage.

In such cases, is no longer sufficient that only one of the parameters, like a generating line, to be streamlined. We have to verify the streamlining of different parameters and of the sum and the ratio on all of them.

In practice, this type of design work is accomplished in this manner: First the top and side views of the fuselage are drawn, taking into account all the necessary space requirements. Then the fundamental shape of the cross-section and the longitudinal variation is fixed. Then a simple solid body of the desired shape is defined, where its sections are geometrically determined. To this base body, other simple shaped bodies, for cockpit, wing connections, etc., are superimposed.
Thus having outlined the fuselage, that is, having defined the various parameters, width \( L \), and the various heights, relative to a common base line or ground plane, we now proceed with their streamlining.

We verify the process by means of a design trick, where the curves are exaggerated. Thus, we design the fuselage with a scale of 1:10 longitudinally and 1:4 or 1:5 transversally.
In any case the ratio between the two scales will be adopted on a case-by-case scenario, according to the particulars of the design. Generally, these curves will exaggerate any irregularity or errors in the data points, and corrections will then be made.

We will return to the design of the sections, once more, with these corrected values, to check that we are still meeting the necessary requirements of space and aerodynamics. The same streamlined design of the various parameters will also serve to extract the changing dimensions for the outline of the cross-sections of the fuselage itself.

**Streamlining of fuselages when the sections are not geometrically defined.** When the sections of a fuselage are not geometrically defined, a streamline study is no longer possible since the required parameters are missing.
We then turn to the *water line* concept, so called because of its extensive use in boat design and construction.

![Diagram of water line concept](image)

*Figure 8-15*

This consists in slicing off parallel sections of the body under study, and verifying that the intersection shape is streamlined.

It’s not necessary for the sections to be aerodynamic, as in the case of Section A-A, because the laminar flow around the body is not parallel to the axis.

**Design of the Sections.** We have seen that the easiest method of streamlining the fuselage is achieved when the shape of its sections are geometrically identifiable. We are not going to describe all the various sections employed in fuselage design, since the designer will adopt the best suited design for the requirements at hand and based on the best aerodynamics, construction methods and space requirements.

We will like to point out though, a type of section, that is simple and practical, both in its design form and in the streamlining of its parameters. This type is brought about by means of parabolic curves, constructed with the tangential method, seen earlier in the design of the wing tips. With this kind of construction, we can achieve most types of fuselage shape sections, from almost circular rounded shapes to ones that are sharp-cornered on the lower section or even on both sections, as it occurs in the aft portion of the fuselage.
To streamline a fuselage with such sections, it is necessary to streamline the various parameters that define the section, such as the width $L$ and the various heights $H$ in relation to the plane of construction, and the ratios of these with the width itself. We can easily see that it is not possible to give a fixed rule for this type of design, since one would have to study in specifics the most convenient and necessary streamlining of the parameters for each fuselage type.

In the case, as an example, where the sections are the arcs of a circle, one would have to streamline the circle’s radii, their centers and the ratio among them. It will then be the design itself that will suggest, case by case, which will be the parameters to be examined.

What we have briefly described is not to be used as a rule, but rather as a basis for the study of this very important work of fuselage design.

51. Empennage Design
What we have seen in the wing design also applies in the empennage design. Even in the tracing of its airfoils, the procedure used is similar to that one of a wing with a constant airfoil. The empennage’s airfoil, in fact, is always symmetric and bi-convex, and also it never has a twist.

In reality, it is often convenient to taper the airfoil in thickness, but the variation is on the same airfoil. Generally the thickness goes from 10% - 12% where it attaches to the fuselage to 6% - 8% at the tips. The variation has to be linear for both the horizontal and vertical section.

52. Design of Movements of the Mechanical Controls
We have seen in the last chapter how to lay out the various controls. The actual movements of these controls is of fundamental importance and should now be considered. Let’s have a few examples that will allow us to make some observations.

