IONOSPHERIC RADIO PROPAGATION

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IONOSPHERIC RADIO PROPAGATION

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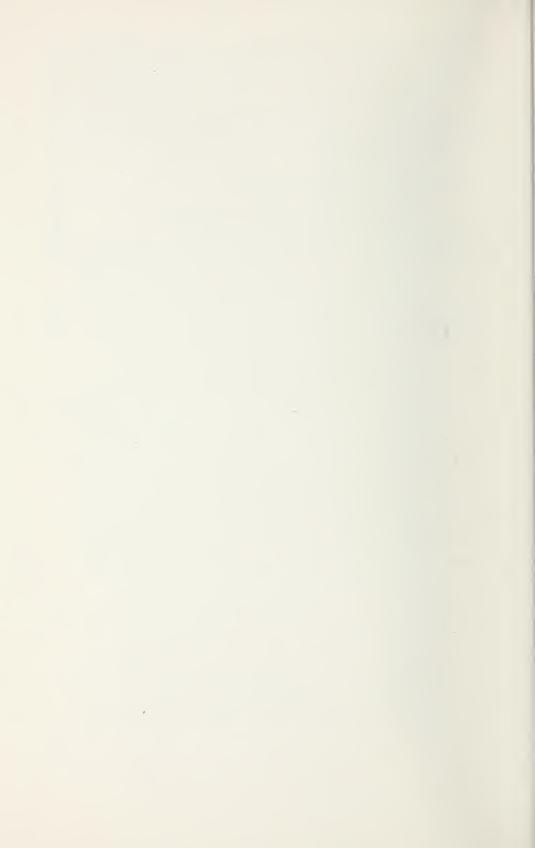
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IONOSPHERIC RADIO PROPAGATION

Preface

The purpose of this book is to replace, in part, a previous publication of the National Bureau of Standards (Circular 462) with the same title. Since the publication of the earlier work in 1948, the whole subject has undergone a considerable transformation. This is partly due to the special geophysical efforts known as the International Geophysical Year (1957–8) and the International Year of the Quiet Sun (1964–5) and to the advent of the Space Age. The scope of the present work has therefore been broadened to include aspects of ionospheric radio propagation which were not treated in the earlier publication.

Such topics as electron-layer production, the geomagnetic field, magneto-ionic theory, and oblique propagation have been expanded with respect to the earlier treatment. On the other hand, such topics as frequency prediction and atmospheric noise have been less thoroughly dealt with because they have been well treated in other publications [1, 2, 3]. Thus, those persons interested in the purely practical aspects of ionospheric radio communications should use this book in conjunction with these other publications.

The bulk of the material in the book is taken from the published literature. However, a certain amount has been based on, or taken verbatim from, certain of the lecture notes prepared by the CRPL staff for the courses in Radio Propagation held in Boulder, Colorado, during the summers of 1961 and 1962. Recognition of the sources of the material has been given in the text (or as footnotes). I wish to express my deepest appreciation to those lecturers who have given me permission to use their notes. Of course, it is impossible to list the names of all those who have contributed in an indirect manner and I apologize for any inadvertent omissions. My thanks are also expressed to the many authors and publishers who have given generous permission for the reproduction of their illustrations. The work of the following authors has been particularly helpful in the preparation of the respective chapters.

Chapter 1: S. Chapman, T. E. VanZandt.

Chapter 3: J. S. Belrose, R. W. Knecht, J. M. Watts, J. W. Wright. Chapter 4: T. N. Gautier, R. S. Lawrence, R. K. Salaman.

¹ Figures in brackets indicate the literature references on p. XIV.

Chapter 5: H. J. A. Chivers, T. N. Gautier.

Chapter 6: V. Agy, R. W. Knecht, C. G. Little.

Chapter 7: W. Q. Crichlow, G. W. Haydon, M. Leftin, S. Ostrow.

Chapter 8: K. L. Bowles, R. S. Cohen, R. C. Kirby, G. Sugar.

Chapter 9: J. S. Belrose, C. J. Chilton, J. H. Crary, D. D. Crombie, A. Glenn Jean, W. L. Taylor, J. R. Wait.

It is intended that the reader who wishes to pursue the subject further will consult the references cited. To this end, whenever possible, the most recent references are cited, as the older (and sometimes more important) works are invariably listed therein. The reference lists are augmented by acknowledgments to the sources of published figures and the reader is advised to consult these references also. An excellent bibliography of ionospheric work has been compiled by Dr. L. A. Manning [4].

While the book is devoted mostly to the propagation of high-frequency radio waves, two chapters have been included in order to give the reader a better perspective of the relationship of the high-frequency band to the lower frequency (LF and VLF) bands and upper (VHF) frequency band.

The book was prepared during a visit to the Radio Research Station of the Department of Scientific and Industrial Research in Slough, England. I want to extend my appreciation to Mr. J. A. Ratcliffe, Director of the Radio Research Station, and his staff for their kindness and help in the preparation of the manuscript and in supplying certain illustrations. In particular, I should like to thank J. W. King, L. Thomas, and W. R. Piggott.

Finally, I should like to thank Mr. J. W. Finney, Mrs. T. Simpson, Dr. J. R. Lebsack, and the staffs of the Technical Information Office (NBS, Boulder) and of the Technical Publications Division (NBS, Washington) for their help in the preparation of the typescript, and my colleagues in the Central Radio Propagation Laboratory and the University of Colorado who kindly read and criticized the earlier versions.

It is hoped that the book will be of use both to research workers and to communications engineers who already have some background knowledge of radio propagation via the ionosphere.

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CHAPTER 1

The Earth's Atmosphere, Geomagnetism, and the Sun

1.1. NOMENCLATURE

Throughout this book, the terminology used to describe the various regions of the upper atmosphere will be that based upon the temperature distribution of the neutral atmosphere [1]. This distribution is shown in figure 1.1, and the following terminology is widely used.

The mesosphere, which lies in the height range of 50 to 85 km, is a region of decreasing temperature with height.

The thermosphere, above 85 km, is a region in which the temperature increases with height.

These "regions" are not well defined and the transition regions are called "pauses."

In addition to the terminology based on temperature, others have been devised based on alternative physical quantities and processes. Two of these are illustrated in figure 1.1. For example, one terminology is based on the fact that turbulence predominates below about 100 km, whereas diffusive separation sets in above about 110 km. Above about 500 km is a region called the exosphere.

The term ionosphere was first applied by Sir Robert Watson-Watt to that part of the atmosphere in which free ions exist in sufficient quantities to affect the propagation of radio waves. The ionosphere can, therefore, be considered as lying between about 40 to 50 km and several earth radii. This definition is essentially that adopted by the Institute of Radio Engineers [2].

It is convenient to define a region as a section of the atmosphere within which there can exist ion distributions called layers. A division

¹ Figures in brackets indicate the literature references on p. 44.

of the ionosphere into regions is given in table 1.1 together with the layers which may exist within these regions. The electron distribution within a region may not contain a peak of electron density.

1.2. PRESSURE AND DENSITY VARIATIONS

The relationship between pressure p and density ρ at any height h is given by the "barometric equation," which is derived as follows: con-

Table 1.1. Ionospheric regions and layers

| Height range (km) | Region | Layers |
|--|-------------|---------------------------------------|
| 50–90 90–(120–140) Above (120–140) | D E F | $E_1, E_2, E_s \ F_1, F_{1^1_2}, F_2$ |

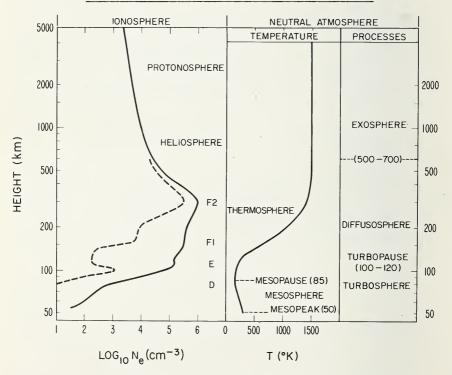


FIGURE 1.1. Atmospheric nomenclature.

(After T. E. VanZandt and R. W. Knecht, See fig. 1.3.)

sider an elementary cylinder of height dh and unit cross section. The net pressure difference dp between the top and bottom surfaces must equal the downward force due to the weight of the fluid in the cylinder, and is given by

$$dp = -\rho g \, dh$$

$$= -N\bar{m}g \, dh,$$
(1.1)

where g is the acceleration due to gravity, N is the number density of molecules and \overline{m} is the mean molecular mass. It should be remembered that N, \overline{m} , and g are all functions of height; e.g., g varies inversely as the square of the radius vector.

The perfect gas law is

$$p = NkT, (1.2)$$

where k is Boltzmann's Constant (=1.372 \times 10⁻¹⁶ erg/deg) and T is the absolute temperature.

From (1.1) and (1.2) we obtain

$$\frac{dp}{p} = -\frac{\overline{m}g}{kT}dh = -\frac{dh}{H}, \qquad (1.3)$$

where $H = kT/\bar{m}g$ is known as the "scale height" of the atmosphere, which again is height dependent. At the earth's surface the value of H is about 8 km.

In an isothermal atmosphere, integration of (1.3) gives

$$p = p_0 \exp\left(-\frac{h - h_0}{H}\right), \qquad (a)$$
(1.4)

or

$$\rho = \rho_0 \, \exp \left(-\frac{h - h_0}{H} \right), \qquad (b)$$

where p is the pressure at a height h corresponding to a pressure p_0 at a height h_0 . Similarly for the density ρ . The quantity $(h-h_0)/H$, which is the height difference in scale height units, is often denoted by z. Below about 100 km it is possible to measure T(h) and $\bar{m}(h)$ directly, by means of rockets, and hence to determine H. Above about 100 km, however, it is much easier to measure $\rho(h)$ and determine H from (1.3) expressed

in the form

$$\frac{1}{H} = -\frac{d}{dh} \ln p = \frac{\rho \cdot g}{\int_{h}^{\infty} \rho g \, dh} \,. \tag{1.5}$$

The following formulas are useful in calculating the scale height at any altitude:

$$H(km) = 0.848 \left(1 + \frac{h}{a}\right)^2 \frac{T \text{ °K}}{M(\text{gm/mole})},$$
 (1.6)

where a is the earth's radius (6370 km approximately). Equation (1.6) can be approximated by

$$H = 0.93 \, \frac{T}{M} \,, \tag{1.7}$$

which is correct to within 7.5 percent between 50 km and 500 km. It is exact at 300 km.

The temperature or scale height structure gives rise to the terminology indicated in the column labeled "temperature" in figure 1.1. Although the terminology is self-explanatory, the causes of the observed temperature structure deserve comment. The mesosphere is heated by the absorption by ozone of solar ultraviolet light with wavelengths between 2550 Å and 1650 Å. The thermosphere is heated by the dissociation and ionization of the atmospheric gases by solar ultraviolet light with wavelengths less than 1760 Å. Up to about 100 km, heat is lost mainly by infrared radiation. Above 100 km, on the other hand, heat is lost mainly by conduction downward towards the mesopause.

Below about 100 km, the specific heat of the atmosphere is so large that even though the rate of heat input almost vanishes at night, the temperature changes very little. Above 100 km the temperature is increasingly variable, both diurnally and with solar activity. For example, at 300 km the temperature decreases by about one third from day to night and probably by about half from sunspot maximum to sunspot minimum. The temperature may also increase by a factor of two during large ionospheric storms. These variations of the structure of the thermosphere are complex and poorly understood, but they are now the object of intensive research.

3.89 (20)

2.45 (19) 1.89 (18)

1.3. CHEMICAL COMPOSITION

Below about 85 km, turbulent mixing keeps the relative composition of the atmosphere essentially the same as that at the ground, which is given in table 1.2. In addition to the primary constituents, there are traces of other chemicals in the atmosphere, chief of which are water vapor, carbon dioxide, ozone, nitric oxide, and hydrogen.

Above about 90 km, dissociation of O₂ becomes important. This results in a marked decrease in the mean molecular weight and hence an increase in the scale height of the atmosphere.

The variation with height of some atmospheric properties are shown in tables 1.3 and 1.4. Table 1.3 is based upon the 1959 ARDC Model Atmosphere [3]. Table 1.4 is that given by Norton, Van Zandt, and Denison [4]. The differences between the values given in these tables are due to the different assumptions made with respect to the degree of dissociation of O₂ and the reference level used, etc. The differences may be taken as an indication of the degree of uncertainty to which the parameters are known.

It is impossible to construct a model of the atmosphere between 90 and 200 km which lies within the range of observations of total density, temperature, mean molecular weight, and density of O₂. For example, if a model agrees with the observations of total density and temperature, then deduced composition cannot agree with the observed composition, etc. It appears that the observations of at least one of these quantities are systematically wrong. Thus atmospheric models differ widely according to which observations have been accepted and which are ignored.

Total per cm² column Concentration Molecule Mass Percentage per cm3 N_2 28.022 78.084 2.098 (19) 1.678(25) O_2 5.629 (18) 4.501(24)32.009 20.946 39.960 2.007(23)A 0.934 2.510(17) CO_2 44.024 0.33 8.870 (15) 7.090(21)28.973 2.687 (19) 2.148(25)Air 100 He 1.13(20)1.41(14)

Ne

Kr

Table 1.2. Chemical composition at the ground

4.89 (14)

3.06 (13)

2.34(12)

Note that the figures in () represent the exponent of 10 by which the number shown must be multiplied.

Table 1.3. 1959 ARDC model atmosphere

| 1 | | | | | |
|------------------------|----------|--|---|---|---|
| Scale * Height | km | 8.43 6.55 6.39 6.83 7.73 | 8.42 7.61 6.34 4.98 5.00 | 6.05 14.62 26.46 38.35 44.93 | 48.12 60.28 72.48 85.04 101.6 113.0 |
| Molecular weight | | 28.966 28.966 28.966 28.966 28.966 | 28.966 28.966 28.966 28.97 28.97 | 28.90 28.71 28.45 28.04 27.36 | 26.32 21.95 19.56 18.28 17.52 |
| Pressure | mm Hg | 760.00 198.80 41.50 8.89 2.25 | 0.66 0.19 4.52 (-2) 7.56 (-3) 1.02 (-3) | 1.60 (-4) 1.53 (-5) 5.63 (-6) 3.01 (-6) 1.88 (-6) | $\begin{array}{c} 1.22 & (-6) \\ 1.92 & (-7) \\ 4.25 & (-8) \\ 1.19 & (-8) \\ 3.98 & (-9) \\ 1.53 & (-9) \end{array}$ |
| Conc." | m_3 | 2.55 (25) 8.60 (24) 1.85 (24) 3.71 (23) 8.32 (22) | 2.25 (22) 7.26 (21) 2.08 (21) 4.42 (20) 5.90 (19) | 7.80 (18) 3.10 (17) 6.40 (16) 2.41 (16) 1.32 (16) | 8.40 (15) 1.31 (15) 2.77 (14) 7.29 (13) 2.28 (13) 8.14 (12) |
| Collision frequency | sec_1 | 6.90 (9) 2.06 (9) 4.35 (8) 9.03 (7) 2.15 (7) | 6.06 (6) 1.86 (6) 4.80 (5) 9.10 (4) 1.22 (4) | 1.75 (3) 1.09 (2) 30.00 13.6 8.06 | 5.30 0.90 0.21 0.068 0.019 |
| Free path | w | $\begin{array}{c} 6.63 & (-8) \\ 2.00 & (-7) \\ 9.10 & (-7) \\ 4.50 & (-6) \\ 2.00 & (-5) \end{array}$ | 7.50 (-5) 2.34 (-4) 8.10 (-4) 3.80 (-3) 2.90 (-2) | 0.22 5.45 26.3 70.0 | 201 1,294 6,098 23,180 74,270 207,500 |
| Particle speed | m/sec | 459 400 398 411 437 | 454 431 391 348 348 | 382 593 795 955 1030 | 1062 1172 1266 1351 1429 1501 |
| Temp | °K | 288 223 217 231 261 | 283 254 210 166 166 | 200 477 850 1207 1371 | 1404 1423 1480 1576 1691 |
| Density | kg/m^3 | 1.22 4.14 (-1) 8.89 (-2) 1.78 (-2) 4.00 (-3) | 1.08 (-3) 3.51 (-4) 1.00 (-4) 2.12 (-5) 2.84 (-6) | $\begin{array}{c} 3.73 & (-7) \\ 1.48 & (-8) \\ 3.02 & (-9) \\ 1.12 & (-9) \\ 6.01 & (-10) \end{array}$ | 3.67 (-10) 4.75 (-11) 9.00 (-12) 2.20 (-12) 6.62 (-13) 2.30 (-13) |
| Altitude | km | 10 20 30 40 | 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.0 | 100 120 140 160 | 200 300 400 500 700 |

* Scale height calculated using eq (1.6).

Table 1.4. Model atmosphere (After Norton, VanZandt, and Denison [4]).

| [N ₂] | cm ⁻³ | 7.37 (12) 3.36 (12) 1.65 (12) 3.92 (11) 1.15 (11) | 4.13 (10) 1.81 (10) 9.46 (9) 5.55 (9) 3.50 (9) 2.32 (9) | 1.60 (9) 1.14 (9) 8.29 (8) 6.15 (8) 4.62 (8) 3.53 (8) | 2.72 (8) 2.11 (8) 1.66 (8) 1.31 (8) 1.04 (8) |
|-------------------|------------------|--|--|--|--|
| [O ₂] | cm ⁻³ | 6.49 (11) 2.96 (11) 1.45 (11) 7.37 (9) | 2.38 (9) 9.63 (8) 4.69 (8) 2.60 (8) 1.56 (8) 9.86 (7) | 6.52 (7) 4.44 (7) 3.11 (7) 2.22 (7) 1.61 (7) 1.19 (7) | 8.85 6.66 5.06 5.06 (6) 2.98 (6) |
| [0] | cm ⁻³ | 2. 66 (12) 1.21 (12) 5.94 (11) 2.40 (11) 1.07 (11) | 5.33 (10) 3.01 (10) 1.92 (10) 1.34 (10) 7.57 (9) | 5.96 (9) 3.92 (9) 3.25 (9) 2.72 (9) 2.30 (9) | 1.96 (9) 1.69 (9) 1.45 (9) 1.26 (9) 1.10 (9) |
| d | gm/cm³ | 4.48 (-10) 2.04 (-10) 1.00 (-10) 2.61 (-11) 8.57 (-12) | 3.47 (-12) 1.70 (-12) 9.76 (-13) 6.29 (-13) 4.34 (-13) 3.14 (-13) | 2.36 (-13) 1.83 (-13) 1.44 (-13) 1.16 (-13) 9.47 (-14) 7.83 (-14) | 6.53 (-14) 5.50 (-14) 4.66 (-14) 3.98 (-14) 3.42 (-14) |
| d | $dyne/cm^2$ | 2.93 (-1) 1.47 (-1) 7.73 (-2) 2.62 (-2) 1.16 (-2) | 6.40 (-3) 4.12 (-3) 2.91 (-3) 2.18 (-3) 1.70 (-3) 1.36 (-3) | 1.10 (-3) 9.12 (-4) 9.63 (-4) 6.44 (-4) 5.49 (-4) 4.70 (-4) | 4.06 (-4) 3.51 (-4) 3.06 (-4) 2.67 (-4) 2.34 (-4) |
| M | dyne/cm² | 25.27 25.27 25.27 23.83 22.53 | 21.51 20.74 20.16 19.68 19.29 18.95 | 18.66 18.41 18.19 17.99 17.82 | 17.52 17.39 17.27 17.17 17.17 |
| Н | km | 6.89 7.55 8.15 10.60 14.37 | 19.67 25.99 32.00 37.37 42.19 | 50.62 54.28 57.77 60.79 63.65 | 68.68 70.80 72.95 74.88 |
| T | °K | 199 218 235 287 367 | 478 606 724 908 983 | 1048 1106 1157 1202 1242 | 1309 1337 1363 1386 1407 |
| h | km | 100 105 110 120 130 | 140 150 170 180 | 220 220 230 240 250 | 260 270 280 290 300 |

1.4. FORMATION OF IONIZED LAYERS

1.4.1. Ion Production

Ions are believed to be produced in the earth's atmosphere partly by cosmic rays but mostly by solar radiation. The latter may include particle radiation (during storm periods), ultraviolet light, and x rays. By far the predominant agent appears to be solar ultraviolet light and soft x rays. With a suitable atmospheric model together with a knowledge of the solar flux, absorption cross section, and ionization efficiency of the various constituents, it is possible to compute the rate of ion production in the atmosphere. Some relevant photoionization data are included in table 1.5 for the major constituents of the E and F regions; i.e., O, O_2 , and O_2 . The ionization efficiency (ion pairs per photon absorbed) is the ratio of the ionization cross section to the absorption cross section. For a more extensive discussion of this subject, the reader is referred elsewhere [0, 5, 6].

