

Some Broad-Band Transformers*

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Summary—Several transmission line transformers are described which have bandwidth ratios as high as 20,000:1 in the frequency range of a few tens of kilocycles to over a thousand megacycles. Experimental data are presented on both transformers and hybrid circuits.

Typical applications are: interstage transformers for broad-band amplifiers; baluns for driving balanced antennas and broad-band oscilloscopes; and hybrids for use in pulse reflectometers, balanced modulators, etc.

These transformers can be made quite small. Excellent transformers have been made using ferrite toroids having an outside diameter of 0.080 inch.

SEVERAL transmission line transformers having bandwidths of several hundred megacycles are described here. The transformers are shown in Figs. 1-9. When drawn in the transmission line form, the transforming properties are sometimes difficult to see. For this reason, a more conventional form is shown

with the transmission line form. Some winding arrangements are also shown. Certain of these configurations have been discussed elsewhere and are included here for the sake of completeness [1-4].

In conventional transformers the interwinding capacity resonates with the leakage inductance producing a loss peak. This mechanism limits the high frequency response. In transmission line transformers, the coils are so arranged that the interwinding capacity is a component of the characteristic impedance of the line, and as such forms no resonances which seriously limit the bandwidth. Also, for this reason, the windings can be spaced closely together maintaining good coupling. The net result is that transformers can be built this way which have good high frequency response. In all of the transformers for which experimental data are presented, the transmission lines take the form of twisted pairs. In some configurations the high frequency response is determined by the length of the windings and while any type of transmission line can be used in principle, it is

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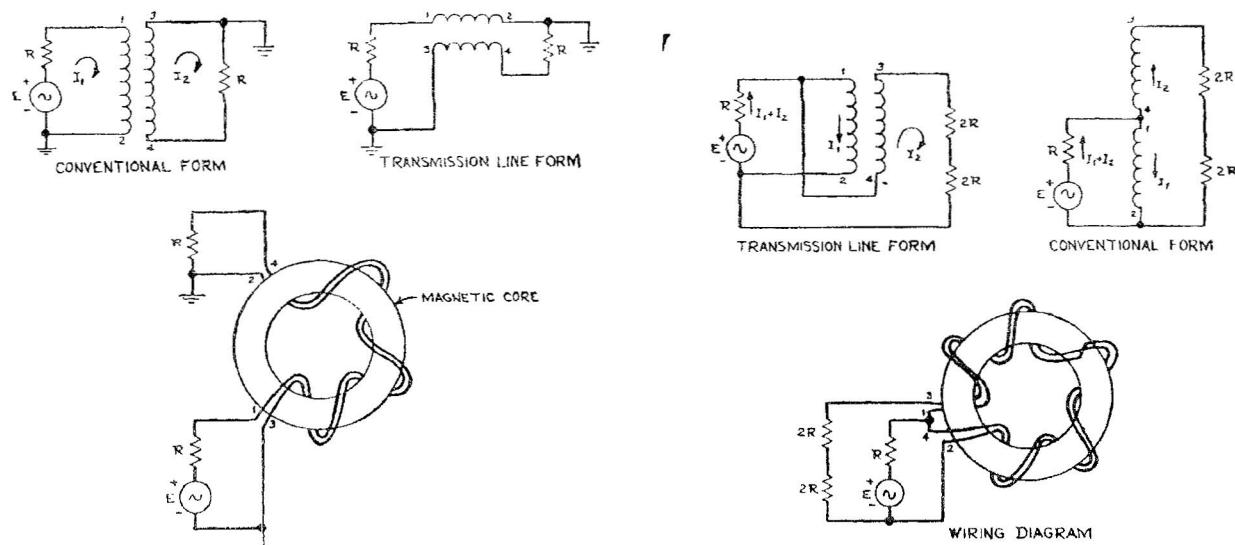


Fig. 1—Reversing transformer.

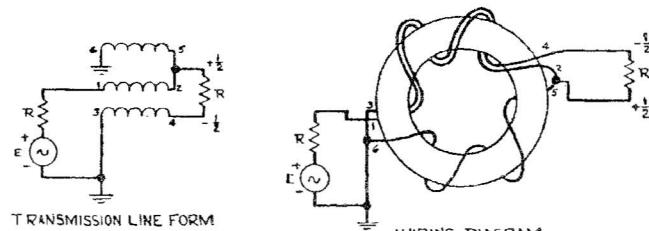


Fig. 2—Unbalanced to balanced transformer.

quite convenient to make very small windings with twisted pairs.