Let’s suppose we have two levers, $l_1$ and $l_2$, hinged on their axis at their half-way point, and placed at a distance $L$. The levers are straight, of equal length and connected to each other at their extremes by cables of equal length, in such a way that the angle between the cables and the lever’s axis is $90^\circ$. Under these conditions, the levers will then be parallel to each other.
Let’s rotate lever $l_1$ in the direction show by an angle $\alpha$. The amount of movements for both the cables is the same, since the lever’s arm are the same. Therefore the other lever, $l_2$ will rotated by the same angle $\alpha$, and the tension of both the cables will remain the constant since the distance $L$ did not change.

Let’s now consider lever $l_1$ bent backwards as in Figure 8-18, with the angle between the cable and the lever’s arm is less than 90°, and the second lever still being straight, with its arm being of equal length to the first lever. Rotating the first lever clockwise by a certain angle, we notice that the lever’s movements at its extremes, in the direction of the cables, is not the same but is greater for the top cable, $S_1$ than it is for the bottom cable $S_2$.

Since lever $l_n$ is controlled by the lower cable which moves by $S_n$, its rotation angle will not be equal to the one for lever $l_f$. Also, and more importantly, the top cable will slack, since the movement $S_f$ of lever $l_f$ is greater than the top movement of lever $l_2$. Consequently, the top cable will slack by a quantity equal to the difference between the movements of lever $l_f$, $S_f$ and $S_2$:

$$\Delta L = S_f - S_2$$
Due to this slack in the top cable, lever $l_2$ has freedom to further rotate even though lever $l_2$ remains stationary. It will rotate until the top cable is taut—resulting in the bottom cable becoming slack.

In conclusion, we can say that at every position away from neutral of lever $l_1$, there is no single corresponding position for lever $l_2$, but lever $l_2$ may rotate between angles $\alpha$ and $\beta$ that correspond to movements $S_1$ and $S_2$. Similarly, if lever $l_2$ is kept stationary, lever $l_1$ can rotate by the same angles.

If we would use this system in the control system of an aileron, for instance, the aileron, when off its neutral position where both the cables are equally taut, will be free to move back and forth by a certain angle even though the control lever is kept secured. Under these conditions, the aileron will start to vibrate with consequences that are easy to appreciate.

A third consideration is having a lever $l_1$ bent forward, with an angle between the lever’s arm and the cables greater than $90^\circ$ as shown in Figure 8-19.

In this case, a rotation of lever $l_1$ off its neutral position will result in a movement $S_1$ greater than $S_2$, and since the top cable is controlling lever $l_2$, $l_2$ will move by the same amount $S_1$ in both its top and bottom arm. This will have the tendency to also move the bottom cable by the same amount, $S_1$, but the bottom portion of lever $l_2$ only allows that cable to move by $S_2$.

This will follow with an over-tensioning of both cables, resulting in a general hardening of the entire system.

From this examples we can draw an important conclusion. In a closed-circuit cable transmission system, in order not to experience slacks or over-tensioning in the system when off its neutral position, it is necessary that the angle between the cable and the lever’s arm, to which the cables are attached, be of $90^\circ$, when in the neutral position.
It is important to notice that at times, due to the construction, the hinged portion of the lever is not on the lever’s axis itself, but placed outside. Therefore, in a more generic way, we can say that the 90° angle has to be between the cable and the radius drawn from the center of the lever’s rotation to the point in the lever to which the cable is attached.

For this reason, the levers that control the various moveable surfaces assume strange forms at times.

**Rigid Controls.** So far we have talked about controls where the transmission of movement is accomplished by means of cables. If instead, the transmission of movement is obtained by means of rods, since these can work in tension as well as compression, the system is not required to be closed, with two arm levers and two cables, but a single arm lever is sufficient to transmit the movement in both directions.

With rigid controls we also eliminate the inconvenience of having slack or hardening of the systems in the conditions we have seen when the angles between levers and cables are not at 90°. The inconvenience of the non-equal angular rotation, between the moving lever and the moved lever does remain, if the angle is not 90°. This inconvenience though, does not lead to serious consequences as we have seen earlier.