1.4.2. Ion Disappearance

When electrons are produced in the upper atmosphere, they tend to reunite with positive ions (recombination) and to attach themselves to neutral molecules to form negative ions such as O_2^- (attachment). The O_2^- ion is later neutralized by further reactions. Electrons can also leave a given volume by moving out of it (diffusion and/or drift).

For our present purposes we shall consider recombination and attachment only. Let the number densities of electrons, of positive ions, and of molecules to which attachment is possible be denoted by N(e), $N(A^+)$, and N(A), respectively. The rate at which electrons are lost by recombining with positive ions is given by

$$\frac{d\;N(e)}{dt} = -\alpha N(e) N(A^+)\,, \tag{1.8}$$

where α is the recombination coefficient. If we assume that there are few negative ions compared with the electron concentration, we have $N(e) \approx N(A^+)$ so that

$$\frac{d N(e)}{dt} = -\alpha \{ N(e) \}^2.$$
 (1.9)

Consider the process of attachment; the rate of disappearance will be proportional to both electron concentration and the neutral atom concentration, that is

$$\frac{dN(e)}{dt} = -bN(e)N(A), \qquad (1.10)$$

where b is a constant of proportionality. If we assume that the number of neutral molecules is enormously greater than the number of electrons, so that it does not change appreciably when a few of the atoms are converted into negative ions, we may write

$$\frac{d}{dt}N(e) = -\beta N(e), \qquad (1.11)$$

where β is known as the attachment coefficient. For a fuller discussion of this subject, the reader is referred to other works on the subject [6]. The coefficients α and β may vary with height because the reactions usually involve three bodies rather than two.

The rate of change of electron density N is, therefore, given by the following continuity equations for the cases of recombination and attachment, respectively:

$$\frac{dN}{dt} = q - \alpha N^2, \tag{1.12}$$

$$\frac{dN}{dt} = q - \beta N,\tag{1.13}$$

where q is the rate of electron production, i.e., number of electrons produced per second.

It should be noted here that if electrons are produced at a rate q and are lost by attachment to neutral atoms to form negative ions, and if these ions are subsequently lost by ionic recombination, it can be shown that the continuity equation assumes the form

$$\frac{dN}{dt} = q_{\rm eff} - \alpha_{\rm eff} N^2, \tag{1.14}$$

where $q_{\rm eff}$ and $\alpha_{\rm eff}$ are effective rates of production and disappearance [6]. Thus the net effect is to make the process appear as simple recom-

Table 1.5. Photoionization data (After Norton, VanZandt, and Denison [4]).

| ź | | Ā | 1206 | 1030-1000 | 1026 | 1000-000 | 063-660 | 977 | 973 | 950 | 937–912 | 912-900 | 900-840 | 885-865 | 835-833 | 200-788 | 780-770 | 704-702 | 630-625 | 019 | 584 | 554 | 553-501 | 200 | 465 | 368 | 360 | 325 $323-310$ |
|--|---|---|------|---------------|---------|----------|---------|------|------|---------|---------|--------------|--------------|--------------|----------|---------|---------|---------|-----------|------|------|------|------------|--------|--------|-------|-------------------|----------------|
| y. | ηN2 | | 00 | - | 0 | 0 | | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.48 | 0.52 | 06.0 | 1.0 | 1.0 | 0.92 | 98.0 | 0.88 | 0.88 | 0.85 | 1.0 | 1.0 | 0.0 |
| Ionization efficiency | η _{Ο2} (ion pairs/photon) | | 9 | 0.0 | 0.58 | 0.75 | 9 | 0.74 | 0.53 | 0.89 | 0.78 | 0.70 | 0.75 | 0.70 | 0.35 | 0.43 | 0.48 | 0.77 | 0.91 | 0.95 | 0.82 | 0.82 | 06.0 | 06.0 | 0.89 | 1.0 | 1.0 | 0.0 |
| Iol | υh | | 0 | > (| 00 | > < | | · c | 0 | 0 | 0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | $\frac{1.0}{1.0}$ | 0.0 |
| +18 | GN ₂ | | 0 | 0.I | 0.002 | 1.03 | 0.0 | 0.0 | 300 | 8.0 | 0.9 | 4.0 | 5.0 | 2.0 | 2.1 | 15 | 25 | 19 | 18 | 15 | 19. | 25 | 16 | 14 | 15.5 | 13 | 12 | 10 8.5 |
| Absorption cross Section X10 ⁺¹⁸ | σ_{O_2} (cm ²) | | 15 | I.3 | 1.9 | 1.9 | 0.00 |) m | : 04 | 5.6 | 0.6 | 7.5 | 7.0 | 8.5 | 10 | 23 | 17 | 25 | 25 | 23 | 22 | 30 | 28 | 28 | 25 | 17 | 17 | 17 |
| cro | ô | | 0 | - | 0 | - | > < | > C | · c | 0 | 0 | 2.6 | 2.8 | 2.9 | 3.2 | 3.3 | 3.4 | 8.1 | 12 | 12.5 | 13 | 13 | 13 | 13 | 13 | 10.3 | 8.6 | ထ ထ ထ က |
| Solar flux | Identification | | Si m | | H 1 Lyβ | 1 | | | | H I Lvô | H I Lve | H I Ly cont. | H I Ly cont. | H I Ly cont. | 0 п, 0 ш | 0 IV | Ne vIII | 0 111 | 0 v, Mg x | , i | He I | 0 IV | Не 1, 0 пп | Si xii | Ne vII | Mg 1x | Fe xvi | Fe xvi |
| So | $ ho \times 10^{-8}$ (ph/cm ² sec) | | 53 | 9 | 25 | 7 06 | 07 66 | 37 | . 4 | | 10 | 30 | 32 | 18 | 5.7 | 3.0 | 3.7 | 2.8 | 6 | 4.4 | 10 | 3.2 | - | 2.9 | 1.9 | 4.1 | က | 23.1 |
| Ź | , | Ā | 1206 | 1030-1000 | 1026 | 1000 | 003-000 | 077 | 973 | 950 | 937-912 | 912-900 | 900-840 | 885-865 | 835-833 | 790–788 | 780-770 | 704-702 | 630-625 | 019 | 581 | 554 | 553-501 | 200 | 465 | 368 | 360 | 335 323–310 |

| 304 285-282 289-260 259-228 228-200 200-166 166-130 105-90 90-75 75-60 60-52 |
|--|
| 0.0000041800001 |
| 0.0002302418875591 |
| 0.0000000000000000000000000000000000000 |
| 5.0 7.0 10.0 115.0 115.5 5.5 2.1 1.0 0.51 0.34 |
| 117 116 118 119 110 110 110 110 110 110 110 110 110 |
| 00.000 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |
| He π Lyα Fe xv He π Ly cont. Ly cont. |
| 26 15 15 20 30 20 20 44 77 1.7 |
| 304 285-282 280-260 229-228 228-200 200-166 166-130 105-90 90-75 75-60 60-52 |

bination. The effective recombination coefficient α_{eff} becomes relatively large in the lower (D and E) regions of the atmosphere.

Another set of reactions which is thought to be of importance in the upper atmosphere is electron disappearance first by atom-ion exchange between a neutral molecule (XY) and the positive ion (A^+) , followed by recombination between an electron and the XA^+ ion:

Production
$$A+\text{photon} \rightarrow A^+ + e$$
, (a)
$$\begin{cases} A^+ + XY \rightarrow XA^+ + Y, & \text{(b)} \\ XY^+ + e \rightarrow X' + A'. & \text{(c)} \end{cases}$$

The primes indicate that the atoms X and A may be left in excited states.

With these reactions it can be shown [6] that, if the number density of XY is high in the F region and low in the E and D regions (as is thought to be the case if A represents atomic oxygen and XY molecular oxygen), the continuity equation takes the form

$$\frac{dN}{dt} = q - \beta_{\text{eff}} N, \tag{1.16}$$

where β_{eff} is an effective attachment coefficient.

We now see that the forms of the continuity equation may not be those expected from simple recombination and attachment.

1.4.3. Formation of a Chapman Layer

The simplest type of ionized layer that can be deduced from theoretical considerations is known as a Chapman Layer [7]. The derivation² is based on the following assumptions:

- (1) An atmosphere with only one type of gas.
- (2) Plane stratification.
- (3) A parallel beam of monochromatic ionizing radiation from the sun.
- (4) An isothermal atmosphere.

To start with, let us invoke assumptions (1), (2), and (3) only. Let the ionizing radiation of intensity S_{∞} be incident, at a zenith angle

² Due to Dr. T. E. Van Zandt.

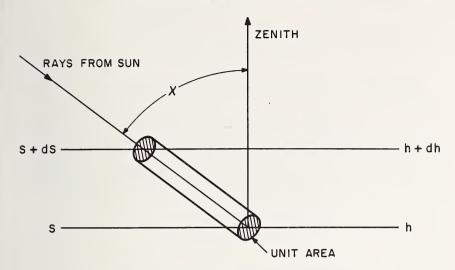


FIGURE 1.2. Absorption of radiation in a slab of gas.

 χ , on the top of the atmosphere. As the radiation is absorbed, as it penetrates into the atmosphere, its intensity diminishes. Let S be the energy flux at a height h and S+dS the flux at a height h+dh as sketched in figure 1.2. Let σ be the absorption cross section of the atoms of the gas and N their number density. The energy absorbed dS in a cylinder of unit cross section and axis parallel to the direction of the incident beam is given by

$$dS = S\sigma N dh \sec \chi. \tag{1.17}$$

Note that (1.17) merely states that the energy absorbed is proportional to the total cross section and to the intensity of the incident radiation. Upon integration we obtain

$$\int \frac{dS}{S} = \sec \chi \int N\sigma \, dh = -\tau \sec \chi, \tag{1.18}$$

where

$$\tau = -\int N\sigma \ dh \tag{1.19}$$

is the optical depth of the atmosphere down to the height h. The minus sign arises because τ increases in the opposite direction to h.

At great heights, $S \rightarrow S_{\infty}$ as $\tau \rightarrow 0$ and (1.18) gives

$$S = S_{\infty} \exp(-\tau \sec \chi). \tag{1.20}$$

The energy absorbed per unit volume is given by

$$\frac{dS}{dh \sec \chi} = N\sigma S = N\sigma S_{\infty} \exp(-\tau \sec \chi). \tag{1.21}$$

Let η be the number of ion pairs produced per unit quantity of energy absorbed, i.e., the ionization efficiency. The number of ion pairs produced per unit volume per second is

$$q(\chi, h) = N\sigma S_{\infty} \eta \exp(-\tau \sec \chi). \tag{1.22}$$

Now τ is a function of χ and h. Using (1.1), (1.2), and (1.3), we obtain

$$\tau = \sigma \int N dh = \frac{\sigma}{mg} \int dp = \frac{\sigma p}{mg} = \frac{\sigma N k \tau}{mg} = \sigma N H. \tag{1.23}$$

Substitution of (1.23) into (1.22) yields

$$q(\chi, h) = \frac{\tau S_{\infty}}{H_{\epsilon}} \eta \exp (1 - \tau \sec \chi), \qquad (1.24)$$

where $\epsilon = 2.718 \cdots$. Note that we have neglected the variation of g with height.

Notice that (1.24) holds for any temperature distribution. To obtain Chapman's formula we invoke assumption (4), an isothermal atmosphere, where H is independent of height.

We can define a quantity z by the relation

$$z = -\ln \tau,$$
 (a)
 $\tau = \exp(-z).$ (b)

i.e.,

Substitution of (1.25b) into (1.24) gives

$$q(\chi, z) = \frac{S_{\infty} \eta}{\epsilon H} \exp \left\{ 1 - z - \sec \chi \exp \left(-z \right) \right\}$$
 (a)

$$= q_0 \exp \{1 - z - \sec \chi \exp (-z)\},$$
 (b)

where

$$q_0 = \frac{S_{\infty} \eta}{\epsilon H} \tag{1.27}$$

is the rate of production of ion pairs at the level z=0 when the sun is overhead, i.e., when $\tau_0=1$, and where τ_0 is the value of τ at the level z=0. From (1.23), (1.25b), and (1.4a) we get

$$\exp (-z) = \frac{\tau}{\tau_0} = \frac{p}{p_0} = \exp \left(-\frac{h - h_0}{H}\right),$$

i.e.,

or

$$z = \frac{h - h_0}{H} \,. \tag{1.28}$$

The reference height h_0 is, therefore, the height of maximum ion production when the sun is overhead.

If, in (1.26b), we replace z by $z-\ln\sec \chi$ and put $\chi=0$, we obtain

$$q(z_0, z-\ln\sec\chi) = \sec\chi \ q(\chi, z). \tag{1.29}$$

Equation (1.29) gives us an important scaling rule. That is, the curve $q(\chi, z)$ has the same shape as q(0, z), but is moved upwards by $\log \chi$ and is diminished by $\cos \chi$. The height of the peak of ion production z_m or h_m is given by

$$z_m = \ln \sec \chi,$$
 (a)
$$h_m = h_0 + H \ln \sec \chi.$$
 (b)

The variation of $q(\chi)$ for various values of z is shown in figure 1.3. It can be seen that the use of a logarithmic scale for q makes the shapes of the q curves identical. The peak rate of production is given by

$$q_m = q_0 \cos \chi. \tag{1.31}$$

The intensity of the ion production is determined by the flux of ionizing radiation and the efficiency η . Changing the flux does not alter the height

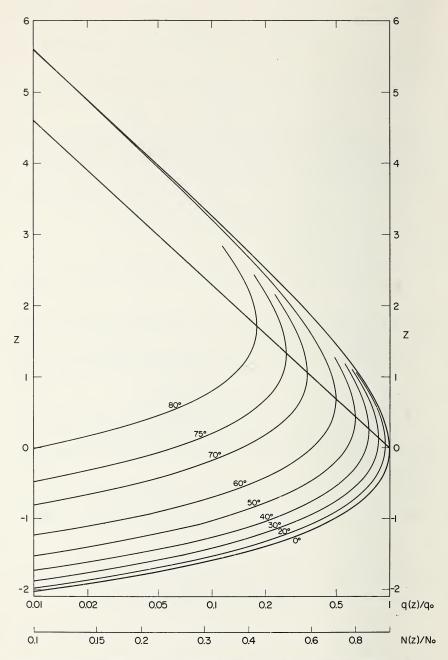


Figure 1.3. Normalized rate of photoionization $q(z)/q_0$ and electron density $N(z)/N_0$ according to Chapman theory.

(After T. E. VanZandt and R. W. Knecht, 1964, Ch. 6, Space Physics, John Wiley & Sons.)

of maximum production. Thus, if there are several wavelengths present in the incident radiation for which the ionization coefficients are markedly different, several distinct layers will result. The most strongly absorbed radiation produces the uppermost layer and vice versa. Likewise, different ionized layers would result with different gases in the atmosphere.

1.4.4. Electron Density Distribution

To determine the electron density distribution, we must assume some process of electron disappearance. Under certain circumstances the left-hand sides of (1.12) and (1.13) are small (quasi-equilibrium conditions). If, therefore, the loss of ions is due to a recombinationlike process, then $q = \alpha N^2$ and

$$N = N_0 \exp \frac{1}{2} \{ 1 - z - \sec \chi \exp (-z) \}, \tag{1.32}$$

where α is independent of height and

$$N_0^2 = \frac{q_0}{\alpha} \,. \tag{1.33}$$

The peak density

$$N_{\text{max}} = \frac{q_0 \cos \chi}{\alpha} \tag{1.34}$$

and the height of the peak is given by (1.30).

When the loss process is "attachmentlike," which is independent of height, we have

$$q = \beta N, \tag{1.35}$$

which gives

$$N = N' \exp \{1 - z - \sec \chi \exp (-z)\},$$
 (1.36)

where

$$N' = \frac{q_0}{\beta} \,. \tag{1.37}$$

This gives

$$N_{\text{max}} = \frac{q_0}{\beta} \cos \chi. \tag{1.38}$$

If we assume that β depends directly on the molecular density,

$$q = \beta_0 N \exp(-z), \tag{1.39}$$

where β_0 is the value of β at the level h_0 . This gives, for the electron density distribution,

$$N = N_0 \exp \{1 - \sec \chi \exp (-z)\}. \tag{1.40}$$

This type of ion distribution has no maximum for the steady state except at very great heights where saturation occurs because all the molecules are ionized. Hence we see that with recombination the maximum electron density varies as $\cos^{\frac{1}{2}}\chi$ whereas with attachment it varies as $\cos\chi$. It is of interest to note that the maximum densities in the E and F_1 layers tend to follow the $\cos^{\frac{1}{2}}\chi$ law, as will be seen later.

It is of interest to examine the dependence on height of the solar control of a Chapman layer. Low down in the layer, below the peak, z is negative and so the term $\sec\chi\exp(-z)$ is relatively large so that there will be a marked solar control of the diurnal variation. This is illustrated in figure 1.4 by the z=-4 curve. On the other hand, high up in the layer

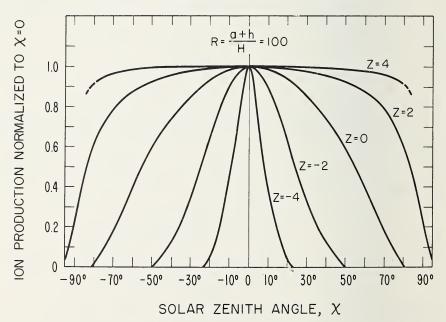


FIGURE 1.4. Ion production as a function of solar zenith angle.

(After T. E. VanZandt and R. W. Knecht. See fig. 1.3.)

where z is positive and large, the sec $\chi \exp{(-z)}$ term is small and so the production increases rapidly near sunrise and remains almost constant until sunset, when it drops rapidly (fig. 1.4, curve z=4). This is the type of diurnal variation to be expected when electron production is due to photodetachment of electrons from negative ions by visible light.

Although the theory given above is useful for purposes of discussion, it should be borne in mind that, in practice, almost all the basic assumptions need qualification. Thus the earth's atmosphere consists of several species of gases, and the incoming radiation has a broad spectrum. The assumption of an isothermal atmosphere is certainly invalid.

 $\cos \chi$ can be found for any location on the earth from the following equation:

$$\cos \chi = \sin \phi \sin \delta + \cos \phi \cos \delta \cos h, \tag{1.41}$$

where ϕ is the geographic latitude, δ is the solar declination, and h is the local hour angle of the sun measured westwards from apparent noon (mean noon corrected for the equation of time and the standard time used at the location). Tables of hourly values of $\cos \chi$ from sunrise to sunset for the fifteenth day of each month for most of the ionospheric vertical incidence sounding stations are given in the URSI Ionosphere Station Manual [8].