The sketches showing the conventional form of transformer demonstrate clearly that the low frequency response is determined in the usual way, *i.e.*, by the primary inductance. The larger the core permeability, the fewer the turns required for a given low frequency response and the larger the over-all bandwidth. Thus a good core material is desirable. Ferrite toroids have been found very satisfactory. The permeability of some ferrites is very high at low frequencies and falls off at higher frequencies. Thus, at low frequencies, large reactance can be obtained with few turns. When the permeability falls off the reactance is maintained by the increase in frequency and good response is obtained over a large frequency range. It is important that the coupling be high at all frequencies or the transformer action fails. Fortunately, the bifilar winding tends to give good coupling. All of the cores used in the experimental transformers described here were supplied by F. J. Schnettler of the Bell Telephone Laboratories, Inc.

POLARITY REVERSING TRANSFORMER—FIG. 1

This transformer consists of a single bifilar winding and is the basic building block for all of the transformers. That a reversal is obtained is seen from the conventional form which indicates current polarities. Both

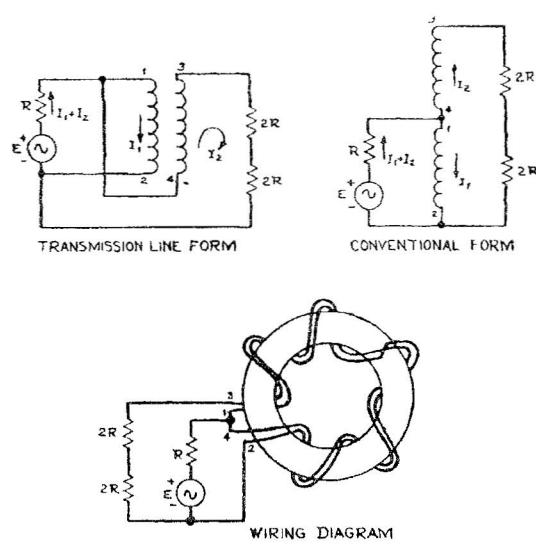


Fig. 3—4:1 Impedance transformer.

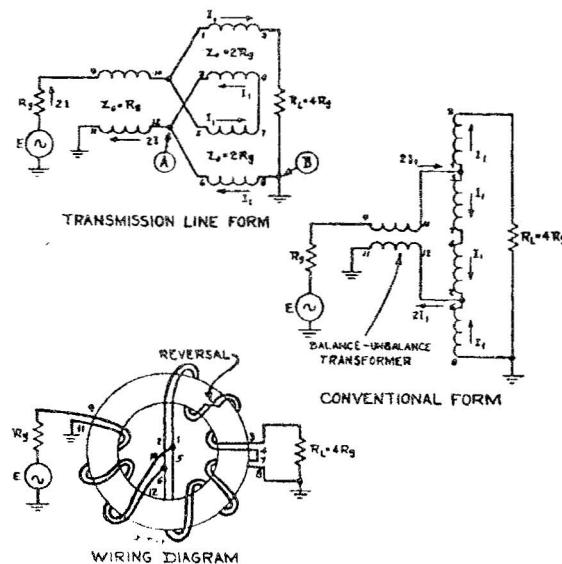


Fig. 4—4:1 Impedance transformer. Unbalanced—symmetrical.

ends of the load resistor are isolated from ground by coil reactance. Either end of the load resistor can then be grounded, depending upon the output polarity desired. If the center of the resistor is grounded, the output is balanced. A suitable winding consists of a twisted pair of Formex insulated wire. In such a winding, the primary and secondary are very close together, insuring good coupling. The interwinding capacity is absorbed in the characteristic impedance of the line.