Often, there is the requirement of not having equal angular rotation of the moving lever in respect to the moved lever. Such is the case in the differential controls of the ailerons. As we already know, in the case in the lateral handling of an aircraft, it is necessary to have the up-going aileron move at a greater angle than the down-going aileron. This is accomplished by having angles, between levers and connecting rods, different from 90°. A simple, and very commonly-used scheme of this type of control is shown in Figure 8-23.
To the torsion rod there are attached two levers forming an angle of $30^\circ$ and with a turning radius of 150mm. The angle of movement of the control stick, also attached to the torsion rod, is $25^\circ$ on both sides. The angular movement of the ailerons results in a down-position of $15^\circ$ and in an up-position of $30^\circ$. The differential ratio is 1:2, a normal value for gliders.

We will not elaborate too much on these topics, even though they are of fundamental importance. What is important is that an idea was given that may serve useful in the orientation of the study of these mechanisms. Also we cannot give many examples, since each aircraft requires its own particular study. These mechanisms are tied to the particular architecture, construction demands and the final use of the aircraft. This is an area, in a way, where the designer can indulge in his own whims, and because of this, we have at times seen solutions that are very ingenious, but also often which are more complicated than necessary.
Chapter 9
Applied Loads and Structural Design

53. Flight Loads
The design of the airframe is carried out in three distinct phases: (1) analysis of all the flight loads to which an aircraft may be subjected, and the analysis of the stresses caused by these conditions, (2) determination of all the strains on the various structures under different conditions, and (3) testing the strength of the various elements.

The first phase is the most difficult analysis due to the number of flight conditions and atmospheric conditions. These stresses are very difficult to foresee.

Today, based on years of experience we can accurately establish the loads that are applied to the various elements of an airplane in various flight conditions. The results of these experiences are common to the majority of aircraft with appropriate adjustments for individual type.

Every country has adopted regulatory engineering standards for the design of the structures, and which establish the loads that affect the components of every aircraft. These standards have been established to help the designer in his work, and also to establish a discipline and regulate the aeronautical design so as to not leave the structural strength and safety of the aircraft at the sole judgment of the designer.

In their standards, each country considers all of the possible flight conditions, and among these have determined and examined the ones that calculations and experience have shown to be the most dangerous ones. In the beginning these standards were very simple, but various countries had a considerable difference of opinions.

Today however while improving they also have become complicated, since not only the weight of the plane and its dimensions are considered and examined but also the aerodynamics. Countries have therefore reached a standardization, especially in the civil sector of aviation.

From tests performed on aircraft under various atmospheric conditions the following conclusions were established: (a) the greatest flight loads occur in sudden pull-ups, (b) the flight loads in rough air generally do not exceed the value of 2.5 g and (c) maximum acceleration withstood by men is roughly 7-8 g for short durations, and 3.5-5.4 g if continuous. With gliders it has been established that the maximum acceleration does not exceed 3.5 g.

From these conclusions the regulatory standards have established a load factor for various categories of aircraft, a value that is equal to the ratio of the maximum load applied to a specific structure and the airplane’s maximum weight. In a steady horizontal flight, the lift is the applied load and equal to the weight, and the load factor is equal to one.

In Italy there are two authorities that regulate aeronautical production: one for civilian aircraft and one for military aircraft. The military airworthiness standards are more complete and complex than the civilian standards, however we will discuss only the civilian regulations.

In these regulations there are three load factors used: gliders: 3.5 g, normal category aircraft: 3.5 g and acrobatic category aircraft: 4.5 g. The civilian standards use these load
factors to calculate the loads applied to the components of the airframe. To make sure that the structures are not subjected to loads that exceed the elastic limits of the construction materials, the airframe components are designed to a greater load.

In mechanical or civil engineering, structures are designed for loads that are 3 to 5 times greater than the anticipated loads. This is the same as saying that the factor of safety is 3 to 5. These safety factors are fairly high, and they are adopted to insure against all possible dangers, including the deterioration of the materials over time, the possibility of errors in the calculation of the loads, and also for unforeseen accidental causes. Adopting a safety factor this high results in a heavy structure. Generally this is not very important in terms of cost or the quantity of material used.