Near grazing incidence (χ greater than about 80°), the assumption of plane stratification breaks down, and it is necessary to replace $\sec \chi$ by the Chapman function of $Ch(R+z,\chi)$, where R=(a+h)/H. Tables of $Ch(R+z,\chi)$ have been published by Wilkes [9].

Finally, it should be realized that the recombination coefficient (effective) is not independent of height. In view of all the above qualifications, it is remarkable that the E and F_1 layers behave approximately as predicted.

1.5. THE EARTH'S MAGNETIC FIELD3

1.5.1. The Dipole Field

To a first approximation, the earth's magnetic field is that of a sphere uniformly magnetized in the direction of the centered dipole axis. The centered dipole axis cuts the surface of the earth at two points A and B known as the south and north dipole poles, as shown in figure 1.5. The

Based on a lecture by Dr. S. Chapman.

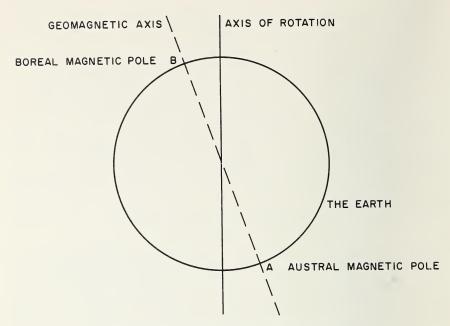


FIGURE 1.5. Earth's dipole magnetic poles.

A-austral pole; B-boreal pole.

best fit between the earth-centered dipole and the actual magnetic field is obtained by taking A at 78.3°S, 111°E and B at 78.3°N, 69°W. It will be seen that the axis of the dipole does not coincide with the axis of rotation. The plane through the center of the earth O perpendicular to BA is called the dipole equatorial plane, and the circle in which it cuts the sphere is called the dipole equator. Dipole latitude Φ is reckoned relative to this equator. The semicircles joining B and A are called the dipole meridians; the one passing through the dipole and south geographic pole is chosen as the zero of dipole longitude Λ . The relationships between the dipole coordinates (Φ the latitude and Λ the longitude) and the corresponding geographic coordinates (Φ , Λ) at a point P are given by

$$\sin \Phi = \sin \phi \sin \phi_0 + \cos \phi \cos \phi_0 \cos (\lambda - \lambda_0) \tag{1.42}$$

$$\sin \Lambda = \frac{\cos \phi \sin (\lambda - \lambda_0)}{\cos \Phi} . \tag{1.43}$$

where ϕ_0 and λ_0 are the geographical latitude and longitude of the north

dipole pole ($\phi_0 = 78.3$ °N, $\lambda_0 = 291.0$ °E). The magnetic potential V of the dipole, of moment M at any point P whose position vector relative to O is \mathbf{r} , is given by

$$V = \frac{\mathbf{M} \cdot \mathbf{r}}{r^3} = -\frac{M \sin \Phi}{r^2} \,, \tag{1.44}$$

where Φ denotes the dipole latitude. This is also the potential of the external field of the uniformly magnetized sphere.

The radial (vertical) component Z of the field, reckoned positive when inward, is given by

$$Z = \frac{\partial V}{\partial r} = \frac{2M\sin\Phi}{r^3} \,. \tag{1.45}$$

The horizontal (tangential) component H at P lies in the meridian through P and is directed towards B. It is given by

$$H = \frac{\partial V}{r \partial \Phi} = \frac{M \cos \Phi}{r^3} \,. \tag{1.46}$$

The magnetic dip or inclination I is given by

$$\tan I = \frac{Z}{H} = 2 \tan \Phi. \tag{1.47}$$

Because this is independent of r, the dip is the same at all points along any radius OP. Note that I is positive when the field direction is below the horizontal. Also,

$$F^2 = H^2 + Z^2. (1.48)$$

At the pole B, F=Z, and at the equator, F=H. Let H_0 denote the equatorial value of H at the surface of the sphere (r=a). Then we have the following relationships:

$$H = H_0 \left(\frac{a}{r}\right)^3 \cos \Phi, \tag{a}$$

$$Z = 2H_0 \left(\frac{a}{r}\right)^3 \sin \Phi, \tag{b}$$

$$F = H_0 \left(\frac{a}{r}\right)^3 \{1 + 3 \sin^2 \Phi\}^{\frac{1}{2}}.$$
 (c)

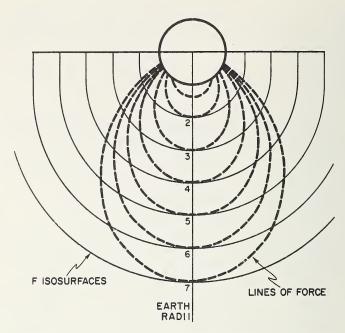


Figure 1.6. Lines of force and of equal intensity of a uniformly magnetized sphere.

(After S. Chapman, 1964, Geophysics—The Earth's Environment, Part III, Solar Plasma, Geomagnetism and Aurora, Gordon and Breach, N.Y.)

It will be seen, from (1.49), that the magnetic intensity at the poles is twice that at the same radial distance (height) at the equator.

The lines of force of the dipole field are given by $dr/Z = rd\Phi/H$; hence their equation is

$$r = ka \cos^2 \Phi. \tag{1.50}$$

Here k is the equatorial radius measured in earth radii. The product ka is the distance at which the line of force crosses the equatorial plane. The points where it meets the sphere are given by $\Phi = \Phi_0$ and $\Phi = -\Phi_0$ where $\cos \Phi_0 = k^{-\frac{1}{2}}$.

The lines of force, together with the isosurfaces of F (on which F is constant), are given by

$$r = k'a(1+3\sin^2\Phi)^{\frac{1}{6}},$$
 (1.51)

and are shown in figure 1.6. The parameter k' of the F isosurface is thus

related to the value of F for the surface:

$$k' = (H_0/F)^{\frac{1}{3}}. (1.52)$$

It is interesting to note that the strength of the magnetic field decreases as the cube of the distance from the earth's center. Thus at one earth radius above the surface, the field is only 0.125 of that at the surface. Thus it may be important to consider the variation of field strength when large distances are involved (e.g., earth-space propagation).

1.5.2. The Real Field

The magnetic intensity F at any point P on the earth's surface can be specified by its downward vertical component Z and its vector horizontal component E, or by E and the angle E by which E dips below the horizontal. On the earth, the direction of E is specified by the angle E between E and the geographic north; E is called the magnetic (or compass) declination and is reckoned positive if eastward. The northward and eastward components of E are denoted by E, E, respectively, and

$$\tan D = \frac{Y}{X}$$
, $X = H \cos D$, $Y = H \sin D$, $H^2 = X^2 + Y^2$. (1.53)

The seven quantities F, Z, H, I, D, X, and Y are called the magnetic elements, and any set of three independent elements serves to specify F; i.e.,

$$F, I, D; H, I, D; H, Z, D; X, Y, Z.$$
 (1.54)

The elements F, H, Z, and I are called *intrinsic* because their only reference to direction is to the natural direction characteristics of P, namely, the vertical. The other three elements, D, X, Y, are called *relative* because they are defined relative to the geographical (or rotational) axis NS, which has no necessary relation to the geomagnetic field.

In geomagnetism, field intensity is measured in gauss units Γ , despite the internationally agreed use of the term oersted for intensity and gauss for induction. A smaller unit, the gamma (γ) , is used, especially in connection with the variations in the geomagnetic field where

$$1\gamma = 10^{-5}\Gamma$$
. (1.55)

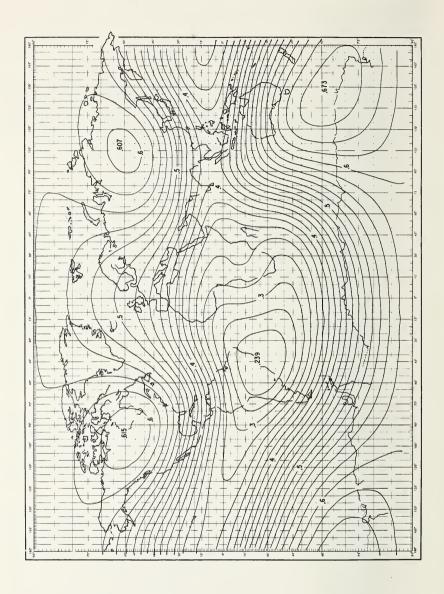


FIGURE 1.7. World map of total magnetic intensity (F). (After J. C. Cain and J. R. Neilon, 1963, J. Geophys. Res. 68, 4689.)

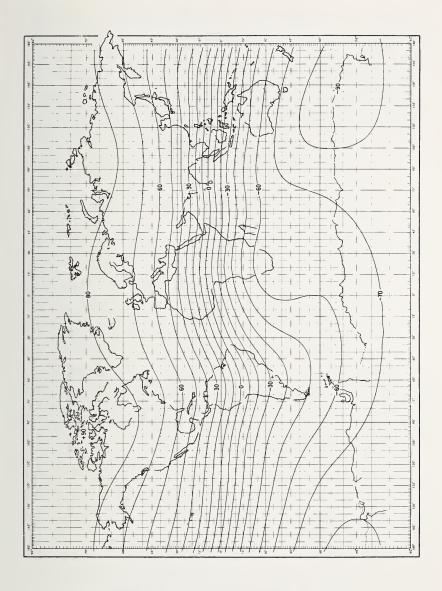


FIGURE 1.8. World map of magnetic dip (1). (After J. C. Cain and J. R. Neilon, 1963, J. Geophys. Res. 68, 4689.)

In practice, the magnetic field of the earth departs somewhat from that of a uniformly magnetized sphere. Maps have been prepared showing the distribution of the various magnetic elements over the earth's surface. The worldwide variation of the total intensity F is shown in figure 1.7 and of the magnetic dip I in figure 1.8. Both of these elements are of importance in ionospheric radio propagation. From the latter figure it will be seen that the magnetic dip poles P_N (north) and P_S (south) are not at opposite ends of a diameter. Their locations are not accurately known because they move around. Approximate positions for 1945 were:

| P_N | 76.0°N; | 102.0°W |
|---------|---------|---------|
| P_{S} | 68.2°S; | 145.4°E |

The antipode of P_S is about 1600 km from P_N , and the line $P_N P_S$ misses the earth center by about 1150 km.

The distribution of the earth's magnetic potential V (from which the vector field can be derived) can be expressed by a mathematical process called spherical harmonic analysis [10]. The potential V can be expressed as a sum of orthogonal functions of the type

$$P_n^m(\cos\theta)(\alpha_n^m\cos m\lambda+b_n^m\sin m\lambda),$$

where θ is the north co-latitude (i.e., angular distance from the north pole) and λ is the east longitude. The functions P_n^m have been tabulated [11]. Using this technique, it has been shown that most of the field originates from within the earth. A small part (less than 0.1 percent) has its origin outside the earth.

1.5.3. Magnetic Variations

Owing to electric currents flowing above the earth's surface, the magnetic field at any point on the surface varies diurnally, seasonally, and with solar activity. The net variation at the earth's surface is due partly to the external currents and partly to induced earth currents. Days on which the transient magnetic variations are "smooth" and regular are called q days, q signifying magnetically quiet. The others, d days, are said to be magnetically disturbed.

On q days the magnetic variations proceed mainly according to local solar time, but they also contain a part, usually small, controlled by the moon. These two parts are called the solar daily and the lunar daily

magnetic variations. They, and the fields of which they are the manifestation, are denoted by S_q and L ($S=\operatorname{solar}, L=\operatorname{lunar}$). Both are caused by currents flowing in the ionosphere, mainly in the E layer. An example of a quiet day magnetogram for a middle latitude station is given in figure 1.9.

The S_q currents are stronger by day than by night, stronger in summer than in winter, and about 50 percent stronger at sunspot maxi-

mum than at sunspot minimum.

Of particular interest, from the point of view of the ionosphere, is the concentration of enhanced currents in a narrow strip along the magnetic equator which is known as the "equatorial electrojet."

During a magnetic disturbance, additional currents circulate in the ionosphere. They are superposed on the S_q and L currents. Unlike the latter, they are strong in high latitudes and are often stronger over the night than over the day hemisphere. They are denoted by DP (D= disturbance, P= polar). They are especially concentrated along the auroral zones (i.e., the region of overhead visible aurora), and hence the currents there are called the auroral electrojet. A strong auroral electrojet may carry a current of the order of a million amperes. The return current flows mainly over the polar cap, but some flows between the north and south auroral zones. The DP currents are believed to be one of the many effects caused by the impact of a solar stream or cloud of ionized gas upon the earth's magnetic field. Some of the gas finds its way into the polar atmosphere and causes the luminescence of the aurora. A magnetogram taken during a magnetic storm is shown in figure 1.10.

Many magnetic storms, particularly the big storms, begin suddenly and almost simultaneously, to within a minute, all over the earth. The sudden commencement is ascribed to the impact of solar ionized gas on the outer part of the geomagnetic field, at a distance of several earth radii.

Though much of the solar gas is turned away from the earth, some is trapped by the field and the trapped particles spiral round the lines of force, between the northern and southern hemispheres; they also drift round the earth under the influence of the magnetic field. The total motion is equivalent to an electric current in the form of a ring around the earth. The net effect at the earth is to decrease the horizontal field, and in many storms the decrease soon overpowers the initial increase.

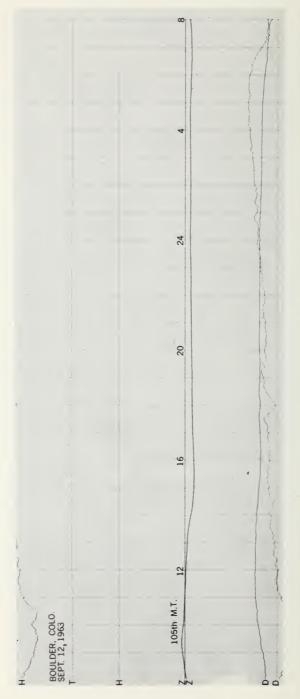


FIGURE 1.9. Sample magnetogram taken on a quiet day.

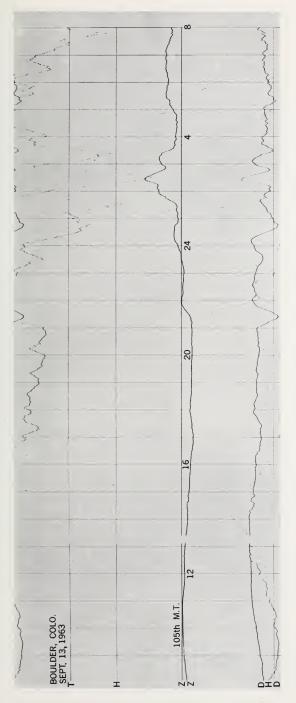


FIGURE 1.10. Sample magnetogram taken during a magnetic storm.

1.5.4. Magnetic Indices

The degree of magnetic disturbance during each Greenwich day is indicated by a variety of indices, according to internationally adopted plans.⁴ Many magnetic observatories throughout the world take part in these plans. They assign *local* indices of magnetic activity. These are sent to an international center at De Bilt, The Netherlands. This is linked with a Permanent Service of Geomagnetic Indices at Göttingen, Germany.⁵ There the local indices are used as the basis for world indices.

Each participating observatory assigns to each Greenwich day its own "daily figure" C. This is one of the numbers 0, 1, or 2, to indicate ascending degrees of disturbance of its records. This local daily index is assigned by simple inspection of the records. Naturally there are many borderline cases where the choice between 0 and 1, or between 1 and 2, is difficult; but the choice is made.

The values of C from all observatories for each day are averaged to one decimal place. This gives C_i , the "international daily character figure." It provides a 21-fold classification of Greenwich days, from 0.0 on days of extreme calm, to 2.0 on days that are magnetically highly disturbed.

By a more detailed and precise method, a local index K is assigned to each three-hourly interval of Greenwich time, 0-3, 3-6, \cdots ; K is one of the integers 0 to 9, giving a tenfold classification of these intervals. The records of the three elements are examined, and for each an estimate is made of the range r during the interval, allowing for the part of the change caused by S_q and L and, when necessary, by SFE (S_q current augmented by solar flare effect) and the recovery phase of the ring current field. Such allowance calls for experience and judgment. The largest of the three ranges is taken as the basis for K; the element concerned may vary from interval to interval, or from one observatory to another.

For each observatory a table is assigned, giving limits of r corresponding to each of the ten values of K. The lower limit of r for K=9 may have any of the values 300, 350, 500, 600, 750, 1000, 1200, 1500, and 2000 γ . The first applies to very-low-latitude observatories (outside the belt of the equatorial electrojet; sec. 1.5.3). The last applies to the most disturbed stations, in the auroral zone. The limit 500 refers to stations in about geomagnetic latitude 50°. The table for this latitude is

⁵ Addresses: C+K Centre, Kon. Ned. Meteor. Inst., De Bilt, The Netherlands; and Geophysikalisches Institut, 180 Herzberger Landstr., (34) Göttingen, Germany.

⁴ The plans are under the auspices and supervision of the Committee on Characterization of Magnetic disturbances of IAGA (International Association of Geomagnetism and Aeronomy), a part of IUGG (International Union of Geodesy and Geophysics); the present Chairman is J. Bartels.

as follows:

For other latitudes, the lower values of the range limits of r are scaled up or down proportionately to the lower limit for K=9.

The C and K figures for some observatories appear currently in their own or other publications. A volume containing the complete set for all participating observatories, together with much other data, including the world indices, is published annually as an issue of IAGA Bulletin 12. These volumes, formerly issued as IATME⁶ Bulletins 12, are now distributed by the North Holland Publishing Co., Amsterdam, from whom information as to the availability of back issues can be obtained⁷.

The values of K for any one observatory show statistically a daily variation, depending on its local time. To obtain a world index this local influence must be eliminated. Corrected or standardized values K_s of K are prepared at the Permanent Service at Göttingen for each of 12 selected observatories, northern and southern, lying between geomagnetic latitudes 48° and 63°. The mean of the 12 values of K_s for these 12 observatories is denoted by K_p , and is called the planetary 3-hr index; it is expressed in a scale of thirds.

$$00, 0+, 1-, 10, 1+, 2-, 20, \dots, 9-, 90.$$

Thus it is a 28-fold classification.

By cooperation between De Bilt and Göttingen, it is possible to issue monthly tables of K_p before the end of the following month. The values are also published in the CRPL F Series, Part B, Solar-Geophysical Data and in the Journal of Geophysical Research. Quarterly Bulletins containing the K_p figures and other magnetic data are issued from De Bilt. A sample table of K_p indices is given in table 1.6.

Along with the values of K_p , values of two daily world indices A_p and C_p are given. These are derived from the eight values of K_p for each day. The values of C_p range like those of C_i , from 0.0 to 2.0 at intervals of 0.1. A table of range limits for the daily sums of K_p has been formed, such that the frequency distributions of C_i and C_p for the 10 years 1940–49

⁶ IATME signifies International Association of Terrestrial Magnetism and Electricity, the former name of IAGA.

⁷ This publication and the work of the two centers for geomagnetic indices, at De Bilt and Göttingen, are sponsored by ICSU (International Council of Scientific Unions) with financial support from UNESCO.