At high frequencies this transformer can be regarded as an ideal reversing transformer plus a length of transmission line. If the characteristic impedance of the line is equal to the terminating impedances, the transmission is inherently broadband. If not, there will be a dip in the response at the frequency at which the transmission line is a quarter-wavelength long. The depth of the dip

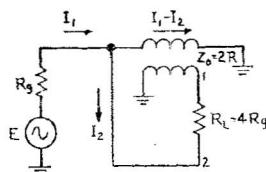
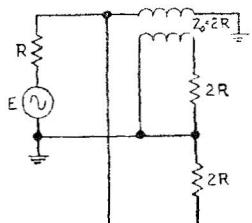
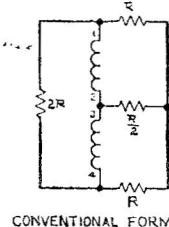
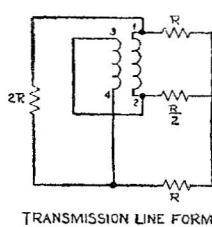
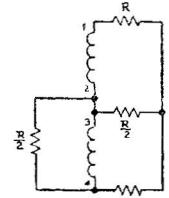
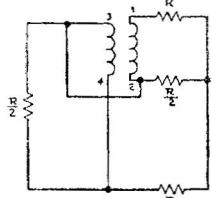


Fig. 5—Balanced—unbalanced 4:1 impedance transformer.



(a)



(b)

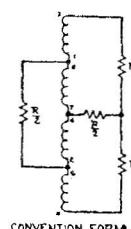
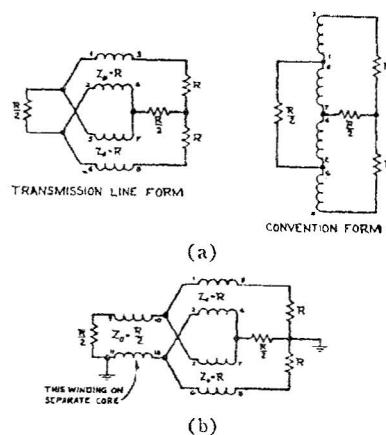
Fig. 6—(a) Basic hybrid. (b) Unsymmetrical hybrid with equal conjugate impedances.

is a function of the ratio of terminating impedance to line impedance and is easily calculated.

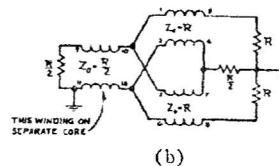
Experimental data on a reversing transformer are shown in Figs. 10 and 11. Fig. 10 is the response of a transformer with no extra impedance matching. The return loss of this transformer to a 3 m μ sec pulse is 20 db. The transformer of Fig. 11 has been adjusted to provide more than 40 db return loss to a 3 m μ sec pulse. The transformer loss (about 0.5 db before matching) is matched to 75 ohms with the two 3.8-ohm resistors. The inductance is tuned out with the capacity of the resistors to the ground plane. The match was adjusted while watching the reflection of a 3 m μ sec pulse.

BALANCED-TO-UNBALANCED 1:1 IMPEDANCE TRANSFORMER—FIG. 2

This is similar to Fig. 1 except that an extra length of winding is added. This is necessary to complete the path for the magnetizing current.



(a)



(b)

Fig. 7—(a) Symmetrical hybrid with equal conjugate impedances. (b) Unbalanced symmetrical hybrid with equal conjugate impedances.

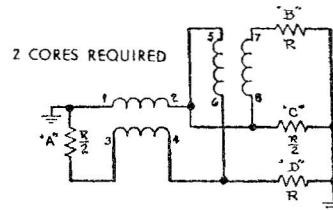


Fig. 8—Hybrid with equal conjugate impedances. Each arm single ended.

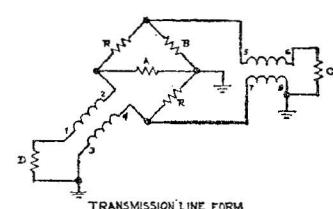
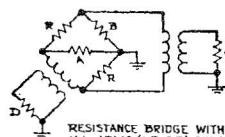
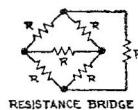


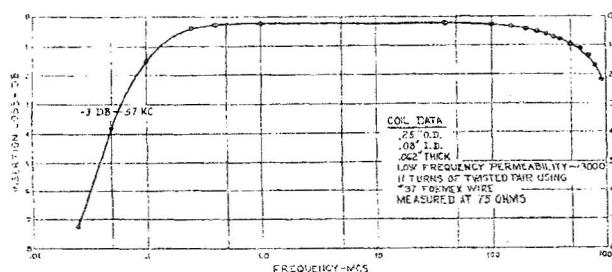
Fig. 9—Resistance hybrid with equal impedance loads. (This hybrid has 3 db loss in addition to transformer loss.)