In aircraft construction, however, weight is very important and extra material cannot be used. For this reason, the factor of safety in aircraft construction is relatively low, and a safety factor of 2 is required by civilian airworthiness standards for all types of aircraft, with some exceptions, thus the structures are designed for a load factor of twice the flight loads. [Today, the standard factor of safety is 1.50.]

54. Static Tests
Because aircraft use a lower factor of safety, the calculations of the strength of the aircraft structure must be done with a greater degree of rigor than for civil and mechanical engineering. We must also verify the airframe’s strength with static tests. Civilian and military airworthiness standards require that every aircraft prototype has to undergo a static test. Once the aircraft passes this test, it is allowed to continue with flight tests and normal flight.

These static tests check the strength of the most important components, such as the wings, fuselage, control surfaces, landing gears, controls, etc. During these tests, the components are attached to a test rig to duplicate the flight loads and conditions. The test rig should be quite strong so that the internal deflection may be ignored or at least measured. This allows controlled forces to be applied to the structure and the failures documented.

The static tests consist of a limit load test and an ultimate load test. The limit load test is performed with limit loads which are imposed for an indefinite period of time, and it should result in no permanent set. The ultimate load test is carried out following a successful limit load test. In this test, ultimate loads are applied for a short duration and failure may not occur. After this, the loads are increased until failure occurs, and the designer may collect data in order to study any divergence of the calculation from the results of the test.

In gliders, since they are manufactured in limited numbers and at times are based only on the prototype, static tests to ultimate loads or failure are never conducted, since an airframe loaded to such extremes, even if it never shows signs of failure, is no longer suited for flight since the structure has gone beyond the limits of elasticity and would be over-stressed.

Static tests to limit loads are used for the main structural components, however tests to ultimate loads and failure may be performed on individual components and assemblies where appropriate and practical.
55. Flight Conditions

Let us see then how to determine the loads affecting an aircraft during various flight conditions. With gliders we consider four fundamental flight conditions for the wing: (1) maximum lift, (2) maximum speed, (3) zero lift, and (4) hard landing.

**Maximum Lift.** The condition at maximum lift occurs during a sudden pull-up or when a strong vertical gust is encountered during high-lift conditions. The limit load factor is 3.5 $g$ for gliders and normal category aircraft, and 4.5 $g$ for acrobatic category aircraft. Under these conditions, we have the maximum bending of the wing.

The forces that are acting in this case are: aerodynamic forces (lift, drag, moment), aircraft weight, centrifugal reactions, and the reaction of all the linkages that transmit the forces of the rest of the aircraft to the wing.

The load applied on the wing is:

$$ L = 2 \cdot N \cdot \left( W_{\text{total}} - W_{\text{wing}} \right) $$

where

- $2 =$ factor of safety \( [\text{today, } 1.50 \text{ is used}] \)
- $N =$ load factor (3.5, 4.5, …)
- $W_{\text{total}} =$ aircraft total weight
- $W_{\text{wing}} =$ wing weight.

As we see in the formula, the load applied to the wing is reduced by the weight of the wing itself. This weight, being distributed with the same laws of aerodynamic loads, is in opposite direction of to the aerodynamic forces, therefore the wing supports itself without generating bending loads due to its own weight. The load $L$ is averaged along the wing span proportionate to the wing chord. The distribution on the chord is assumed triangular with center of lift at 1/3 from the leading edge.

![Figure 9-1](image)

The wing including the wing fillet is considered a lifting surface only.
Maximum Speed. The coefficient of lift at maximum speed in gliders is one where:

\[ C_L = 0.25 \cdot C_{L,\text{max}} \]

at the same altitude.

In this condition the center of lift is always aft, thus there is a heavy load on the aft spar, its attachments and on the aft structure of the wing. The load factor is set at 0.75 of the one used for the calculation of the maximum lift condition. The load on the wing therefore will be:

\[ L = 2 \cdot (0.75 \cdot N) \cdot (W_{\text{total}} - W_{\text{wing}}) \]

This is divided among the ribs with the distribution shown in Figure 9-2 with a center of lift at 50% of the chord.