Table 1.6. Geomagnetic activity indices (June 1963)

| June C 1963 | | Values $K_{\mathcal{P}}$ | | | | | | Sum | A_{p} | Final selected days |
|---------------|--|--------------------------|--|------|----------|---------------|-----------|-------------|-------------|---------------------------|
| | | Three-hour Gr. interval | | | | | | | | |
| | | 1 2 | 3 4 | 5 | 6 | 7 | 8 | | | |
| $\frac{1}{2}$ | $\begin{bmatrix} 0.6 \\ 0.7 \end{bmatrix}$ | 2 + 2 + 2 + 20 30 | 20 3+ 2+ 2+ | | | 1+ 2+ | | 20o 19 – | 11 10 | Five |
| 3 | 0.4 | 2 - 2 - | 2o 2o | 2+ | 1- | 2 – | 2- | 14- | 6 | quiet |
| 4 5 | $\begin{bmatrix} 0.2 \\ 0.0 \end{bmatrix}$ | lo lo 0+ lo | 3 - 1 - 00 0 + | | | $\frac{1}{0}$ | | 9 – 3 + | 5 2 | 5 |
| 6 7 | 1.1 | | 0 + 10 | | | 5- | | 160 | 16 | 16 22 |
| 8 | 0.8 | 2o 2o | 5 - 3 - 3 o | 2 — | 3 — | 3 — | 4+ | 35+ 20+ | 43 12 | 23 |
| 9 10 | $\begin{array}{c} 0.6 \\ 0.4 \end{array}$ | | 2+ 3- lo 2- | | | 1+ 20 | | 18+ 11o | 10 5 | |
| 11 | 0.4 | | 1+ 10 | | | 1+ | | 13 - | 6 | Five |
| 12 13 | $\begin{array}{c c} 0.1 \\ 0.3 \\ 0.3 \end{array}$ | | lo 2- | - 1+ | lo | 1+ | 2 — | 10 - | 5 5 5 | disturbed |
| 14 15 | $\begin{array}{c} 0.2 \\ 0.6 \end{array}$ | 3 - 00 $2 - 3 +$ | $\frac{10}{3+1}$ | | | $\frac{0}{2}$ | | 11o 16o | 9 | 7 18 |
| 16 | 0.1 | | 00 0- | | | 1+ | | 50 | 2 | 25 26 |
| 17 18 | 0.8 | lo 3+ | $\frac{2+20}{3-30}$ | 4+ | 30 | 50 | 4o | 18+ 26+ | 9 21 | 27 |
| 19 20 | 0.7 | | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | 2+ 20 | | 3 - 2 - | 18+ 21o | 10 13 | |
| 21 | 0.4 | | 3 - 30 | | | 1+ | | 14+ | 8 | Ten |
| 22 23 | $\begin{array}{c} 0.1 \\ 0.1 \end{array}$ | lo 1- | · 1+ lo · 1- 1- | + 0+ | · lo | | lo | 9+ 70 | 4 | quiet |
| 24 25 | $\begin{array}{ c c }\hline 0.3\\ 1.1\end{array}$ | | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | | | | 13 — 28o | 6 23 | 4 5 |
| 26 | 1.3 | 6- 5- | 5o 3- | + 2+ | 20 | 2+ | 3- | 28o | 26 | 10 11 |
| 27 28 | 0.9 | | 3 + 30 $3 + 30$ | 2+3- | 1-3+ | 4 – 30 | 30 1+ | 24 - 210 | 16 13 | 12 13 |
| 29 30 | 0.6 | 1+ lo | 2 + 10 | 2o | 3+ | 3+ | 2+ | 17- | 9 | 14 |
| 30 | 0.8 | 2+3- | - 3 - 2 - | T 41 | - 20 | 4- | 2+ | 20+ | 11 | 16 22 23 |
| Mean | n: 0.59 | | | | | | | Mean | : 11 | |

are nearly identical. The indices of C_i and C_p are approximately logarithmically related to the ranges r of the magnetic elements during the disturbance (corrected for S and L). The indices A_p are more nearly linearly related to these ranges.

The planetary index K_p is designed to measure solar particle radiation by its magnetic effects, specifically to meet the needs of research workers in the ionospheric field.

The K tables for the individual observatories, in the IAGA Bulletins 12, give a very detailed indication of the incidence, in time and place,

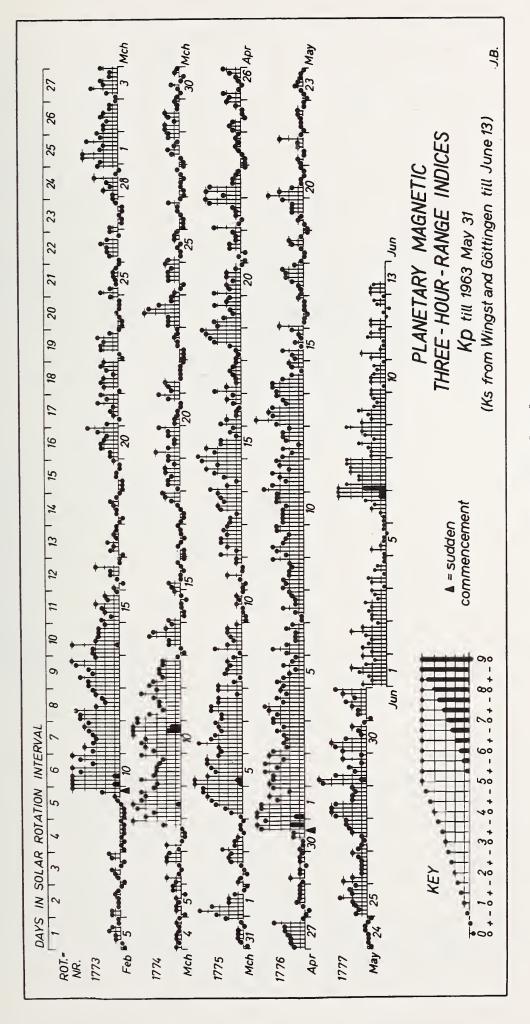


FIGURE 1.11. Bartels musical scales.



Figure 1.12. Location of the northern zone of maximum frequency of occurrence of overhead aurora on magnetically quiet and on magnetically disturbed days.

(After Y. I. Feldstein, Investigations of the Aurora, Moscow, 1960.)

of the magnetic effects of the solar eruptions. The K_p , C_p , A_p , and C_i tables give a concise indication of the overall world effects [11]. These tables are now available from the time of the Second International Polar Year (1932/3) to date. The tables of C_i go back still further. Details regarding these publications are given in Bulletin 12(1) (pp. iv and 268); see also IGY Annals, vol. 4, pp. 227–236, where also, on pp. 220–226, an account is given of the quarter-hourly indices Q to be issued, covering the period of the IGY. These will permit studies of correlations between magnetic disturbance and other phenomena in much more time detail than is possible with the daily and three-hourly indices.

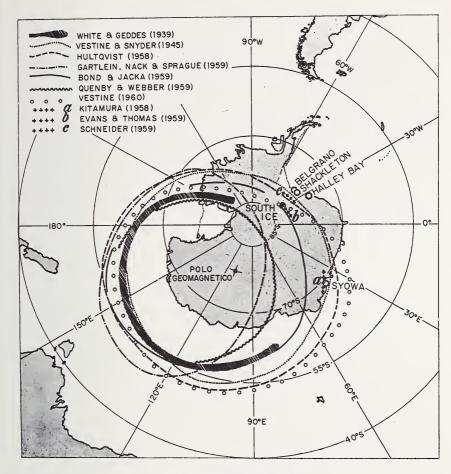


FIGURE 1.13. South auroral zone.

(After O. Schneider, 1961, Instituto Antarctico Argentino 55, Buenos Aires.)

Finally, note in this connection the publication of diagrams (Bartels' "musical scales") graphically illustrating the sequence of the K_p values, figure 1.11. These are arranged in rows so as to show the 27-day recurrence tendency of magnetic disturbance, arising from the solar rotation. The diagrams are issued monthly along with the K_p tables, in time to be helpful in making 27-day recurrence forecasts.

The monthly diagrams issued during the IGY have been combined into a diagram for the whole IGY period, and since then annual diagrams have been issued (see Bulletins 12 for further information).

1.6. THE AURORAL ZONES

These regions of the earth where visible aurora occurs overhead are of particular importance to the radio communicator because of the frequent occurrence there of ionospheric disturbance, as will be discussed in a later chapter.

As was mentioned in section 1.5.3 above, aurora is thought to be the result of the entry into the atmosphere of charged corpuscles. Owing to the interaction between the moving charges and the geomagnetic field, the corpuscles are deflected north and south of the equatorial plane and are deposited in a relatively narrow ring situated between dipole latitudes of about 64° and about 70°. Maps showing lines of constant frequency of occurrence (called isochasms) have been prepared for the northern and southern auroral zones and are shown in figures 1.12 and 1.13. The north auroral isochasms are not quite circular, but are elongated along the Siberia-North American axis. The geographical areas enclosed by the auroral rings are often called "polar caps."

It should be borne in mind that the auroral zone is not fixed but moves with varying magnetic activity. Thus during strong magnetic storms the auroral zones, both north and south, move towards the equator. For example, a great aurora on September 25, 1909, was observed in Singapore, latitude 1°N. Even during magnetic storms of moderate strength there is a close connection between the position of the aurora and the strength of the magnetic disturbance.

In addition to the visible aurora, radio techniques have revealed the existence of enhanced ionization in the ionosphere in these latitudes [12]. This enhanced ionization is manifested as sporadic E (sec. 6.3.4), D-region absorption (sec. 6.3.3), and radio aurora (sec. 8.6.1). However, it may not necessarily follow that the various auroral zones coincide.

1.7. THE SUN

1.7.1. Quiet Conditions

1.7.1.1. Structure

For our present purposes it will be sufficient to consider the sun as made up of four parts:

- (1) the interior;
- (2) the photosphere, or visible surface;
- (3) the chromosphere, the bright region above the photosphere, seen during total solar eclipses; and
 - (4) the corona, the outer atmosphere of the sun.

Although the various sections merge into one another, the radiation from the photosphere comes entirely from a layer about 400 km thick compared to a solar radius of about 700,000 km so that the concept of a solar surface has a fairly well-defined meaning. Approximate values of the heights and temperatures of the various regions are given in table 1.7. For further information the reader should consult "The Sun" [13].

The sun is composed chiefly of the elements hydrogen and helium together with smaller amounts of the heavier elements, notably calcium.

Table 1.7. Approximate heights and temperatures of the sun's outer layers

| Solar layer | h (km) | T °K | | |
|---|--|--|--|--|
| Outer corona Middle corona Inner corona Upper chromosphere Lower chromosphere Photosphere | 1,400,000 700,000 21,000 to 140,000 7,000 to 14,000 1000 — | 1,500,000 1,500,000 1,000,000 25,000 to 300,000 5300 6000 effective | | |

1.7.1.2. Ionizing Radiations

To a first approximation, the quiet sun radiates as a blackbody at a temperature around 6000° Kelvin. Superimposed on the blackbody continuum are certain lines characteristic of the elements in the sun. Some of the more important lines are hydrogen α (6563 Å), Lyman α (1216 Å), and helium I (584 Å). These radiations are responsible for the ionization of the upper atmosphere discussed in section 1.4. A number of lines in the ultraviolet part of the solar spectrum are given in table 1.5. For example, it is thought that Lyman α radiation is the major source of ionization in the quiet D region. The quiet E region is believed to be produced by x rays (10–100 Å), Lyman β (1025.7 Å), C III (977 Å), and the Lyman continuum (910 to 980 Å) [14]. The primary source of ionization in the F region appears to be the Lyman continuum and the band 350 to 200 Å (which includes the He III 304 Å resonance line).

The amount of visible light from the sun changes very little from one day to the next. On the other hand, the day to day variability of the quiet ionosphere suggests that the solar emissions in the ultraviolet and x-ray regions vary appreciably.

In addition to the wave radiations, the quiet sun emits a stream of charged corpuscles (mostly electrons and protons) which is called the "solar wind."

1.7.1.3. Radio Emissions

The sun is a source of radiation on radio frequencies. These emissions are caused by plasma oscillations (see sec. 2.3.1.1) and gyro-oscillations



FIGURE 1.14a. Photograph of the sun at sunspot minimum (1954).

(see sec. 2.3.1.2) in the solar atmosphere, as well as "noise" originating in random collisions of the electrons [15]. The noise from the quiet sun is of the last type.

The flux of solar radio noise at the earth's surface is monitored at a number of observatories, and the data are available in the CRPL F Series Part B [16] and in Quarterly Bulletin on Solar Activity of the International Astronomical Union [17]. There are several methods of recording, such as fixed frequency, sweep frequency, total flux, interferometers for exploring the distribution of radio sources on the solar disk, etc. A list of observing stations, the frequencies (or frequency bands) of observation, and the universal times of recording are listed in the Bulletin [17]. The unit of measurement of flux is 10^{-22} watts per square



FIGURE 1.14b. Photograph of the sun at sunspot maximum (1958).

meter per cycle per second. In general, the flux increases with frequency in the range 100 Mc/s to 10,000 Mc/s, but the day to day variability is much greater on the lower frequencies as can be seen on pages 464-6 of the Bulletin [17].

1.7.2. The Active Sun

1.7.2.1. Sunspots

One of the most notable phenomena on the sun's surface is the appearance, and disappearance, of certain dark areas known as sunspots. The life of a sunspot is highly variable; some spots last only a few days, whereas a few may survive four or five solar rotations (of about 27 days each). Their exact nature is not known, but they appear to be vortices in the matter comprising the photosphere. Sunspots appear dark because the surface temperature is only about 3000 °K, compared with the 6000 °K of the quiet photosphere. Sunspots tend to group together. A group may contain a few isolated spots or dozens of spots.

One of the more interesting features of sunspots is their unusually strong magnetic fields. These may approach 0.4 Wb/m² (weber per square meter) (4000 G) for the larger spots.

1.7.2.2. The Sunspot Cycle

The appearance of the sun in 1954 and in 1958 can be seen in figures 1.14a and 1.14b. Clearly, there is a variation in the sunspot "activity." To measure this activity an index is required. The most common index of sunspot activity is the Wolf number R given by

$$R = k(10g + s),$$
 (1.56)

where g is the number of groups and s is the number of observable individual spots. The factor k is a correction factor to take into account the equipmental and observer characteristics. It will be seen that this number is weighted heavily in favor of groups, so that its value as an index of sunspot activity is questionable. Nevertheless, it is valuable because of its availability for a period of about 200 yr. It thus provides a large homogeneous sample of data. Sunspot numbers are available on a daily basis and as monthly and yearly averages.

When the yearly sunspot numbers are plotted, for a long period of time, such as is shown in figure 1.15, it is clear that the sunspot activity has a periodicity of about 11 yr. The duration of an individual cycle may vary over much wider limits; thus the periods between minima range from about 8.5 yr to about 14 yr and those between maxima range from 7.3 yr to about 17 yr. Furthermore, the annual minima of R lie in the range 0 to 10, whereas the maxima range from about 50 to about 190. The daily values of R vary between 0 and 355 or more.

In addition to the 11-yr period, there are periods, particularly near the 11-yr minima, when a 27-day (approximate) recurrence is evident. This period corresponds to a solar rotation.

Many attempts have been made to represent, analytically, the existing sunspot data with a view to the prediction of future cycles. The predictions have never been particularly successful.

In addition to the relatively dark sunspots, bright areas often appear on the solar disk. These areas, called plages, are observed in the light of calcium K and are intimately associated with sunspots. Plages are comparatively long-lived active regions; they precede in appearance the spots, which develop in them, and persist after the spots have disappeared.

1.7.2.3. Flares

A solar flare is a burst of "light" occurring in the chromosphere near a sunspot. It is most easily observed in the $H\alpha$ light (6563 Å), although, in some rare cases, flares have been seen in white light. At present, solar patrol observations are almost continuous and so most of the flares occurring on the solar hemisphere facing the earth are detected. Flares are frequent occurrences, particularly at the peak of the sunspot cycle.

Flares are divided into classes of importance 1-, 1, 1+, 2, 2+, 3, and 3+, according to area and brightness. The average duration of a flare increases with its importance; thus 1 flares last about 20 min, 2 flares last about 30 min, and 3 flares last about 60 min. Of course, the life of an individual flare may vary greatly from the mean value. Flares smaller than importance 1 are referred to as subflares.

The development of a flare is somewhat as follows: a rapid rise (flash) to peak intensity, a brief period of peak intensity, followed by a steady decline. There is a close statistical relation between the number of flares per solar rotation, N_F , and the corresponding mean sunspot numbers \bar{R} , given by

$$N_F = a(\bar{R} - 10).$$
 (1.57)

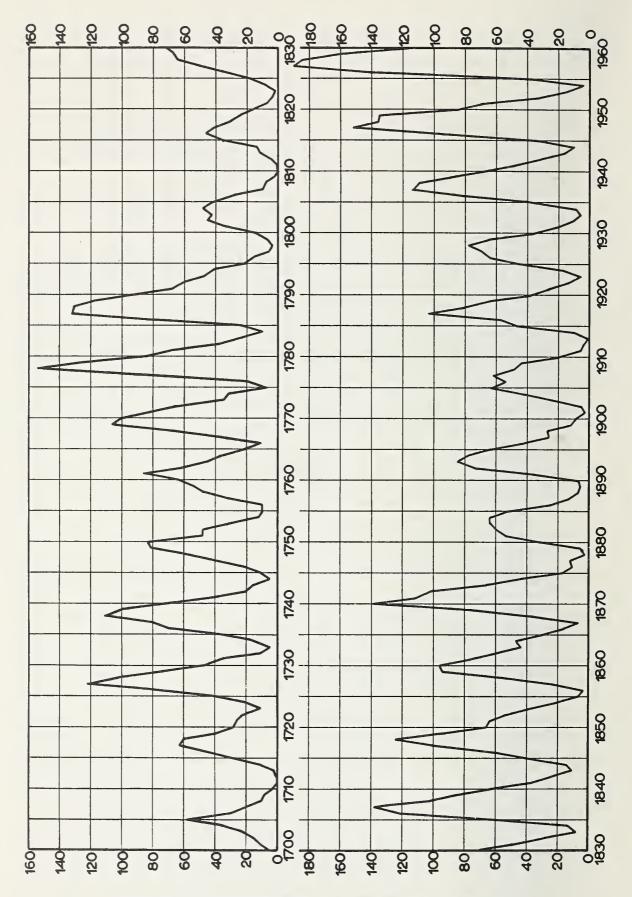


FIGURE 1.15. Sunspot activity in the years 1700 to 1960.

(After M. Waldmeier, 1961, Schulthess, Zurich.)

The mean values of a for the sunspot cycles having peaks in 1937 and 1947 are 1.98 and 1.47 respectively [18].

During some flares there is a marked increase in the flux of solar ionizing radiation in the far ultraviolet and soft x-ray regions of the spectrum. This results in enhancements in the electron densities in the D and E regions, as will be seen later. Data on the duration and importance of flares, etc., can be found in the F Series Part B [16] and in the IAU Bulletin [17].

1.7.2.4. Radio Emissions

The amplitude of the solar signals may remain relatively constant for long periods of time and then will be greatly enhanced during a "noise storm." These storms are often associated with solar flares and certain geophysical disturbances and may last for a period of hours or days.

Noise bursts are categorized as follows:

Type I, or noise storms, occur most frequently on frequencies less than about 300 Mc/s. Type I bursts extend over a narrow frequency range, 5 to 30 Mc/s, for instance, while their lifetimes range from 0.2 sec to 1 min or so. During the lifetime of a single burst, the frequency of emission may drift with time to higher or to lower frequencies.

Certain outbursts, which last for the order of several minutes, are associated with the larger solar flares and may involve signal enhancements of the order of a million times the quiet values.

The chief characteristic of Type II (slow drift) and Type III (fast drift) bursts is the drift of the emission to lower frequency with time. This drift can be explained as due to a source moving outwards through the corona, emitting at the plasma frequency, which decreases as the electron density decreases (see sec. 2.3.1.1). Type III events are very frequent.

Type IV events are long-lived emissions emanating from a source of large extent that moves to heights of the order of a solar radius. Radiation occurs over a broad band of frequencies at each height. The characteristics of type IV radiation can be explained by synchrotron emission of electrons. From the point of view of sun-earth relationships, type IV events are particularly important because of the strong association with solar corpuscular radiation, evidenced by polar cap absorption events [19, ch. 6], ground-level cosmic ray increases, and great magnetic storms.