UNBALANCED-UNSYMMETRICAL 4:1 IMPEDANCE TRANSFORMER—FIG. 3

This transformer is interesting because with it a 4:1 impedance transformation is obtained with a single bifilar winding such as used in the reversing transformer. The transforming properties are evident from Fig. 3. Not so easily seen is the high frequency cutoff characteristic.

The response of this device at high frequencies is derived in the Appendix and only the result for matched impedances is given here.

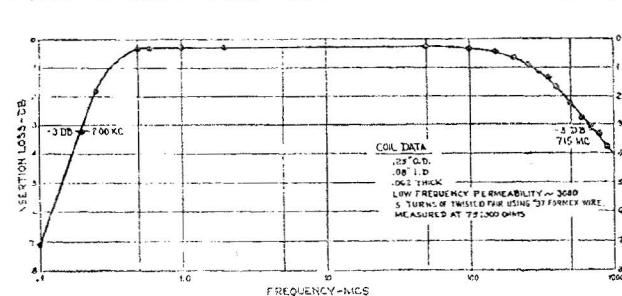
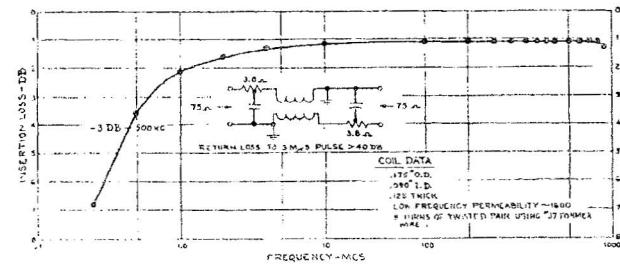
$$\frac{\text{Power Available}}{\text{Power Output}} = \frac{(1 + 3 \cos \beta l)^2 + 4 \sin^2 \beta l}{4(1 + \cos \beta l)^2}, \quad (1)$$



BALANCED-TO-UNBALANCED 4:1 IMPEDANCE TRANSFORMERS—FIG. 5

The circuit of Fig. 5 is quite simple. The single bifilar winding is used as a reversing transformer as in Fig. 1. The high frequency cutoff is the same as that for the transformer of Fig. 3.

In some applications it is desirable to omit the physical ground on the balanced end. In such cases, Fig. 5(b) can be used. The high frequency cutoff is the same as for the transformer of Fig. 3. The low frequency analysis is presented in Appendix B.



where β is the phase constant of the line, and l is the length of the line. Thus, the response is down 1 db when the line length is $\lambda/4$ wavelengths and the response is zero at $\lambda/2$. For wideband response this transformer must be made small. For a plot of (1) see Fig. 16.

Experimental data are given for a transformer of this type in Fig. 12.

UNBALANCED-SYMMETRICAL 4:1 IMPEDANCE TRANSFORMER—FIG. 4

This configuration requires three bifilar windings as shown in Fig. 4. All three windings can be placed on one core, a procedure which improves the low frequency response.¹ When winding multiwinding transformers the following well-known rule should be followed: with the generator connected and the load open, a completed circuit should be formed by the windings so that the core will be magnetized. The fields set up by the currents should be arranged so as to aid each other.

¹ Pointed out to the author by N. J. Pierce of Bell Telephone Labs., Inc., Holmdel, N. J.

HYBRID CIRCUITS: FIGS. 6-9

Various hybrid circuits are developed from the basic form using the transformers discussed previously. The drawings are very nearly self-explanatory. In all hybrids in which all four arms are single-ended, it has been found necessary to use two cores in order to get proper magnetizing currents.

Two hybrids have been measured and data included here. The response of a hybrid of the type shown in Fig. 8 is given in Fig. 13. For this measurement $R = 150$ ohms. In order to measure the hybrid in a 75-ohm circuit, arms B , D were measured with 75-ohm series resistances in series with the 75-ohm measuring gear. This accounts for 3 db of the loss. Under these conditions arms B and D have a 6 db return loss.

The transmission of the resistance hybrid of Fig. 9 is given in Fig. 14. This hybrid has been matched using the technique described previously for the reversing transformer. The results of this matching are included in the figure. This hybrid was designed for use in a pulse reflectometer, the main part of which is a stroboscopic oscilloscope with a resolution of better than 3 μ sec. The oscilloscope was designed by W. M. Goodall.