Zero Lift. The zero-lift condition is the equivalent of a straight-down nose dive at maximum velocity in acrobatic category aircraft and at a lesser velocity in normal and utility category aircraft. This produces the maximum torsion on the wing, therefore you must analyze the resistance of the wing and its attachment to the fuselage to this load. The minimum value of torsion is given by:

\[ Torsion_{\text{min}} = 0.20 \cdot N \cdot W_{\text{total}} \cdot MAC \]

where

- \( N \) = load factor (3.5, 4.5, ...)
- \( W_{\text{total}} \) = total weight
- \( MAC \) = mean aerodynamic chord

The regulations also dictate that under a maximum load of 1.25 \( N \) the twist at the wing tips may not be over 4 degrees. In gliders, due to the length of the wings, this last condition is more critical than the resistance to twist itself, therefore special attention is given to the design in order to keep the elastic deformation within 4 degrees.
**Hard Landing.** In a hard landing the wing and its linkages are subjected to downwards forces of inertia when the aircraft touches ground. These forces are considered to be at 15 degrees forward of the perpendicular plane of the wing. The landing load in a glider is calculated by multiplying the combined weight of all the wing elements complete with the accessories attached to the wing by a factor of 4, no matter what category of glider.

In this condition, as in the maximum lift condition, the wing is subjected to forces that are in a forward direction in the first case and a backward direction in the second case. Due to scarcity of aerodynamic data, regulations dictate that in gliders, the maximum load in the wing plane in the forward direction be equal to:

$$\frac{1}{8} \cdot N \cdot W_{total}$$

where $N$ and $W_{total}$ are already established.

Following the civilian regulations we have briefly looked at the loads on the wing in various flight conditions. Later, we will study the load conditions for the fuselage, the empennage and other elements.

**56. Wing Stress Analysis.**

Let us again consider the wing and analyze what we have called the second phase of the design of the supporting structures, that is, the calculation of the structural stresses considering the architecture itself.

In this design phase, we enter a field of engineering that deals directly with construction. Since it is evident that we cannot discuss this topic in great length, or even assume that the reader will have complete knowledge of this discipline, we will discuss a simple and practical method of calculation.

**1) Load distribution at maximum lift.** The load on the half-wing

$$n = (Q - Q_a)$$

is distributed on the wing according to the area, and thus proportionally to the chord of the wing. In practice, the rounding of the wing tip is not considered, therefore the calculated area is slightly greater than the actual wing area. It is acceptable to do this, since we use worse-than-actual load conditions, because the center of the wing area will be located farther outboard.
The drawing that shows the wing area also represents the load distribution on it. Since the stresses increase from the extremities to the center, the distances are counted starting from the wing tip where the origin of the x and y axis is placed.

If $a$ is the minimum chord, $(a + b)$ is the maximum chord at the wing root, and $L$ is the wing half-span, the intensity of the loads corresponding to these chords will be

On the minimum chord: $C_1 = a \frac{P}{S} \text{ (kg/m)}$

On the maximum chord: $C_2 = (a + b) \frac{P}{S} \text{ (kg/m)}$

Where $P$ is the load on half-wing and $S$ is the half-wing area.

Example. Let us suppose that the wing of a glider has a minimum chord of $a = 0.5 \text{ m}$; half-span $L = 8 \text{ m}$; maximum chord $(a + b) = 1.5 \text{ m}$; total weight $Q = 300 \text{ Kg}$; wing weight $Q_a = 100 \text{ Kg}$; $n = 3.5$; half-wing area $S = 8 \text{ m}^2$.

The load for the half-wing will be

$$n \times (Q-Q_a) = 3.5 (300-100) = 700 \text{ kg}.$$
\[ C_1 = a \times \frac{P}{S} = 0.5 \times 700/8 = 43.75 \text{ kg/m} \]

\[ C_2 = (a + b) \times \frac{P}{S} = 1.5 \times 700/8 = 131.25 \text{ kg/m} \]

In the wing schematic, the chords in an appropriate scale represent the ordinates \( y \) of the load diagram.