Type V is continuum emission of shorter duration, following a type III burst.

A considerable amount of data is made available every month in the F Series Part B $\lceil 16 \rceil$.

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CHAPTER 2

Theory of Wave Propagation

2.1. PURPOSE

The purpose of this chapter is to acquaint the reader with the basic ideas needed for an understanding of the propagation of radio waves in the ionosphere. In the presence of the earth's magnetic field, the ionosphere behaves as a birefringent medium and so it is necessary to discuss the properties of such a medium. These properties include the decomposition of a plane polarized wave into ordinary and extraordinary waves and the deviation of the direction of energy flow away from the direction of phase propagation.

We shall consider first the early history of the subject leading to the formulation of Maxwell's equations and their experimental verification by Hertz. Next we shall derive the Appleton formula for the complex refractive index of a magneto-ionic medium and consider its properties.

The weakness of the Appleton theory will be considered and more generalized formulas will be discussed. Finally, we shall discuss the propagation of wave packets in a magneto-ionic medium.

2.2. ELECTROMAGNETIC WAVES

2.2.1. Electrostatics and Magnetostatics

The principles underlying the propagation of radio waves are based on the relationships between electricity and magnetism which were discovered in the eighteenth and nineteenth centuries. It is now generally known that the attractive and repulsive properties of electrified bodies and of lodestone were first recorded by the ancient Greeks. Little further progress was made until the eighteenth century, when attempts were made to establish laws of electrical and magnetic forces similar to the

gravitational law of Newton. This search bore fruit when, in 1785, the French scientist Coulomb, using a torsion balance, showed that the mechanical force between two small electrified spheres varies inversely as the square of the distance r between them. Later work showed that the force was proportional also to the amounts of charge q_1 , q_2 on the two bodies and so we obtain the relationship

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2},\tag{2.1}$$

where ϵ_0 is the permittivity of free space (8.85×10⁻¹² F/m).

A relationship similar to (2.1) was found to hold for the mutual forces exerted by long bar magnets.

It is useful to introduce the concept of electric field E at this point. Let us assume that the charge q_2 produces an electric field E at the site of q_1 and that this field exerts the force F on q_1 where

$$\mathbf{F} = q_1 \mathbf{E}. \tag{2.2}$$

Thus the electric field E at a point may be defined as the force experienced by a small unit test charge. It is assumed that the test charge itself does not alter the field.

The field at a vector distance \mathbf{r} from a point charge q is, therefore, given by

$$\mathbf{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^3} \mathbf{r},\tag{2.3}$$

so that the vector E is in the direction of r. If the charge is distributed throughout a volume of space, we have

$$\mathbf{E} = \frac{\mathbf{A}_r}{4\pi\epsilon_0} \int \frac{dq}{r^2} \,, \tag{2.4}$$

where dq is an element of charge and A_r is a unit vector in the direction from dq.

Many electrical and magnetic problems, particularly static field problems, are best tackled through the idea of potential difference. The potential difference between two points A and B can be defined as the work done by an external force on a unit test charge in moving it from A to B as shown in figure 2.1. The zero of potential is, therefore, arbitrary;

ELECTRIC FIELD E

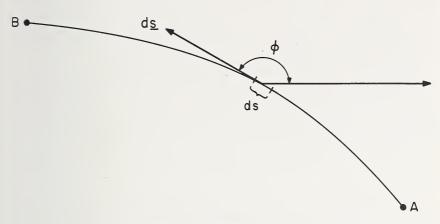


FIGURE 2.1. Potential difference.

and it is sometimes convenient to define the zero at infinity. The work done on the test charge in moving it from A to B is

$$V_B - V_A = -\int_A^B E \cos \phi \, ds = -\int_A^B \mathbf{E} \cdot d\mathbf{s},$$
 (2.5)

and hence

$$\mathbf{E} = -\frac{dV}{ds} = -\operatorname{grad} V. \tag{2.6}$$

Gauss showed that the integral of the electric field over a surface A enclosing a medium of permittivity ϵ is given by

$$\epsilon \int_{A} \mathbf{E} \cdot d\mathbf{A} = \int_{V} \rho \ dV = Q, \tag{2.7}$$

where ρ is the charge density, V is the volume enclosed, and Q is the total charge enclosed.

Similarly, for a magnetic field of induction B Wb/m² (webers per square meter),

$$\int_{A} \mathbf{B} \cdot d\mathbf{A} = 0. \tag{2.8}$$

This follows since there are no free magnetic poles.

Before proceeding to a consideration of current electricity let us consider some elementary properties of dielectrics. Consider a parallel plate capacitor with a large area of cross section (so that edge effects are negligible), and distance d between plates, connected to a voltage source V, and let σ be the charge density on one of the plates. From (2.7) we can show that the field E between the plates is given by

$$\epsilon_0 E = \sigma, \tag{2.9}$$

and, by definition,

$$E = \frac{V}{d} \,. \tag{2.10}$$

Now on the introduction of a slab of dielectric, of thickness d, between the plates, the positive nuclei in the atoms of the dielectric will tend to be displaced in the direction of smaller field while the negative charges (electrons) will tend to be displaced up the field, i.e., the medium becomes polarized. Thus a back electromotive force is set up which will tend to decrease the field between the plates.

Now the total field E, as given by (2.10), is independent of the dielectric. Hence, the charge density on the plates must increase by an amount σ_i , for instance. We can regard the polarization of the dielectric as conferring on it an effective permittivity ϵ so that from (2.7) we obtain

$$\epsilon E = \sigma + \sigma_i. \tag{2.11}$$

Imagine a cylinder of dielectric of unit cross section with its axis perpendicular to the plates. At the end surfaces will be charges $+\sigma_i$ and $-\sigma_i$ at a distance d apart. Hence we have the equivalent of a dipole of moment $\sigma_i d$. The electric moment per unit volume is, therefore, σ_i which is called the polarization P. The total quantity $\sigma + \sigma_i$ is known as the displacement D. Hence we have the relationship

$$D = \epsilon_0 E + P. \tag{2.12}$$

Now in certain media (anisotropic) the application of an electric field in one direction gives rise to a polarization in some other direction. Under these circumstances (2.12) has to be expressed as a vector equation:

$$\mathbf{D} = \epsilon_0 \mathbf{E} + \mathbf{P}. \tag{2.13}$$

This relation is of great importance in ionospheric radio propagation as will be seen later.

2.2.2. Ampère's Circuital Law

One of the most important observations in the study of electromagnetism was that of Oersted, who found, in 1819, that a pivoted magnet was deflected when in the vicinity of an electric current. This experiment demonstrated that a current of electricity produced a magnetic field. As in the case of static electricity and magnetism, it was found that the magnetic field produced by a current element decreased as the square of the distance from the element. This led Ampère to formulate his circuital law, namely, that the line integral of the tangential magnetic field \mathbf{H}_t taken around a current i was equal to the component of the current flowing normal to the surface A enclosed (see fig. 2.2),

$$\oint_{S} \mathbf{H}_{t} \cdot d\mathbf{s} = \int_{A} \mathbf{J} \cdot d\mathbf{A} = i,$$
(2.14)

where **J** is the current density through the surface A enclosed by the path of integration S. Note that **H** refers to magnetic intensity which, in a medium of magnetic permeability μ , is related to magnetic induction **B** by the formula

$$\mathbf{B} = \mu \mathbf{H}.\tag{2.15}$$

2.2.3. Faraday's Law

Efforts to observe the electrical effects of magnetic fields bore fruit in 1831 when Faraday found that a current was produced in a coil of

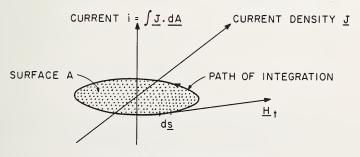


FIGURE 2.2. Ampère's circuital law.

wire by the following processes: (1) when a magnet was moving near it and/or (2) when a current in an adjacent coil was switched on and off.

Faraday carried out a large number of beautiful experiments to verify the phenomena of electromagnetic induction and the serious reader is recommended to read Faraday's account in his book Experimental Researches in Electricity [1].¹

Faraday's results may be summed up in the following two laws:

- (a) When the flux of magnetic induction through a coil is changing, an electromotive force is induced in the circuit.
- (b) The magnitude of the emf ϵ is proportional to the rate of change of flux.

The sign of the emf is given by Lenz's law, which states that it is such that any current flow is in the direction which would oppose the flux change causing the emf.

Therefore

$$\mathcal{E} = -\frac{dN}{dt},\tag{2.16}$$

where N is the total flux through the coil, i.e., induction times area, normal to the surface, that is

$$N = \int_{A} \mathbf{B} \cdot d\mathbf{A}. \tag{2.17}$$

Consider now the integral of the electric field round a loop which, as shown in figure 2.3, has a small gap *CD* and through which is threaded a time-varying magnetic field. The integral

$$\int_C^D \mathbf{E} \cdot \mathbf{ds}$$

is the total voltage between C and D, that is, the induced emf, ε .

Hence, when C and D are brought together we arrive at the formula

$$\oint \mathbf{E} \cdot d\mathbf{s} = -\frac{d}{dt} \int \mathbf{B} \cdot d\mathbf{A}. \tag{2.18}$$

It must be stressed that this relationship is quite general in spite of the fact that we have derived it for a particular case only.

¹ Figures in brackets indicate the literature references on p. 99.

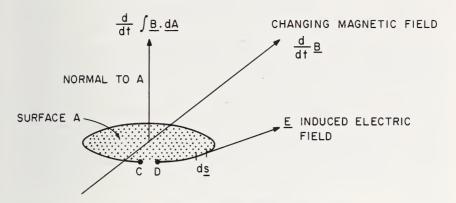


Figure 2.3. Faraday's electromagnetic induction law.

It is convenient, at this point, to summarize the essential equations obtained above. They are:

The electric field
$$\epsilon \int_{A} \mathbf{E} \cdot d\mathbf{A} = \int_{V} \rho \ dV$$
, (a)

The magnetic field $\int_{A} \mathbf{B} \cdot d\mathbf{A} = 0$, (b)

Magnetic field of a current $\oint \mathbf{H} \cdot d\mathbf{s} = \int \mathbf{J} \cdot d\mathbf{A}$, (c)

Electromagnetic induction $\oint \mathbf{E} \cdot d\mathbf{s} = -\frac{d}{dt} \int \mathbf{B} \cdot d\mathbf{A}$. (d)

2.2.4. The Displacement Current

It would appear, at first sight, as if eqs (2.19) are complete in themselves and define the electromagnetic field uniquely. However, that this is not so was discovered by Maxwell in the course of his studies on the charging of a capacitor (Leyden jar).

Consider the charging of a parallel plate capacitor with an insulator as dielectric so that no current can flow between the plates. Let us apply (2.19c) to a closed loop around the wire to a plate. If the surface enclosed by the loop cuts the wire, then $\mathcal{F}\mathbf{H}\cdot d\mathbf{s}$ around the loop is non-zero. Now it is possible to construct a surface which envelopes the plate of the capacitor and which passes between the plates. Since there is no flow of electricity between the plates, application of (2.19c) shows that $\mathcal{F}\mathbf{H}\cdot d\mathbf{s}$ around the loop is zero. We thus arrive at a contradiction. James Clerk Maxwell's great contribution to electromagnetic theory was his assertion that the circuit through a capacitor should be considered as closed. He showed, furthermore, that the current density through the insulator between the plates is due to the time rate of change of the displacement D, i.e.,

$$J = \frac{i}{A} = \frac{1}{A} \frac{dq}{dt} = \frac{1}{A} \frac{d}{dt} (\sigma + \sigma_i) A = \frac{dD}{dt}, \qquad (2.20)$$

where q is the charge on the plate.

Maxwell maintained that as far as the electromagnetic field was concerned, the displacement current was just as important as a flow of electricity and that it must be added to the current on the right hand side of (2.19c). This enables us to write Maxwell's equations in integral form as follows:

$$\int_{A} \mathbf{D} \cdot d\mathbf{A} = \int_{V} \rho \, dV, \qquad (a)$$

$$\int_{A} \mathbf{B} \cdot d\mathbf{A} = 0, \qquad (b)$$

$$\oint \mathbf{H} \cdot d\mathbf{s} = \int \mathbf{J} \cdot d\mathbf{A} + \frac{d}{dt} \int \mathbf{D} \cdot d\mathbf{A}, \qquad (c)$$

$$\oint \mathbf{E} \cdot d\mathbf{s} = -\frac{d}{dt} \int \mathbf{B} \cdot d\mathbf{A}. \qquad (d)$$

For Maxwell's own account of the derivation of these formulas the reader should consult his "A Treatise on Electricity and Magnetism" [2].

2.2.5. A Solution of Maxwell's Equations

In order to solve the set of eqs (2.21), it is necessary to express them in their differential forms. This can be achieved by means of the following two vector theorems:

Green's Theorem

Let F be any vector function and V a volume bounded by the closed surface A: then

$$\int_{A} \mathbf{F} \cdot d\mathbf{A} = \int_{V} \operatorname{div} \mathbf{F} \ dV. \tag{2.22}$$

Stokes' Theorem

Let F be a vector function and A a surface (not closed) bounded by a simple closed curve S; then

$$\oint_{S} \mathbf{F} \cdot d\mathbf{s} = \oint_{A} \operatorname{curl} \mathbf{F} \cdot d\mathbf{A}. \tag{2.23}$$

Applying these transformations to (2.21) we obtain

$$\operatorname{div} \mathbf{D} = \rho, \qquad (a)$$

$$\operatorname{div} \mathbf{B} = 0, \qquad (b)$$

$$\operatorname{curl} \mathbf{H} = \mathbf{J} + \dot{\mathbf{D}}, \qquad (c)$$

$$\operatorname{curl} \mathbf{E} = -\dot{\mathbf{B}} = -\mu \dot{\mathbf{H}}, \qquad (d)$$

where the dot signifies the time derivative.

Let us consider a solution of these equations in a medium having the following properties:

- (i) Magnetically and electrically isotropic, that is, having the same properties in all directions.
 - (ii) Electrically neutral, no net space charge so that $\rho = 0$.
 - (iii) Electrically nonconducting, i.e., J=0.
 - (iv) A field varying in the 1-direction only in a right-handed orthog-

onal system of axes (1, 2, 3), so that

$$\frac{\partial}{\partial x_2} = \frac{\partial}{\partial x_3} = 0.$$

With these restrictions, we obtain

$$\operatorname{curl} \mathbf{H} = +\dot{\mathbf{D}}, \qquad (a)$$

$$\operatorname{curl} \mathbf{E} = -\mu \dot{\mathbf{H}}. \qquad (b)$$
(2.25)

Taking the curl of (2.25a) we have

curl curl
$$\mathbf{H} = +\text{curl } \dot{\mathbf{D}}$$

= $+\epsilon$ curl $\dot{\mathbf{E}}$ (2.26)
= $-\epsilon \mu \dot{\mathbf{H}}$.

Now it can be shown that, for any vector F,

curl curl
$$\mathbf{F} = \text{grad div } \mathbf{F} - \text{div grad } \mathbf{F}$$
. (2.27)

Since div B=0, then div H=0 and hence grad div H=0. Furthermore, under restriction (iv) we have

div grad
$$\mathbf{H} = \frac{\partial^2 H_1}{\partial x_1^2} + \frac{\partial^2 H_2}{\partial x_1^2} + \frac{\partial^2 H_3}{\partial x_1^2}$$
. (2.28)

Equation (2.26) thus reduces to

$$\frac{\partial^2 H_1}{\partial x_1^2} + \frac{\partial^2 H_2}{\partial x_1^2} + \frac{\partial^2 H_3}{\partial x_1^2} = \epsilon \mu \frac{\partial^2 H}{\partial t^2} . \tag{2.29}$$

Now

div
$$\mathbf{H} = \frac{\partial H_1}{\partial x_1} + \frac{\partial H_2}{\partial x_2} + \frac{\partial H_3}{\partial x_3} = \frac{\partial H_1}{\partial x_1} = 0,$$
 (2.30)

and if we select the 2- and 3-axes so that $H_2=0$, we obtain

$$\frac{\partial^2 H_3}{\partial x_1^2} = \epsilon \mu \frac{\partial^2 H_3}{\partial t^2} \,. \tag{2.31}$$

This is the equation of a plane transverse wave traveling in the 1-direction with a phase velocity v where

$$v = \frac{1}{\sqrt{\mu \epsilon}} \,. \tag{2.32}$$

Note that this can be shown by substituting a wave of the form $\cos 2\pi [ft \pm (x_1/\lambda)]$ and remembering that $v=f\lambda$. The — sign represents a wave traveling in the positive 1-direction and vice versa.

The free space velocity c is given by

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \,. \tag{2.33}$$

Now the refractive index n of the medium is given by the ratio c/v, so that

$$n = \frac{c}{v} = \sqrt{\frac{\mu \epsilon}{\mu_0 \epsilon_0}} \,. \tag{2.34}$$

In media which have no particular magnetic properties, $\mu = \mu_0$ and then

$$n = \sqrt{\frac{\epsilon}{\epsilon_0}} = \sqrt{K} \tag{2.35}$$

where K is the dielectric constant of the medium.

The equation of such a wave may be written in several different forms, each of which has its peculiar advantages, such as

$$E = E_0 \cos \omega \left(t - \frac{x_1}{v} \right), \qquad (a)$$

$$E = E_0 \cos k_0 (ct - nx_1), \qquad (b)$$

$$E = E_0 \cos (\omega t - kx_1), \qquad (c)$$

$$E = E_0 \exp i(\omega t - kx_1), \qquad (d)$$

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$$k = \frac{2\pi}{\lambda}$$
 the propagation factor,

$$k_0 = \frac{2\pi}{\lambda_0}$$
 the phase constant,

 λ_0 = the free space wavelength,

 λ = actual wavelength in the medium,

$$i = \sqrt{-1}$$
.

It is of historical interest to note that Maxwell used a mixed (electrostatic and electromagnetic) system of units and he found that the velocity c is given by the ratio of the electromagnetic to the electrostatic unit of charge. This ratio was known to be about 3×10^8 m/sec, or close to the velocity of light. This agreement led Maxwell to claim that light was indeed an electromagnetic phenomenon.

The existence of electromagnetic waves was demonstrated conclusively, around 1888, when Hertz [3] showed that the disturbances generated by a spark coil could be reflected, refracted, focused, and polarized.

2.2.6. Some Properties of Electromagnetic Waves

Let us consider some of the properties of a plane electromagnetic wave propagating in an isotropic nonconducting medium. If the wave is traveling in the 1-direction we have $\partial/\partial x_2 = \partial/\partial x_3 = 0$, since, for a given value of x_1 , the fields are constant over the whole 2-3 plane. Equation (2.25) can be written

$$\frac{\partial H_3}{\partial x_2} - \frac{\partial H_2}{\partial x_3} = \epsilon \frac{\partial E_1}{\partial t}, \qquad (a)$$

$$\frac{\partial H_1}{\partial x_3} - \frac{\partial H_3}{\partial x_1} = \epsilon \frac{\partial E_2}{\partial t}, \qquad (b)$$

$$\frac{\partial H_2}{\partial x_1} - \frac{\partial H_1}{\partial x_2} = \epsilon \frac{\partial E_3}{\partial t}, \qquad (c)$$

$$\frac{\partial E_3}{\partial x_2} - \frac{\partial E_2}{\partial x_3} = -\mu_0 \frac{\partial H_1}{\partial t}, \quad (a)$$

$$\frac{\partial E_1}{\partial x_3} - \frac{\partial E_3}{\partial x_1} = -\mu_0 \frac{\partial H_2}{\partial t}, \qquad (b)$$
 (2.38)

$$\frac{\partial E_2}{\partial x_1} - \frac{\partial E_1}{\partial x_2} = -\mu_0 \frac{\partial H_3}{\partial t} \,. \tag{c}$$

Let us rotate our system of axes so that the 2-axis lies parallel to the **E** vector. Then $E_2 = E$, and $E_3 = 0$. Since $\partial/\partial x_2 = \partial/\partial x_3 = 0$, (2.37) and (2.38) become

$$\frac{\partial E_1}{\partial t} = 0,$$
 (a)

$$-\frac{\partial H_3}{\partial x_1} = \epsilon \frac{\partial E_2}{\partial t}, \qquad (b)$$

$$\frac{\partial H_2}{\partial x_1} = \epsilon \frac{\partial E_3}{\partial t} = 0, \quad (c)$$

$$\frac{\partial H_1}{\partial t} = 0, \qquad (a)$$

$$\frac{\partial E_3}{\partial x_1} = -\mu_0 \frac{\partial H_2}{\partial t} = 0, \qquad (b)$$

$$\frac{\partial E_3}{\partial x_1} = -\mu_0 \frac{\partial H_2}{\partial t} = 0, \qquad (b)$$

$$\frac{\partial E_2}{\partial x_1} = -\mu_0 \frac{\partial H_3}{\partial t} \,. \tag{c}$$

From (2.39a) and (2.40a) we see that there is no time-varying component of E or H in the 1-direction. That is, the electromagnetic wave is entirely *transverse*.