APPLICATIONS

Many applications for these transformers will occur to the reader. For purposes of illustration, a few of them are listed here.

- 1) The reversing transformer of Fig. 1 can be used to reverse the polarity of short pulses, an operation which is frequently necessary. It has also been used in balanced detectors and to drive push-pull amplifiers from single-ended generators.
- 2) The transformers of Figs. 2 and 5(b) are useful for driving balanced antennas. The circuit of Fig. 5(b) may find application in connecting twin lead transmission line to commercial television receivers.
- 3) The transformer of Fig. 3 has found wide use in broadband amplifier interstages. It will also be useful in transforming the high output impedances of distributed amplifiers to coaxial cable impedances. They can also be cascaded to get higher turns ratios.

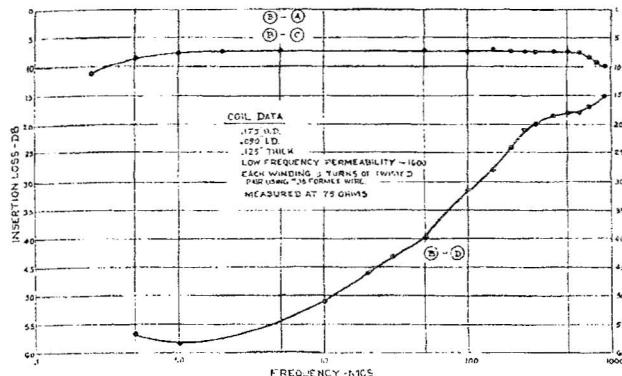


Fig. 13—Hybrid of Fig. 8. Insertion loss vs frequency.

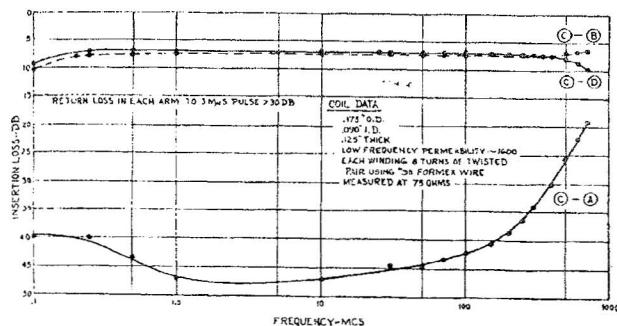


Fig. 14—Matched resistance hybrid. Insertion loss vs frequency.

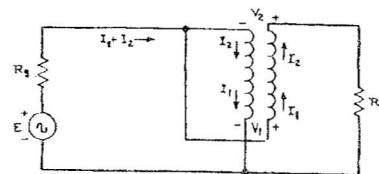
- 4) The circuit of Fig. 5(a) has been used to drive broadband oscilloscopes, with balanced inputs, from single-ended generators. It can also find use in balanced detectors.
- 5) Hybrids have many uses such as in power dividers, balanced amplitude and phase detectors; as directional couplers for pulse reflectometers, IF and broadband sweepers. They might also be used as necessary components in a short pulse repeater for passing pulses in both directions on a single transmission line.

APPENDIX A

The high frequency response of the circuit of Fig. 3 is derived from Fig. 15. The loop equations are as follows:

$$\begin{aligned} e &= (I_1 + I_2)Rg + V_1 \\ e &= (I_1 + I_2)Rg - V_2 + I_2R_L \\ V_1 &= V_2 \cos \beta l + jI_2 Z_0 \sin \beta l \\ I_1 &= I_2 \cos \beta l + j \frac{V_2}{Z_0} \sin \beta l. \end{aligned} \quad (2)$$

This set of equations is solved for the output power P_0 . $P_0 = |I_2|^2 R_L$



CHARACTERISTIC IMPEDANCE OF BIFILAR WINDING $= Z_0$
THE REACTANCE OF THE WINDINGS $X \gg R_L, R_g$

Fig. 15—Transformer schematic.