**Cantilever Wing. Shear stress. Bending moment.** Let us consider first a tapered wing without external means of support. In a generic section \( S \) of the wing, the shear stress is none other than the sum of all the loads outside this section, while the bending moment is given by the product of this outside load and the distance \( d \) of the center of gravity of the section.

To determine these shear stresses and bending moments in the various sections of the wing, we may use two methods: analytic and graphic.

![Figure 9-5](image)

**Analytic method for a tapered cantilever wing.** The shear and bending loads are calculated by integrating the load once and then a second time. This gives us the relation that ties the load distribution to the wing span.

From Figure 9-4, we get the equation of the line \( AB \) that represents the load distribution

\[ y = \left(\frac{C_2 - C_1}{L}\right)x + C_1 \quad [28] \]

for every value of \( x \) distance of the section to the tip, we get the value of load \( y \).

Integrating this function will give us the one for shear stress

\[ T_x = \frac{C_2 - C_1}{L} \cdot \frac{x^2}{2} + C_1 x \quad [29] \]

and integrated one more time will give us the function of the bending moment.
\[ M_{f x} = \frac{C_2 - C_1}{L} \cdot \frac{x^3}{6} + \frac{C_1 x^2}{2} \quad [30] \]

In these equations \( C_1 \), \( C_2 \), and \( L \) are known values, and for every value of \( x \) we get the values for \( T \) and \( M_f \).

Example. Let us consider the wing from the previous example and obtain \( C_1 \) and \( C_2 \), let’s round off the values to

\[ C_1 = 44 \text{ kg/m} \]
\[ C_2 = 131 \text{ kg/m} \]
\[ L = 8 \text{ m} \]

Let’s suppose we want to obtain the values of \( T \) and \( M_f \) at a distance from the tip of \( x = 4 \text{ m} \).

\[ T_x = \frac{C_2 - C_1}{L} \cdot \frac{x^2}{2} + C_1 x = \left( \frac{131 - 44}{8} \right) \cdot \frac{16}{2} + 44 \cdot 4 = \frac{87}{8} \cdot 8 + 176 = 263 \text{ kg} \]

\[ M_f = \frac{C_2 - C_1}{L} \cdot \frac{x^3}{6} + \frac{C_1 x^2}{2} = \left( \frac{131 - 44}{8} \right) \cdot \frac{64}{6} + 44 \cdot \frac{16}{2} = \frac{87}{8} \cdot 10.7 + 352 = 468 \text{ kgm} \]

By repeating the calculation for the other values of \( x \) we obtain the shear loads and bending moments of the various sections of the wing.

In practice \( T \) and \( M_f \) are calculated for the location of wing ribs.

**Rectangular cantilever wing.** In the case of a rectangular wing, we will have a load diagram with a line parallel to the \( x \) axis as shown in Figure 9-6, so \( C_1 = C_2 = C \).

Therefore the load equation is \( y = C \), thus the load is constant.

And with \( C_2 - C_1 = 0 \) the shear equation will be

\[ T_x = C \cdot x \quad [31] \]
And for the bending moment

\[ M_f = C \cdot \frac{x^2}{2} \quad [32] \]

Thus, the calculations for \( T \) and \( M_f \) are rather simple for a rectangular wing.

**Rectangular-tapered cantilever wing.** Finally, let us consider a wing with a rectangular center section and an outboard section tapered to the wing tip. See loading diagram in Figure 9-7.

![Figure 9-7](image)

The shear equation for the tapered portion from the wing tip to Section B, as we have seen in equation 29 is

\[ T_{x1} = \frac{C_2 - C_1}{l_1} \cdot \frac{x_1^2}{2} + C_1 x_1 \]

Where \( x_i \) may vary from zero to \( l_i \)

\[ 0 < x_i < l_i \]