Equations (2.39c) and (2.40b), respectively, tell us that H has no space- or time-varying components in the 2-direction. Hence E and H are perpendicular to each other and to the direction of propagation. We shall see later that this is not necessarily the case for propagation in the ionosphere.

To determine the phase relationship between E and H, substitute the expression $E_2 = E_{20} \cos (\omega t - kx_1)$ in (2.39b) or (2.40c). This gives

$$H_{3} = \frac{kE_{2o}}{\omega\mu_{0}}\cos(\omega t - kx_{1}), \qquad (a)$$

$$H_{3} = H_{3o}\cos(\omega t - kx_{1}), \qquad (b)$$
(2.41)

where

$$H_{3o} = \frac{k}{\omega \mu_0} E_{2o} = \frac{v}{\mu_0} E_{2o} = \frac{n}{c\mu_0} E_{2o}. \tag{2.42}$$

Equations (2.41) show that, if n is real, E and H are in phase. Equation (2.42) gives us the relationship between the peak amplitudes of E and H in terms of the refractive index n of the medium.

The energy density U_e in the electric field is given by

$$U_e = \frac{1}{2}DE = \frac{1}{2}\epsilon E^2,$$
 (2.43)

and in the magnetic field

$$U_m = \frac{1}{2}BH = \frac{1}{2}\mu_0 H^2. \tag{2.44}$$

Hence the ratio of the energy densities is given by

$$\frac{U_e}{U_m} = \frac{\epsilon}{\mu_0} \left(\frac{E}{H}\right)^2 = 1,\tag{2.45}$$

so that the energy is divided equally between the electric and magnetic fields.

The flux of energy per unit area in the direction of propagation is given by the Poynting vector [4],

$$S = E \times H. \tag{2.46}$$

For a sinusoidally varying wave, S has to be averaged over a complete cycle. This gives

$$S_{\rm av} = \frac{1}{2} E_0 H_0. \tag{2.47}$$

In general, the E and H vectors will be complex quantities and, in this case, it can be shown [4] that the average of the complex Poynting vector is given by

$$S_{av} = \frac{1}{2}E \times H^* \tag{2.48}$$

where H* is the complex conjugate of H.

2.3. Magneto-Ionic Theory

2.3.1. Motion of lons in Electric and Magnetic Fields

2.3.1.1. Motion in an Electric Field

It will be recalled that, in chapter 1, we discussed the existence of free electrons and ions in the earth's atmosphere (ionosphere) and, also, the existence of the earth's magnetic field. It is the purpose of this section to discuss the propagation of radio waves in a conducting medium in the presence of a superposed magnetic field.

First of all, let us examine the motions of ions in the presence of static fields.

The equation of motion of an ion of charge e and mass m in an electric field E V/m, in the 2-direction, is

$$m\ddot{x}_2 = eE, \tag{2.49}$$

from which, by integration, we obtain the velocity

$$\dot{x}_2 = -\frac{e}{m}Et \tag{2.50}$$

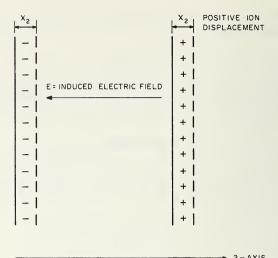


FIGURE 2.4. Force on an electron due to plasma displacement.

assuming that the ion starts from rest.

If the ion concentration is N (per cubic meter), the current density created is

$$J = Ne\dot{x}_2 = \frac{Ne^2}{m}Et.$$
 (2.51)

Consider now a slab of plasma (a medium containing free charges) in which the light electrons and the heavy positive ions are displaced, as shown in figure 2.4, by a distance x_2 . Such a displacement will produce charges on the surface of the slab and an electric field E will be set up in the slab as in the case of a parallel plate capacitor.

The surface charge density is Nex_2 so that from (2.9) the field is given by

$$E = -\frac{Ne}{\epsilon_0} x_2. \tag{2.52}$$

The — sign arises because E is in the *opposite* direction to the displacement x_2 . There will be a restoring force due to the electrostatic attraction; the equation of motion of an ion is

$$m\ddot{x}_2 = eE = -\frac{Ne^2}{\epsilon_0}x_2$$

$$\ddot{x}_2 + \frac{Ne^2}{\epsilon_0 m} x_2 = 0. \tag{2.53}$$

This is the equation of a simple harmonic motion with angular frequency ω_N given by

$$\omega_N^2 = \frac{Ne^2}{\epsilon_0 m},\tag{2.54}$$

where ω_N is called the angular plasma frequency.

2.3.1.2. Motion in a Magnetic Field

The force F exerted on an ion of charge e moving with velocity v in a magnetic field B Wb/m^2 is

$$\mathbf{F} = e\mathbf{v} \times \mathbf{B},\tag{2.55}$$

$$F = ev\mathbf{B}\sin\theta,\tag{2.56}$$

where θ is the angle between v and B. Equation (2.56) shows that the force on a moving charge is proportional to the component of the magnetic field transverse to the direction of motion. Thus, if we shoot an ion into a region where there is a magnetic field, the component of motion parallel to the field will be unaltered whereas there will be a force, and hence an acceleration, due to the component of motion perpendicular to the magnetic field. This acceleration tends to bend the path around the lines of force. The ion motion is, therefore, a helix. The projection on to a plane perpendicular to the magnetic field is a circle of radius r_H , which is determined by balancing the centrifugal force $mr_H\omega_H^2$ against the centripetal force ev_TB . Here ω_H is the angular velocity and v_T is the transverse component of velocity $r_H\omega_H$. Now $mr_H\omega_H^2 = er_H\omega_H B$, hence,

$$\omega_H = \frac{e}{m}B, \qquad (a)$$

$$f_H = \frac{1}{2\pi} \frac{e}{m}B. \qquad (b)$$
(2.57)

Here f_H is called the gyro (or gyromagnetic) frequency and ω_H the angular gyrofrequency.

Notice that f_H is independent of the velocity of the ion. For electrons we have

$$f_H = 2.84 \times 10^{10} B = 3.57 \times 10^4 H.$$
 (2.58)

Now in the ionosphere, B is on the order of 0.5 G or 0.5×10^{-4} Wb/cm⁻²; therefore, $f_H = 1.42 \times 10^6$ c/s⁻¹ or 1.42 Mc/s.

The numerical value of f_H is of great importance in ionospheric radio wave propagation because it lies in the band of frequencies, reflected from the ionosphere, which are of use in radio communication.

2.3.1.3 Motion in Crossed Electric and Magnetic Fields

When magnetic and electric fields are present, the motion of an ion is complicated except in the case where they are parallel.

When the fields are perpendicular, for example, when E is in the 1-direction and B is in the 2-direction, of a right-handed system of axes (see fig. 2.5), the motion produced by the electric field is altered by the magnetic field. The motion in the direction of the electric field does not increase indefinitely, but the ion swings around and eventually moves

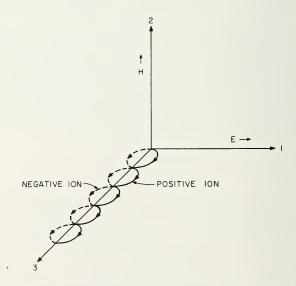


FIGURE 2.5. Motion of ions in the presence of crossed electric and magnetic fields.

against the electric field, as illustrated in figure 2.5. The average ion motion is in the 3-direction and is independent of the mass and charge of the ion and even of the sign of the charge, negative and positive ions both moving in the same direction. Hence, in an electrically neutral medium there is no resultant current in the 3-direction, except insofar as these conditions may be altered by collisions.

2.3.2. Derivation of the Appleton Formula

The formulas for the complex refractive index of a medium such as the ionosphere were derived by a number of people during the 1920's but the name most commonly associated with the theory is that of Sir Edward Appleton [5].

In 1931, D. R. Hartree [6] suggested that it was appropriate to include the Lorentz polarization term in the theory. Although the bulk of both theoretical and experimental evidence indicates that the inclusion of the term is unjustified, the formula for the complex refractive index is often referred to as the Appleton-Hartree formula.

The influence of heavy ions on the refractive index was considered by Goubau [7] in 1935, and since then more realistic distributions of collision statistics have been introduced by Phelps [8] and by Sen and Wyller [9].

In order to derive the formula for the refractive index it is necessary to define certain properties of both the wave and the medium. For our present purposes we shall assume the following properties:

Wave Properties

- (1) Simple harmonic progressive wave.
- (2) Steady-state solution.
- (3) Plane waves with given polarization. We shall call such waves characteristic waves [10].

Properties of the Medium

- (4) Electrically neutral.
- (5) Charges distributed with statistical uniformity so that there is no resultant space charge.
 - (6) Uniform external magnetic field.
 - (7) Electrons only are effective.
 - (8) Electronic collisions are independent of electron energy.
- (9) The thermal motions of the electrons are unimportant. Such a medium is called a *cold plasma*.
 - (10) The magnetic properties are those of free space.

Our procedure will now be as follows. First, we will apply Maxwell's equations to the wave and, secondly, we shall impose the properties of the medium, the so-called "constitutive relations."

In our application of Maxwell's equations in the form given in (2.24) we are at liberty either to consider the medium as a conductor, so that there is a conduction current (i.e., $J\neq 0$), or we may consider it as a polarizable medium in which the movement of the ions is included in the P term of (2.13). It is most important to realize that we cannot do both. For our present purposes let us use the second alternative, and express the refractive index in terms of the components of P and E.

From (2.24) and condition 4 we have

$$\operatorname{div} \mathbf{D} = \frac{\partial D_1}{\partial x_1} + \frac{\partial D_2}{\partial x_2} + \frac{\partial D_3}{\partial x_3} = 0, \qquad (a)$$

$$\operatorname{div} \mathbf{B} = \frac{\partial B_1}{\partial x_1} + \frac{\partial B_2}{\partial x_2} + \frac{\partial B_3}{\partial x_3} = 0, \qquad (b)$$

$$\operatorname{curl} \mathbf{H} = \dot{\mathbf{D}} = \epsilon_0 \dot{\mathbf{E}} + \dot{\mathbf{P}}, \qquad (c)$$

$$\operatorname{curl} \mathbf{E} = -\dot{\mathbf{B}}. \qquad (d)$$

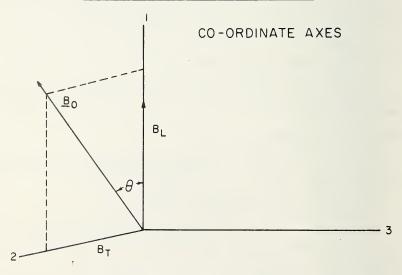


FIGURE 2.6. System of axes.

Consider a characteristic wave, having properties (1), (2), and (3) above, to be traveling along the 1-axis of a right-handed orthogonal system with axes 1, 2, and 3 as shown in figure 2.6. The components of the wave vary in time as $\exp(+i\omega t)$ and in space as $\exp(-ikx_1)$ and do not vary in the 2- and 3-directions.

Since we are considering the charge oscillation as a polarization of the medium then we have, from (2.13)

$$D = \epsilon_0 E + P$$
,

which expresses the electrical anisotropy of the medium. The magnetic properties, given by $B = \mu_0 H$, are those of free space.

A plane wave traveling in the positive 1-direction can be expressed by an equation of the form

$$E = E_0 \cos (\omega t - kx_1), \qquad (a)$$
or $E = E_0 \exp i(\omega t - kx_1). \qquad (b)$

Since the electric and magnetic vectors of the wave do not vary in the 2- and 3-directions we have, using the notation of (2.60b),

$$\frac{\partial}{\partial x_1} = ik, \qquad (a)$$

$$\frac{\partial}{\partial x_2} = \frac{\partial}{\partial x_3} = 0, \quad (b)$$

$$\frac{\partial}{\partial t} = i\omega, \qquad (c)$$

$$\frac{\partial^2}{\partial t^2} = -\omega^2. \qquad (d)$$

Substituting these in (2.59a) and (b) we obtain

$$D_{1} = \epsilon_{0}E_{1} + P_{1} = 0, \quad (a)$$

$$B_{1} = \mu_{0}H_{1} = 0. \quad (b)$$
(2.62)

Before dealing with the curl equations, let us consider the implications of (2.62). Equation (2.62a) states that there is no component of D in the direction of phase propagation. However P_1 and E_1 are not necessarily non-zero; this means that P and E may have components in the 1-direction. Furthermore, since the vector P is a measure of the electron displacement from its mean position, the electron motion has a component in the direction of propagation. Equation (2.62b) implies that both the B and H vectors are entirely transverse to the direction of propagation.

Substituting (2.61) in the curl equations (2.59c) and (d) we obtain

$$egin{aligned} &-rac{\partial H_3}{\partial x_1} = -ikH_3 = i\omega \left(\epsilon_0 E_2 + P_2
ight), \ &-rac{\partial E_3}{\partial x_1} = ikE_3 = -\mu_0 i\omega H_2, \ &rac{\partial H_2}{\partial x_1} = ikH_2 = i\omega \left(\epsilon_0 E_3 + P_3
ight), \ &rac{\partial E_2}{\partial x_1} = ikE_2 = -\mu_0 i\omega H_3. \end{aligned}$$

This is

$$\epsilon_0 E_2 + P_2 = -\frac{k}{\omega} H_3 = D_2,$$
 (a)
$$\epsilon_0 E_3 + P_3 = \frac{k}{\omega} H_2 = D_3,$$
 (b)
$$k E_3 = \mu_0 \omega H_2,$$
 (c)
$$-k E_2 = \mu_0 \omega H_3.$$
 (d)

Our next step is to express the refractive index in terms of the P's and E's. To do this we shall eliminate H_3 from (2.63a) and (d). This gives

$$\epsilon_0 E_2 + P_2 = -\frac{k}{\omega} \left(-\frac{kE_2}{\mu_0 \omega} \right) = \frac{k^2}{\omega^2 \mu_0} E_2,$$

or

$$1 + \frac{1}{\epsilon_0} \frac{P_2}{E_2} = \left(\frac{k}{\omega}\right)^2 \frac{1}{\mu_0 \epsilon_0} = \left(\frac{ck}{\omega}\right)^2. \tag{2.64}$$

From the definitions of k, ω , and n it follows that

$$n = \frac{ck}{\omega} \ . \tag{2.65}$$

Hence

$$n^2 = 1 + \frac{1}{\epsilon_0} \frac{P_2}{E_2}, \qquad (a)$$
 similarly
$$(2.66)$$

$$n^2 = 1 + \frac{1}{\epsilon_0} \frac{P_3}{E_3}. \qquad (b)$$

From these equations it follows that

$$\frac{E_2}{E_3} = \frac{P_2}{P_3}$$
,

and with (2.63) we obtain

$$-\frac{H_2}{H_3} = \frac{E_3}{E_2} = \frac{P_3}{P_2} = R,$$
 (2.67)

where R is called the wave polarization.

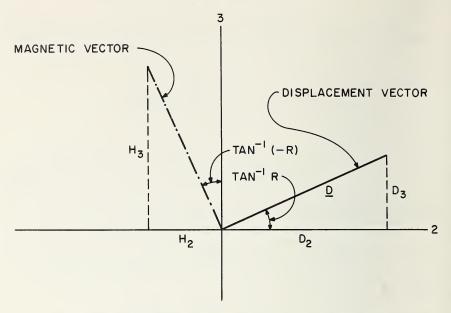


FIGURE 2.7. Relationship between the instantaneous D and H vectors in the plane of the wavefront.

Note that when R is real, the E, D, and P vectors are linearly polarized along a direction making an angle $\tan^{-1} R$ with the 2-axis. On the other hand, the H vector is linearly polarized in a direction $\tan^{-1} (-R)$ with the 3-axis (see fig. 2.7). From this it follows that the H vector is perpendicular to the D vector and to the projections of the E and P vectors on the 2-3 plane.

When R is complex the H and D vectors describe ellipses in the 2-3 plane as also do the projections on the wavefront of the E and P vectors.

When the propagation factor k is real, equations (2.63) imply that the H vector and the D vector, and hence the projections of the E and P vectors on the wavefront, are always at right angles to each other and rotate in the same sense.

The above considerations apply to the propagation of characteristic waves in any medium. To find the refractive index we must now introduce the properties of the magneto-ionic medium. These properties are embodied in the constitutive relations.

We consider now the motion of electrons under the following influences:

- (1) The electric field of the wave.
- (2) The imposed magnetic field B₀.
- (3) Collisions between electrons and neutral molecules. For our present purposes we shall neglect the motion of the heavy ions.

The forces acting on an electron are

- (a) The electric force eE.
- (b) A force $ev \times B_0$ due to the electron motion v relative to the imposed magnetic field B₀.
- (c) A force mvv which represents the average rate of loss of momentum of the electron per collision.
- (d) A force due to electron motion in the magnetic field of the wave. This force is on the order of v/c of the force (a) above and will, therefore, be neglected.

To obtain the constitutive relations, we write down the equations of motion of the electrons under the combined influence of the electric field of the wave and of the imposed magnetic field. If the direction of propagation is along the 1-axis, as shown in figure 2.6, and the imposed magnetic field B_0 lies in the 2-3 plane making an angle θ with the direction of propagation, then the equations of motion are

$$m\ddot{x}_{1} = eE_{1} - e\dot{x}_{3}B_{T} - m\nu\dot{x}_{1}, \qquad (a)$$

$$m\ddot{x}_{2} = eE_{2} + e\dot{x}_{3}B_{L} - m\nu\dot{x}_{2}, \qquad (b)$$

$$m\ddot{x}_{3} = eE_{3} + e\dot{x}_{1}B_{T} - e\dot{x}_{2}B_{L} - m\nu\dot{x}_{3}. \qquad (c)$$

$$m\ddot{x}_2 = eE_2 + e\dot{x}_3B_L - m\nu\dot{x}_2,$$
 (b) (2.68)

$$m\ddot{x}_3 = eE_3 + e\dot{x}_1B_T - e\dot{x}_2B_L - m\nu\dot{x}_3.$$
 (c)

We now proceed to transform these equations by the following operations:

- Multiply throughout by Ne, where N is the electron number (i) density;
- Replace \dot{x}_1 by $i\omega x_1$, \ddot{x}_1 by $-\omega^2 x_1$, etc;
- (iii) Put $Nex_1 = P_1$, etc., the volume polarization.