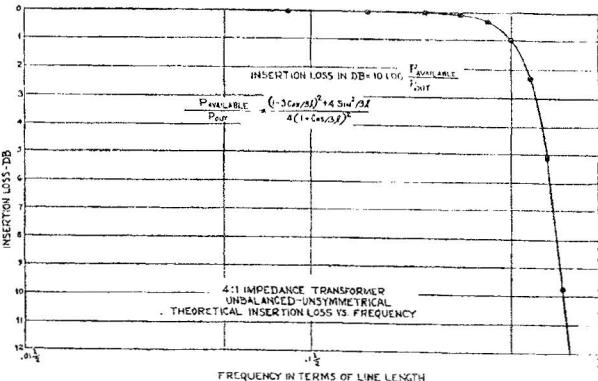


Fig. 16—Theoretical insertion loss vs frequency.

From this expression, the conditions for maximum power transmission are obtained by setting $l=0$ and setting $dP_0/dR_L|_{l=0}=0$. The transformer is matched when $R_L=4Rg$. The optimum value for Z_0 is obtained by minimizing the coefficient of $\sin^2\beta l$ in (3). In this manner the proper value for Z_0 is found to be $Z_0=2Rg$.

Now, setting $R_L=4Rg$ and $Z_0=2Rg$, (3) reduces to

$$P_0 = \frac{e^2(1 + \cos \beta l)^2}{Rg[(1 + 3 \cos \beta l)^2 + 4 \sin^2 \beta l]} \quad (4)$$

Also,

$$P_{\text{available}} = \frac{e^2}{4Rg}, \quad (5)$$

and dividing (4) by (5):

$$\frac{\text{Power Available}}{\text{Power Output}} = \frac{(1 + 3 \cos \beta l)^2 + 4 \sin^2 \beta l}{4(1 + \cos \beta l)^2}. \quad (6)$$

This function is plotted in Fig. 16.

The impedances seen at either end of the transformer with the other end terminated in Z_L have been derived. They are:

Z_{in} (low impedance end)

$$= Z_0 \left(\frac{Z_L \cos \beta l + jZ_0 \sin \beta l}{2Z_0(1 + \cos \beta l) + jZ_L \sin \beta l} \right) \quad (7)$$

$$P_0 = |I_2|^2 R_L = \frac{e^2(1 + \cos \beta l)^2 R_L}{[+2Rg(1 + \cos \beta l) + R_L \cos \beta l]^2 + \left[\frac{Rg R_L + Z_0^2}{Z_0} \right]^2 \sin^2 \beta l} \quad (3)$$

and

Z_{in} (high impedance end)

$$= Z_0 \left(\frac{2Z_L(1 + \cos \beta l) + jZ_0 \sin \beta l}{Z_0 \cos \beta l + jZ_L \sin \beta l} \right). \quad (8)$$

APPENDIX B

In the low frequency analysis of the transformer of Fig. 5 the series impedance of each half of the bifilar winding is denoted by Z . The loop equations are:

$$E = (Rg + Z)I_1 - (Z + kZ)I_2$$

$$E = (Rg - kZ)I_1 + (R_L + Z + kZ)I_2, \quad (9)$$

from which

$$\frac{I_1}{I_2} = \frac{R_L + 2Z(1 + k)}{Z(1 + k)} \approx 2 \text{ if } Z \gg R_L. \quad (10)$$

We now proceed to calculate the voltages from points 1 and 2 to ground

$$V_{2G} = E = I_1 Rg.$$

When the transformer is matched, $E = 2I_1 Rg$ and

$$V_{2G} = I_1 Rg. \quad (11)$$

Similarly,

$$V_{1G} = I_2 Z - kZ(I_1 - I_2).$$

With the aid of (10) this can be rearranged to

$$V_{1G} = ZI_1 \left[\frac{Z(1 + k)^2 - kR_L - 2kZ(1 + k)}{R_L + 2Z(1 + k)} \right]. \quad (12)$$

Now let the coupling coefficient $k = 1$, then

$$V_{1G} = I_1 Z \left[\frac{-kR_L}{R_L + 2Z(1 + k)} \right] \approx -\frac{I_1 R_L}{4}$$

for $Z \gg R_L$.

When the transformer is matched, $R_L = 4Rg$ so that

$$V_{1G} = I_1 Rg = -V_{2G}, \quad (13)$$

and the load is balanced with respect to ground.

From (13) it is clear that the center point of R_L is at ground potential. This point can therefore be grounded physically, resulting in Fig. 5(a).

ACKNOWLEDGMENT

In addition to those mentioned in the text, the author is indebted to D. H. Ring for many stimulating discussions on every aspect of these transformers.

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