For the rectangular portion from \( B \) to \( C \), the shear is given by the summation of the maximum in \( B \) that is equivalent to

\[ T_B = \left( \frac{C_2 - C_1}{l_1} \right) \cdot \frac{l_i^2}{2} + C_1 l_i \]

or

\[ T_B = (C_2 - C_1) \cdot \frac{l_i}{2} + C_1 l_i \]

with the resultant of the rectangular portion starting from \( B \) that is equal to equation 31.
\[ T_{x2} = C_2 \cdot x_2 \]

Where \( x_2 \) is taken starting from \( B \) and may vary from zero to \( l_2 \)

\[ 0 < x_2 < l_2 \]

Therefore in a generic section between \( B \) and \( C \) shear is equivalent to

\[ T_{x2} = T_B + C_2 \cdot x_2 \]

To represent a wing of this type, we use a diagram as shown in Figure 9-8 where the line is parabolic from \( 0 \) to the \( B \) section and linear from the \( B \) section to the fuselage.

For the bending moment also, the two sections are considered separately. For the tapered portion from the tip to section \( B \) it is the same as we have previously seen in equation 30

\[ M_{fx1} = \frac{C_2 - C_1}{l_1} \cdot \frac{x_1^3}{6} + C_1 \cdot \frac{x_1^2}{2} \]

For the rectangular section from \( B \) to \( C \) the moment is equal to the product of the load in the tapered section and the distance \( d \) from the center of gravity \( G \) for the generic section \( s \) under consideration as shown in Figure 9-9 and adding the moment of the rectangular section originating at \( B \) that is

\[ M_{fx2} = \left( \frac{C_2 - C_1}{l_1} \right) \cdot \frac{x_1^3}{6} + C_1 \cdot \frac{x_1^2}{2} \]

The distance of the center of gravity \( G \) from the \( B \) section may be found either with a simple graphic method, or with the ratio between the bending moment and the shear in \( B \).
Calling this distance $e$, we have

$$e = \frac{M_{fb}}{T_B}$$

Finally, it follows that the bending moment equation in the rectangular section is

$$M_{fx} = T_B (e + x_2) + C_2 \cdot \frac{x_2^2}{2}$$

Where $T_B$ is the shear stress at B, and $(e + x_2)$ is the distance of the center of gravity of the load on the tapered section we are considering.

Here also, the diagram of the total moment may be considered as the summation of the one given by the load in the tapered section ($\bar{R}$), with the one given by the rectangular section ($S$) in Figure 9-10.

The resulting line is parabolic (cubic parabola) from 0 to B, linear from B to D, and again parabolic from D to C.
Example. Let us consider a wing of this type, a rectangular section followed by a linearly tapered section.

Let it be:

\[ C_1 = 40 \text{ kg/m.} \]
\[ C_2 = 130 \text{ Kg/m} \]
\[ l_1 = 4m \]
\[ l_2 = 5m \]

We want to determine \( T \) and \( M \) in a section \( s \) at 7m from the tip.

We will have therefore \( x_2 = 3m \).

For shear at section \( B \), the maximum value for the tapered section will be

\[
T_B = \left( \frac{C_2 - C_1}{l_1} \right) \cdot \frac{l_1^2}{2} + C_1l_1 = \frac{130 - 40}{4} \cdot \frac{4^2}{2} + 40 \cdot 4 = 340\text{kg}
\]

The shear in this section \( s \) will be

\[
T_s = T_B + C_2x_2 = 340 + 130 \cdot 3 = 730\text{kg}
\]

Let us determine now \( M_f \). In Section \( B \) it is equal to

\[
M_{fb} = \left( \frac{C_2 - C_1}{l_1} \right) \cdot \frac{l_1^3}{6} + \frac{C_1l_1^2}{2} = \frac{130 - 40}{4} \cdot \frac{4^3}{6} + 40 \cdot \frac{4^2}{2} = 560\text{kgm}
\]

The distance \( e \) of the center of gravity of the load on the tapered section is

\[
e = \frac{M_{fb}}{T_B} = \frac{560}{340} = 1.65m
\]
The bending moment in the section $s$ is therefore

$$M_{fs} = T_b(e + x_2) + C_2 \frac{x_2^2}{2} = 340(1.65 + 3) + 130 \frac{3^2}{2} = 2165 \text{kgm}$$

We have seen how the shear stresses and moment in a tapered wing are calculated analytically. Let us now continue with a graphic procedure.