With some rearrangement and introducing the accepted symbols, we obtain the constitutive relations.

$$\epsilon_{0}XE_{1} = -P_{1} + iP_{1}Z + iP_{3}Y_{T}, \qquad (a)$$

$$\epsilon_{0}XE_{2} = -P_{2} + iP_{2}Z - iP_{3}Y_{L}, \qquad (b)$$

$$\epsilon_{0}XE_{3} = -P_{3} + iP_{3}Z - iP_{1}Y_{T} + iP_{2}Y_{L}, \qquad (c)$$

$$\epsilon_0 X E_2 = -P_2 + i P_2 Z - i P_3 Y_L,$$
 (b) (2.69)

$$\epsilon_0 X E_3 = -P_3 + i P_3 Z - i P_1 Y_T + i P_2 Y_L,$$
 (c)

where $X = Ne^2/\epsilon_0 m\omega^2$, $Y_L = eB_L/m\omega$, $Y_T = eB_T/m\omega$, and $Z = \nu/\omega$.

The subscripts T and L refer to the transverse and longitudinal components of the imposed magnetic field with reference to the direction of the wave normal (i.e., phase propagation).

The next step in our derivation is to express the ratio P_2/E_2 or P_3/E_3 in terms of the parameters X, Y, and Z. This is best done via the wave polarization term R as follows: From (2.62a),

$$\epsilon_0 X E_1 = -X P_1.$$

Substitution in (2.69a) gives

$$\frac{P_1}{P_3} = \frac{i Y_T}{1 - X - iZ}. (2.70)$$

From (2.67) it follows that $P_2E_3 = P_3E_2$ so that by multiplying (2.69b) by P_3 and (2.69c) by P_2 and subtracting, we end up with

$$P_3^2 Y_L = P_1 P_2 Y_T - P_2^2 Y_L. (2.71)$$

With a little rearrangement, and remembering that $R = P_3/P_2$, we have from (2.70) and (2.71) the following quadratic expression in R:

$$Y_L R^2 - \frac{i Y_T^2}{1 - X - iZ} R + Y_L = 0. (2.72)$$

There are, in general, two solutions of this quadratic which are given by

$$R = \frac{i}{2Y_L} \left\{ \frac{Y_T^2}{(1 - X - iZ)} \mp \sqrt{\frac{Y_T^4}{(1 - X - iZ)^2}} + 4Y_L^2 \right\}.$$
 (2.73)

For the propagation of high-frequency radio waves through the E and F regions of the ionosphere, Z is usually very small and can be neglected. For instance, with a frequency of 10 Mc/s at the 100-km level ($\nu = 1.75 \times 10^3$ from table 1.3) we have $Z = 3 \times 10^{-4}$. Under these conditions R is given by

$$R = \frac{i}{2Y_L} \left\{ \frac{Y_T^2}{1 - X} \mp \sqrt{\frac{Y_T^4}{(1 - X)^2}} + 4Y_L^2 \right\}. \tag{2.74}$$

This formula tells us that, in general, there are two, and only two, char-

acteristic waves capable of propagation in our magneto-ionic medium. From (2.69b) we obtain

$$-\frac{P_2}{\epsilon_0 E_2} = \frac{X}{1 - iZ + iY_L R}, \qquad (2.75)$$

which, on substituting, in (2.66a) gives

$$n^{2} = 1 - \frac{X}{1 - iZ - \frac{Y_{T}^{2}}{2(1 - X - iZ)} \pm \sqrt{\frac{Y_{T}^{4}}{4(1 - X - iZ)^{2}}} + Y_{L}^{2}}}, \quad (2.76)$$

which is the Appleton formula.

In the upper regions of the ionosphere the collision frequency is sufficiently small so that, for frequencies greater than about 1 Mc/s, we may put Z=0, and hence the real part² μ of the refractive index is given by

$$\mu^{2} = 1 - \frac{2X(1-X)}{2(1-X) - Y_{T}^{2} \pm \sqrt{Y_{T}^{4} + 4(1-X)^{2}Y_{L}^{2}}}.$$
 (2.77)

In the absence of an imposed magnetic field $(Y_T = Y_L = 0)$ and of collisions (Z=0) the refractive index is given by

$$\mu^{2} = 1 - X = 1 - \left(\frac{f_{N}}{f}\right)^{2} = 1 - k\frac{N}{f^{2}}, \qquad (2.78)$$

where $k = (e^2/4\pi^2\epsilon_0 m) = 80.5$ and f is in cycles per second.

2.3.3. Some Properties of the Appleton Formula

2.3.3.1. No Magnetic Field, No Collisions

In a discussion of the properties of the Appleton formula it is best to start with the simplest case, that is, with (2.78). First it will be seen that the square of the refractive index must be equal to or less than unity. Furthermore, for propagation of the wave, μ must be real so that μ must

² Henceforth the symbol μ will be used in this sense and not for magnetic permeability.

lie between 0 and 1. Secondly, we see that, for a given wave frequency, the refractive index decreases with increase of electron density, and that, for a given electron density, the refractive effects decrease with increase of frequency but are independent of the amplitude of the wave.

Curves depicting the variation of μ^2 (or μ) with X are often called dispersion curves. The simplest dispersion curve is that representing (2.78) and is shown in figure 2.8. This curve can be interpreted in terms of ionospheric propagation as follows:

Imagine a radio wave incident normally on a plane stratified ionosphere; at the bottom of the ionosphere (N=0) μ is unity. As we penetrate into levels of higher and higher electron concentration, μ falls lower and lower. If the electron density is sufficiently high, then μ will go to zero. To find what happens when μ reaches zero we apply Snell's law to the wave. Snell's law states that for a wave incident at an angle ϕ_0 to the normal, the angle ϕ with the normal at a level where the refractive index is μ is given by

$$\mu \sin \phi = \mu_0 \sin \phi_0. \tag{2.79}$$

Now $\mu_0 = 1$ outside the ionosphere and at reflection ϕ must be 90° so that the refractive index at reflection μ_r must be equal to $\sin \phi_0$. With normal incidence $(\phi_0 = 0)$ the condition of reflection becomes $\mu_r = 0$. Thus we see that if the electron density is sufficiently large to reduce μ to zero then a wave (incident normally) will be reflected. Otherwise the wave will penetrate through the layer.

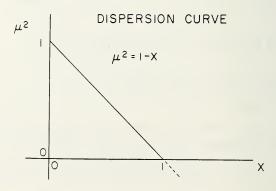


FIGURE 2.8. Dispersion curve (no field, no collisions).

2.3.3.2. Magnetic Field, No Collisions

Dispersion. For a more complete discussion of the properties of the refractive index formula, the reader should consult the excellent books by J. A. Ratcliffe [10], K. G. Budden [11], and J. M. Kelso [17]. However, we shall derive some formulas which will be needed in future chapters.

First consider the case of the reflection of a wave, of frequency f, incident normally in an ionospheric layer. Putting $\mu = 0$ in (2.77) and solving for X we obtain the following:

With
$$+ \text{ sign } X = 1$$
 (2.80)

With
$$-$$
 sign $X=1-Y$, (a)

or

$$X = 1 + Y.$$
 (b) (2.81)

where

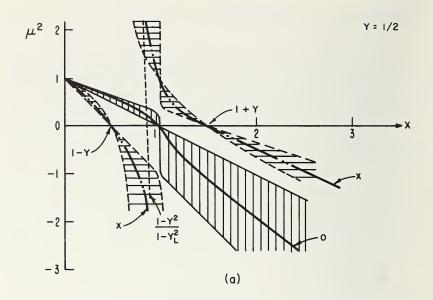
$$Y^2 = Y_T^2 + Y_L^2$$
. (c)

Equation (2.80) tells us that, for one of the magneto-ionic waves, the wave is reflected as in the absence of the magnetic field. This wave is called the "ordinary" wave. Equations (2.81) show that the level of reflection of the other magneto-ionic wave (called the extraordinary) is dependent on the strength, but not on the direction, of the imposed magnetic field. For waves of frequency greater than the gyrofrequency (f_H) the usual level of reflection is given by X=1-Y whereas on frequencies below f_H (so that Y>1) the condition is X=1+Y.

The dispersion curves corresponding to (2.77) are shown in figures 2.9a and b for values of $Y=\frac{1}{2}$ and Y=2, respectively, and for $\theta \approx 45^{\circ}$ together with the limiting cases of longitudinal and transverse propagation. Note that these curves are not drawn to scale but are intended merely to illustrate the general shapes.

Approximate formulas. Even in the absence of electronic collisions, the refractive index formula (2.77) is complicated. There are certain practical conditions under which considerably simpler approximations are useful. Although, with the advent of electronic computers, the necessity for using approximations in numerical work has decreased, there is still some need for them in practical work and, furthermore, they are widely used to simplify theoretical discussion.

The usual rules for determining whether the quasi-transverse (QT) or the quasi-longitudinal (QL) approximations hold are,



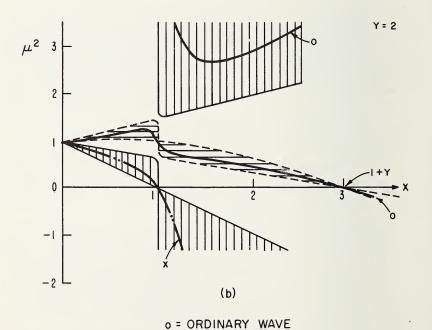


FIGURE 2.9. Dispersion curves for the general direction of propagation.

x = EXTRAORDINARY WAVE

Cross-hatched areas represent the limits between transverse and longitudinal propagation. Curves shown are for $\theta \approx 45^{\circ}$. Vertical cross-hatch represents the + sign and the horizontal cross-hatch represents the - sign.

$$\begin{array}{cccc} \text{QT} & Y_T^4 \gg 4(1-X)^2 Y_L^2, & \text{(a)} \\ \\ \text{QL} & Y_T^4 \ll 4(1-X)^2 Y_L^2. & \text{(b)} \end{array} \tag{2.82}$$

It is important to notice that these conditions do not depend on the value of θ only. Thus QT may hold either for $\theta \approx 90^{\circ}$ or for $X \approx 1$ which is the value of X near the level of reflection (with normal incidence) of the o-wave in almost all magnetic latitudes. Similarly the QL condition is good for the extraordinary wave, near its level of reflection (normal incidence) at almost all magnetic latitudes. Davies and King [12] have discussed the usefulness of the following approximations in the case of the magnetic dipole field and vertical propagation. Ordinary wave:

QT:
$$\frac{X}{1-\mu_1^2} = 1, \qquad (a)$$

$$\frac{X}{1-\mu_2^2} = 1 - (1-X) \cot^2 \theta, \qquad (b)$$

QL:
$$\frac{X}{1-\mu_3^2} = 1 + |Y_L|$$
. (2.84)

Extraordinary wave:

QT:
$$\frac{X}{1-\mu_4^2} = 1 - \frac{Y^2}{1-X}$$
, (2.85)

QL:
$$\frac{X}{1-\mu_{5}^{2}} = 1 - |Y|, \qquad (a)$$

$$\frac{X}{1-\mu_{6}^{2}} = 1 - |Y_{L}|. \qquad (b)$$

Care must be taken when using these approximations, as the range of validity may be very small. This is illustrated in figures 2.10a and b. Note that the extraordinary wave curves are plotted in terms of the parameter $\xi^2 = f^2(1-Y) = f^2 - ff_H$.

The following are suitable formulas for the refractive indices near the levels of reflection with normal incidence. For the ordinary wave

$$\mu_{+} = (1 - \frac{1}{2}\epsilon \cot^{2}\theta) \csc^{2}\theta, \qquad (2.87)$$

where $\epsilon = 1 - X$, and for the extraordinary wave we have

$$\mu_{-} = \sqrt{\frac{2\epsilon_{1}}{(1 - Y)(1 + \cos^{2}\theta)}} \left[1 - \frac{\epsilon_{1} \tan^{2}\theta}{4(1 - Y)(1 + \sec^{2}\theta)} \left(\frac{3 + \sec^{2}\theta}{Y} + \tan^{2}\theta \right) \right],$$
(2.88)

where $\epsilon_1 = 1 - Y - X$.

For further details the reader is referred to Budden [11, Ch. 12). Note that if Y is replaced by -Y in (2.88) the refractive index is that when X approaches 1+Y.

Other approximations of interest are those applicable to audio frequency waves (the whistler mode). When $X\gg Y\gg 1$ and $|Y_L|>1$, Storey [13] has shown that the + sign in (2.77) reduces to the following approximations for a wide range of θ , not too near 90°:

$$\mu^2 = 1 + \left| \frac{X}{Y_L} \right|, \qquad \text{(a)}$$
 or approximately $\mu^2 = \left| \frac{X}{Y_L} \right|. \qquad \text{(b)}$

Wave polarization. One other aspect of the Appleton formula which is of interest is the wave polarization R given by (2.74). This gives the amplitude ratio and the phase difference between the oscillations of the D, E, and P vectors along the 2- and 3-axes. In general, the tips of these vectors describe ellipses. The D ellipse is similar in shape to the projections of the E and P ellipses on to the 2-3 plane and the sense of rotation is the same. The H ellipse is similar to the D ellipse (and lies wholly in

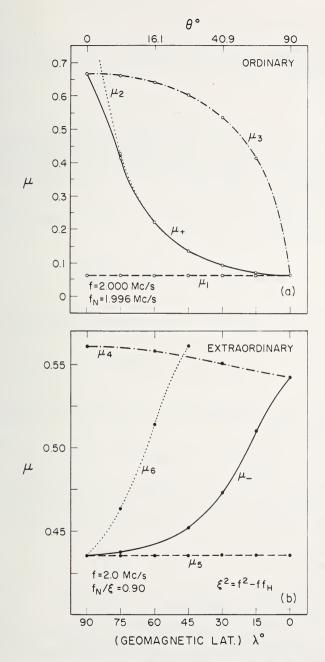


Figure 2.10. Refractive index curves under quasi-longitudinal and quasi-transverse conditions.

Vertical propagation, dipole magnetic field. (a) ordinary wave; (b) extra ordinary wave. The indices μ_+ and μ_- are from (2.77).

the 2-3 plane) but is rotated through 90° as shown in figure 2.11a and the sense of rotation is the same.

The relationship between the ordinary wave ellipses and the extraordinary wave ellipses can be deduced from (2.74), from which it follows that

$$R(-)R(+) = 1.$$
 (2.90)

Hence, in the absence of collisions, the ellipse of the extraordinary wave can be obtained from the corresponding ellipse of the ordinary wave by rotating it through 90°. Furthermore, the sense of rotation is reversed as shown in figure 2.11b.

While the vectors **D**, **B**, and **H** lie in the plane of the wavefront (2-3 plane), the **P** and **E** ellipses are tilted forward making angles ϕ and ψ respectively with the 2-3 plane where

$$\cot \phi = \frac{P_2}{P_1} = \frac{Y_T}{2Y_L} \mp \sqrt{\frac{Y_T^2}{4Y_L^2} + \frac{(1-X)^2}{Y_T^2}},$$
 (2.91)

where the + and - signs refer to the corresponding signs in (2.77), and where

$$\tan \psi = \frac{E_1}{E_2} = i \frac{(1 - \mu^2) R Y_T}{1 - X}.$$
 (2.92)

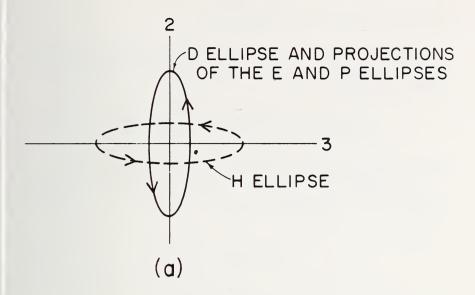
From these equations we see that the forward tilt is different for the two magneto-ionic waves.

It can be shown from (2.91) and (2.92) that, for waves incident normally on the ionosphere, at reflection

- (i) the E and P vectors of the ordinary wave vibrate linearly in the direction of the imposed magnetic field, since $\cot \phi = \tan \theta = \cot \psi$.
- (ii) the E and P ellipses of the extraordinary wave are perpendicular to the imposed magnetic field, since $\phi = \psi = -\theta$.

The following properties are of interest:

- (1) With longitudinal propagation the two magneto-ionic waves are circularly polarized, in opposite senses.
- (2) With transverse propagation the ordinary wave is polarized with the E and P vectors parallel to the imposed magnetic field, whereas for the extraordinary wave the P and E ellipses lie entirely in the 1-3 plane.



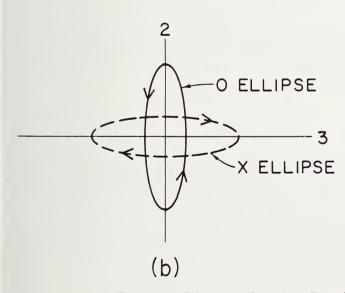


FIGURE 2.11. Polarization ellipses (no collisions).

(a) Wave polarization D and H ellipses. (b) Relation between the corresponding ellipses of the ordinary and the extraordinary waves.

2.3.3.3. No Magnetic Field, With Collisions

Meaning of a complex index. For the sake of simplicity we now set $Y_T = Y_L = 0$, but retain Z, in (2.76). This yields a complex refractive index n given by

$$n^{2} = (\mu - i\chi)^{2} = 1 - \frac{X}{1 - iZ} = 1 - \frac{X}{1 + Z^{2}} - \frac{iXZ}{1 + Z^{2}}, \qquad (2.93)$$

where μ and χ are the real and imaginary parts of n respectively.

Let us pause for a moment to consider the meaning of a complex refractive index. The equation for a wave traveling in the 1-direction is of the form (see 2.36)

$$E = E_0 \exp i \left(\omega t - \frac{\omega}{c} n x_1 \right), \tag{2.94}$$

or

$$E = E_0 \exp\left(\frac{\omega}{c} x_1\right) \exp i\left(\omega t - \frac{\omega}{c} \mu x_1\right). \tag{2.95}$$

Thus, if χ is non-zero, this represents a wave whose amplitude is decreasing exponentially with distance. The quantity $(\omega/c)\chi$ is a measure of the decay of amplitude per unit distance and is called the absorption coefficient κ (kappa).

$$\kappa = -\frac{\omega}{c}\chi. \tag{2.96}$$

Dispersion. Consider first the real part of the refractive index. The variation of μ^2 with X, for a series of values of Z, is shown in figure 2.12. It will be seen that, for a given value of X, the effect of a large collision frequency is to diminish the refracting properties of the medium. It is important to notice also that, when collisions are present, the real part of the refractive index never goes to zero but attains a minimum value given by

$$\mu_m^2 = 1 - \frac{1}{(1+Z^2)} \,, \tag{2.97}$$

at X=2.

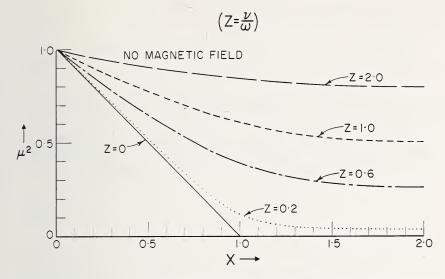


Figure 2.12. Variation of refractive index μ with X for different collision frequencies (no magnetic field), $Z = \nu/\omega$.

This means that in a lossy medium total reflection never really occurs. However, strong reflections still occur near levels at which μ is small.

Absorption. We shall return now to the absorption of the radio wave. From (2.93) and (2.96) we get

$$\kappa = \frac{\omega}{c} \frac{1}{2\mu} \frac{XZ}{1 + Z^2} = \frac{e^2}{2\epsilon_0 mc} \frac{1}{\mu} \frac{N\nu}{\omega^2 + \nu^2}.$$
 (2.98)

This formula gives the absorption in nepers per meter, where 1 neper = 8.69 dB.

Equation (2.98) enables us to distinguish between two extreme types of absorption, namely:

Non-deviative absorption occurs in the D region of the ionosphere; it predominates when μ is near unity and when the product N_{ν} is large.