**Graphic method.** The stress determination of $T$ and $M_f$ are based on a graphic integration. In this method, the function of load is expressed graphically by a curve that when integrated one or two times will give us the diagrams of shear and bending moment.

Generally to complete a diagram where $l$ as an example is the line that determines it, we divide this in many parallel strips that are perpendicular to the $x$ axis. We trace the middle of these strips, their intersection with the line $l$ are projected horizontally to the $y$ axis. We then take a point $P$ at will on the $x$ axis, and we connect this point with each of the projections on the $y$ axis.

We will have a number of lines with various angles all originating from $P$. The distance of $P$ from the vertical axis where the projected points of $l$ were traced is called the polar distance, and it is indicated with the letter $\lambda$.

Starting from the axis origin $O$, we trace segments parallel to the lines $s_1, s_2\ldots s_n$ that will intersect the vertical lines in points $1, 2\ldots n$. The resulting segmented line $I$ is the integral line we were looking for.

To read the diagram we need to establish the scale for the $y$ axis. This is obtained by the product of the value of the $x$ axis by the ordinate values of line $I$ and the distance of polar $\lambda$. 

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The Glider

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Example. Let’s construct a graphic diagram of shear and moment. Let’s use a convenient scale for the shear loads of a cantilever wing as shown in Figure 9-13

1 cm = 0.5 m for the dimensions on the x axis
1 cm = 25 kg/m for the loads on the y axis.

In relation to the wing’s ribs, from the smallest one to the largest one, and with a linear variation in between them, the load is

\[
C_1 = 50 \text{ kg/m} \\
C_2 = 130 \text{ kg/m}
\]

The half-wing span is \( L = 8 \text{ m} \). Taking \( P_1 \) at a distance from y axis

\[
\lambda_1 = 8 \text{ cm}
\]

we divide the loading diagram into ten strips, and as we have seen, we obtain the shear diagram.

We need now to establish the scale in order to read the diagram. This is given by the product of the loading scale, the length scale and the polar distance \( \lambda_1 \). Thus the shear scale is

\[
1 \text{ cm} = 25 * 0.5 * 8 = 100 \text{ kg}
\]

In the diagram the maximum value of \( T \) is given as 7.2 cm, therefore

\[
T = 7.2 * 100 = 720 \text{ kg}
\]
To verify this, let’s determine the total load on the half-wing, that is, the maximum shear. The average load intensity is

\[ \frac{C_1 + C_2}{2} = \frac{50 + 130}{2} = 90 \text{ kg/m} \]

This multiplied by the span \( L \) gives us the total load of

\[ P = 90 \times 8 = 720 \text{ kg} \]

Exactly coinciding with the value found graphically.

Using the same procedure, we now integrate the shear diagram plotting a polar distance \( \lambda_2 = 5 \text{ cm} \) to the right of the diagram, so not to interfere with the previous lines. The resulting new diagram will be the one for the bending moment.

The scale is given by the product of the shear with the length and the polar distance \( \lambda_2 \). Thus, the moment scale is

\[ 1 \text{ cm} = 100 \times 0.5 \times 5 = 250 \text{ kgm} \]

From the diagram we obtain the maximum value of the bending moment as

\[ M_f = 9.85 \times 250 = 2460 \text{ kgm} \]

The advantages of the graphic method over the analytic one are several.

First of all, with the graphic integration method we can derive to the diagrams of shear much faster than we can analytically and also the procedure is not complicated by the various shapes of wing being considered, that is for the distribution of loads it is not always possible to analytically establish an equation that represents the distribution of the load itself.

The precision of the graphic method may be inferior to the analytic one, but with the graphic method is impossible to commit the gross errors are often easily made analytically. Also for greater safety, all analytically-found values should be reported graphically in order to check their validity.

In the graphic method, it is advisable to operate with a small scale in order to obtain maximum precision. In practice 1/10 used for the lengths, and the loads and shears diagrams are divided in many strips.