Deviation absorption occurs near the level of reflection and whenever there is marked bending of the ray, that is, when μ tends to zero. For non-deviative absorption we have, when ω is much greater than ν ,

$$\kappa \approx \frac{e^2}{2\epsilon_0 mc} \frac{N_{\nu}}{\omega^2}, \qquad (2.99)$$

so that the absorption varies inversely as the square of the frequency. For deviative absorption we have

$$\kappa = \frac{\nu}{2c} \left(\frac{1}{\mu} - \mu \right). \tag{2.100}$$

Note that this type of absorption does not, in general, vary inversely as the square of the frequency.

Let us consider now the case when the angular wave frequency is small compared with the collision frequency (i.e., $\omega^2 \ll \nu^2$). With this condition we have from (2.98) for non-deviative absorption

$$\kappa \approx \frac{e^2}{2\epsilon_{omc}} \frac{N}{\nu}$$
. (2.101)

Under these conditions, the absorption may actually decrease with increase of collision frequency. The physical reason for this appears to be that the electronic motions are so confined that little energy is extracted from the wave. Absorption of this type is thought to occur during some polar cap absorption events and certain solar flare effects.

It is of interest to note that differentiation of (2.98) (for $\mu \approx 1$) shows that a maximum of absorption occurs when $\nu = \omega$.

2.3.3.4. Magnetic Field, With Collisions

Dispersion. With one exception, the inclusion of a magnetic field and collisions introduces great complication into the dispersion and absorption relationships. The one exception is that of transverse propagation of the ordinary wave which is the same as the "no field" case.

The dispersion curves for the general case of any angle of propagation are discussed usually in terms of the so-called critical collision frequency ν_c where

$$\frac{\nu_c}{\omega} = \frac{1}{2} \frac{Y_T^2}{Y_L} = \frac{Y}{2} \frac{\sin^2 \theta}{\cos \theta}. \tag{2.102}$$

The curves are sketched in figure 2.13 and show how profound are the effects of collisions (in comparison with figure 2.9), especially near X=1. Collisions play an important part in modifying the QT and QL conditions. Thus QL conditions may hold even near X=1 for the ordinary wave

DISPERSION CURVES WITH COLLISIONS

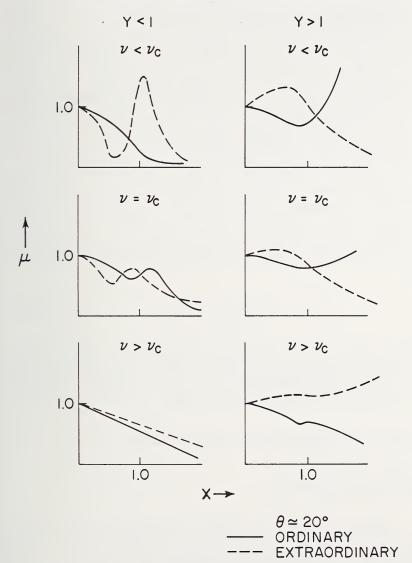


Figure 2.13. Dispersion curves with magnetic field and collisions for a fixed $\theta = 20^{\circ}$.

whereas QT conditions may apply near $X=1\mp Y$ for the X-wave. The interested reader can find more information on this in Mr. Ratcliffe's book [10].

Polarization. As far as polarization is concerned, the introduction of collisions causes the polarization ellipses (in the 2-3 plane) to rotate about the 1-axis. All the ellipses associated with one magneto-ionic wave rotate in the same direction and through the same angle as shown in figure 2.14a. The ellipses associated with the other wave rotate in the opposite direction through the same angle (figure 2.14b). Hence, for the projections of the ellipses onto the wavefront, we may deduce the ellipses of one magneto-ionic wave from that of the other as follows: Rotate the ellipse through 90° about the direction of phase propagation and then reflect in the magnetic meridian. It may be noted that one ellipse is the reflection of the other in the plane making an angle of 45° with the magnetic meridian.

Absorption. In principle it is possible to express the complex refractive index in terms of its real and imaginary parts and thus to obtain the absorption. In practice the expressions which would be obtained by this procedure are so complex as to be of little or no value. For a variety of conditions, however, the propagation conditions are quasi-longitudinal and the non-deviative absorption coefficient is then given, approximately, by

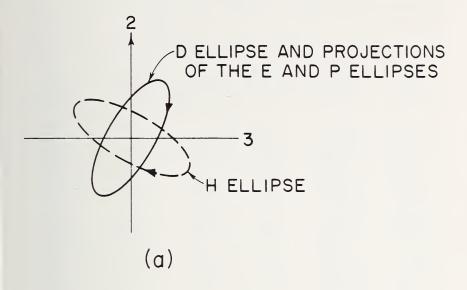
$$\kappa \approx \frac{e^2}{2\epsilon_0 mc} \frac{N_{\nu}}{(\omega \pm \omega_H)^2 + \nu^2}. \tag{2.103}$$

The + and - signs refer to the ordinary and extraordinary waves respectively. From this we see that the ordinary wave suffers less absorption, and the extraordinary suffers more absorption, than the corresponding wave in the absence of a magnetic field.

2.3.4. Generalized Magneto-Ionic Formulas

2.3.4.1. Collision Statistics

In our derivation of the Appleton formula it was assumed that the electrons all possessed the same average velocity and that the collision frequency ν was independent of the electron velocity. Now the question of finding an "average" velocity while not important in the upper regions of the ionosphere, where ν is small, is of considerable importance in the D region where ν may be equal to or greater than the angular wave



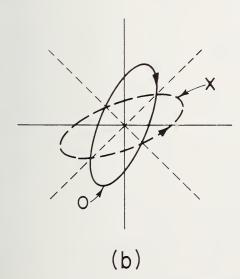


FIGURE 2.14. Polarization ellipses with collisions.

(a) Polarization D and H ellipses. (b) Relation between the corresponding ellipses of ordinary and extraordinary waves.

frequency. The method of averaging collisions is indeed the weakest point in the theory developed above, and to improve upon the above theory it is necessary to consider the energy distribution of the electrons and the dependence of collision frequency on electron energy. Thus a few

Table 2.1. Table of $\mathfrak{S}_p(x) = \frac{1}{p!} \int_0^\infty \frac{\epsilon^p \epsilon^{-\epsilon} d\epsilon}{\epsilon^2 + x^2}$

| | | | - 0 | | |
|--------------------------------------|---|---|--------------------------------------|--|--|
| <i>p</i> | 3/2 | 5/2 | <i>p</i> | 3/2 | 5/2 |
| 0.00 | 1.333 | $\begin{array}{c} 0.2667 \\ 0.2615 \\ 0.2542 \\ 0.2463 \\ 0.2384 \end{array}$ | 3.00 | 0.07034 | 0.05454 |
| 0.05 | 0.9744 | | 3.20 | 0.06404 | 0.05044 |
| 0.10 | 0.8425 | | 3.40 | 0.05854 | 0.04677 |
| 0.15 | 0.7502 | | 3.60 | 0.05369 | 0.04347 |
| 0.20 | 0.6786 | | 3.80 | 0.04941 | 0.04048 |
| 0.25 0.30 0.35 0.40 0.45 | 0.6202 0.5710 0.5289 0.4922 0.4598 | $\begin{array}{c} 0.2306 \\ 0.2230 \\ 0.2156 \\ 0.2085 \\ 0.2017 \end{array}$ | 4.00 4.20 4.40 4.60 4.80 | $\begin{array}{c} 0.04562 \\ 0.04223 \\ 0.03920 \\ 0.03647 \\ 0.03402 \end{array}$ | 0.03778 0.03533 0.03311 0.03107 0.02921 |
| 0.50 0.55 0.60 0.65 0.70 | $\begin{array}{c} 0.4310 \\ 0.4052 \\ 0.3818 \\ 0.3607 \\ 0.3414 \end{array}$ | 0.1951 0.1889 0.1828 0.1771 0.1715 | 5.00 5.20 5.40 5.60 5.80 | $\begin{array}{c} 0.03179 \\ 0.02978 \\ 0.02794 \\ 0.02627 \\ 0.02474 \end{array}$ | $\begin{array}{c} 0.02751 \\ 0.02594 \\ 0.02450 \\ 0.02317 \\ 0.02195 \end{array}$ |
| 0.75 | 0.3237 | 0.1662 | 6.00 | 0.02333 | 0.02081 |
| 0.80 | 0.3075 | 0.1611 | 6.20 | 0.02204 | 0.01976 |
| 0.85 | 0.2926 | 0.1563 | 6.40 | 0.02085 | 0.01878 |
| 0.90 | 0.2787 | 0.1516 | 6.60 | 0.01976 | 0.01787 |
| 0.95 | 0.2659 | 0.1471 | 6.80 | 0.01874 | 0.01702 |
| 1.00 | 0.2540 | 0.1428 | 7.00 | 0.01780 | 0.01623 |
| 1.10 | 0.2325 | 0.1347 | 7.20 | 0.01693 | 0.01549 |
| 1.20 | 0.2137 | 0.1273 | 7.40 | 0.01612 | 0.01480 |
| 1.30 | 0.1971 | 0.1204 | 7.60 | 0.01536 | 0.01415 |
| 1.40 | 0.1824 | 0.1140 | 7.80 | 0.01466 | 0.01355 |
| 1.50 | 0.1693 | 0.1081 | 8.00 | 0.01400 | 0.01298 |
| 1.60 | 0.1576 | 0.1026 | 8.20 | 0.01339 | 0.01244 |
| 1.70 | 0.1471 | 0.09750 | 8.40 | 0.01281 | 0.01194 |
| 1.80 | 0.1376 | 0.09275 | 8.60 | 0.01227 | 0.01146 |
| 1.90 | 0.1289 | 0.08831 | 8.80 | 0.01176 | 0.01101 |
| 2.00 | 0.1211 | 0.08417 | 9.00 | 0.01128 | 0.01059 |
| 2.10 | 0.1139 | 0.08030 | 9.20 | 0.01084 | 0.01019 |
| 2.20 | 0.1073 | 0.07668 | 9.40 | 0.01041 | 0.009811 |
| 2.30 | 0.1013 | 0.07328 | 9.60 | 0.01001 | 0.009453 |
| 2.40 | 0.09580 | 0.07009 | 9.80 | 0.009635 | 0.009114 |
| 2.50 | 0.09070 | 0.06710 | 10.00 | 0.009278 | 0.008792 |
| 2.60 | 0.08599 | 0.06428 | 10.50 | 0.008468 | 0.008059 |
| 2.70 | 0.08164 | 0.06163 | 11.00 | 0.007758 | 0.007408 |
| 2.80 | 0.07759 | 0.05913 | 11.50 | 0.007132 | 0.006833 |
| 2.90 | 0.07384 | 0.05677 | 12.00 | 0.006578 | 0.006321 |

Table 2.1—Continued

| <i>p</i> | 3/2 | 5/2 | <i>p</i> | 3/2 | 5/2 |
|---|---|---|---|---|--|
| 12.50 13.00 13.50 14.00 14.50 | 0.006086 0.005647 0.005252 0.004898 0.004578 | 0.005864 0.005453 0.005084 0.004750 0.004448 | 28.00 29.00 30.00 32.00 34.00 | 0.001262 0.001177 0.001101 0.0009684 0.0008586 | 0.001251 0.001168 0.001092 0.0009620 0.0008536 |
| 15.00 15.50 16.00 16.50 17.00 | $\begin{array}{c} 0.004287 \\ 0.004024 \\ 0.003784 \\ 0.003564 \\ 0.003363 \end{array}$ | $\begin{array}{c} 0.004173 \\ 0.003922 \\ 0.003693 \\ 0.003484 \\ 0.003291 \end{array}$ | 36.00 38.00 40.00 42.00 44.00 | $ \begin{array}{c} 0.0007665 \\ 0.0006884 \\ 0.0006216 \\ 0.0005641 \\ 0.0005142 \end{array} $ | $\begin{array}{c} 0.0007625 \\ 0.0006851 \\ 0.0006190 \\ 0.0005619 \\ 0.0005124 \end{array}$ |
| 17.50 18.00 18.50 19.00 19.50 | 0.003179 0.003009 0.002852 0.002707 0.002573 | 0.003114 0.002950 0.002799 0.002660 0.002530 | 46.00 48.00 50.00 55.00 60.00 | $ \begin{array}{c} 0.0004707 \\ 0.0004324 \\ 0.0003986 \\ 0.0003296 \\ 0.0002771 \end{array} $ | $\begin{array}{c} 0.0004691 \\ 0.0004311 \\ 0.0003975 \\ 0.0003289 \\ 0.0002766 \end{array}$ |
| 20.00 21.00 22.00 23.00 24.00 | 0.002448 0.002225 0.002031 0.001860 0.001711 | $\begin{array}{c} 0.002409 \\ 0.002192 \\ 0.002003 \\ 0.001837 \\ 0.001691 \end{array}$ | 65.00 70.00 75.00 80.00 85.00 | $\begin{array}{c} 0.0002362 \\ 0.0002037 \\ 0.0001775 \\ 0.0001560 \\ 0.0001382 \end{array}$ | $\begin{array}{c} 0.0002358 \\ 0.0002034 \\ 0.0001773 \\ 0.0001559 \\ 0.0001381 \end{array}$ |
| 25.00 26.00 27.00 | $\begin{array}{c} 0.001578 \\ 0.001461 \\ 0.001356 \end{array}$ | $\begin{array}{c} 0.001562 \\ 0.001446 \\ 0.001343 \end{array}$ | 90.00 95.00 100.00 | 0.0001233 0.0001107 0.0000999 | $\begin{array}{c} 0.0001232 \\ 0.0001106 \\ 0.0000998 \end{array}$ |

electrons with high energy may lose as much energy as a large number of electrons with low energy.

Little was known about the energy dependence of ν until Phelps and Pack [14] and Phelps [8] established, experimentally, that for slow electrons in nitrogen, the frequency of collisions for momentum transfer was directly proportional to electron energy.

Margenau [15] has shown that, to include the distribution of electron energies, it is necessary to use the Boltzmann transfer equation. This theory has been extended to the case of a magneto-ionic medium by Sen and Wyller [9] but their development is beyond the scope of this book. We shall, however, consider their results in the important case where there is no imposed magnetic field. This case applies also to transverse propagation of the ordinary wave. With a Maxwellian velocity distribution and with a collision frequency which varies linearly with electron energy, the complex refractive index is given by the expression

$$n^{2} = (\mu - i\chi)^{2} = 1 - \frac{X}{Z_{m}^{2}} \mathcal{C}_{3/2} \left(\frac{1}{Z_{m}}\right) - i\frac{5}{2} \frac{X}{Z_{m}} \mathcal{C}_{5/2} \left(\frac{1}{Z_{m}}\right), \qquad (2.104)$$

in which $Z_m = \nu_m/\omega$. Here ν_m is the electron collision frequency associated with the most probable energy rather than with the mean energy.

$$\mathfrak{C}_{p}(x) = \frac{1}{p!} \int_{0}^{\infty} \frac{\epsilon^{p} \exp((-\epsilon)) d\epsilon}{\epsilon^{2} + x^{2}}.$$
 (2.105)

The values of $\mathcal{C}_{3/2}(x)$ and $\mathcal{C}_{5/2}(x)$ given in table 2.1 are taken from Burke and Hara [16] and are published by permission of the Superintendent, Defence Research Telecommunications Establishment, Ottawa, Canada.

2.3.4.2. Dispersion

For the sake of simplicity let us consider the case where the absorption is relatively small so that $\chi^2 \ll \mu^2$. Under this condition we have

$$\mu^{2} = 1 - \frac{X}{Z_{m}^{2}} \mathcal{C}_{3/2} \left(\frac{1}{Z_{m}}\right), \qquad (a)$$
or $\mu^{2} = 1 - \frac{\omega_{N}^{2}}{\nu_{m}^{2}} \mathcal{C}_{3/2} \left(\frac{\omega}{\nu_{m}}\right). \qquad (b)$
(2.106)

From (2.105) it can be seen that when x is small, i.e., when $\nu_m \gg \omega$, $\mathfrak{C}_{3/2}(0) = \frac{4}{3}$. Substitution of this value into (2.106) gives $\mu^2 = 1 - (\omega_N^2/\nu^2)$ which is similar to (2.97) with $Z \gg 1$. Thus it is possible to use the classical formula provided that $\nu = (\sqrt{3}/2)\nu_m$. When x is large, i.e., when $\omega \gg \nu_m$, (2.106) reduces to (2.78).

2.3.4.3. Absorption

The non-deviative absorption per unit length $(\chi^2 \ll \mu^2)$ is obtained from the imaginary part of (2.104), namely

$$\kappa = \frac{5}{2} \frac{\omega}{c} \frac{1}{2\mu} \frac{X}{Z_m} \mathcal{C}_{5/2} \left(\frac{1}{Z_m}\right), \qquad (a)$$
or $\kappa = \frac{5}{4c} \frac{1}{\mu} \frac{\omega_N^2}{\nu_m} \mathcal{C}_{5/2} \left(\frac{\omega}{\nu_m}\right).$ (b)

To see how the absorption from the generalized theory compares with that from the Appleton equation, we need to compare the following function:

$$\kappa_G = \frac{5}{2} \frac{1}{\nu_m} \mathcal{C}_{5/2} \left(\frac{\omega}{\nu_m} \right), \tag{2.108}$$

with

$$\kappa_A = \frac{\nu}{\omega^2 + \nu^2} \,. \tag{2.109}$$

This comparison is made in figure 2.15. As in the case of the dispersion curves, it is not possible to use a single effective collision frequency $\nu_{\rm eff}$ across the entire frequency band. Nevertheless, on high frequencies the Appleton theory can be used with $\nu_{\rm eff} = 2.5 \ \nu_m$, whereas on low frequencies it is necessary to use $\nu_{\rm eff} = 1.5 \ \nu_m$. It must be realized, however, that on intermediate frequencies appreciable error is involved in using one or the other of these values of $\nu_{\rm eff}$.

2.4. GROUP PROPAGATION

2.4.1. Phase Velocity

From (2.78) it follows that the phase velocity (v) of a wave in a plasma containing no imposed magnetic field and in which electronic collisions are negligible is given by

$$v = \frac{c}{\mu} = c \left[1 - \frac{Ne^2}{m\epsilon_0 \omega^2} \right]^{-\frac{1}{2}}.$$
 (2.110)

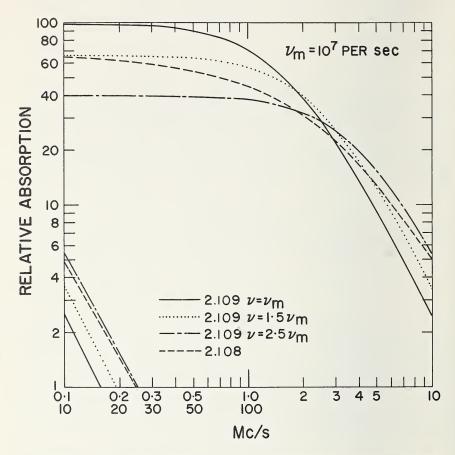


Figure 2.15. Comparison of absorption curves of Appleton theory and of generalized theory.

This indicates that the phase velocity, in the medium, is greater than that of light. It might be thought, at first sight, that this is a violation of the special theory of relativity. However, this is not so; all it means is that the wavelength (i.e., the distance between one wave crest and the next) is greater in the medium than in free space. It does not mean that energy is propagated faster than light.

The relationships between phase velocity (v), wavelength λ , and refractive index μ are given by

$$v\mu = c$$
, (a) (2.111) and $\frac{v}{\lambda} = \frac{c}{\lambda_0}$, (b)

where λ_0 is the free space wavelength.

2.4.2. Group Velocity

When the phase velocity of a wave in a medium is a function of the wave frequency, the medium is said to be "dispersive." This term arose in the dispersion of colors by a prism. Inspection of (2.110) reveals that, for radio waves, the ionosphere is dispersive. This means that two waves differing slightly in frequency will travel with slightly different velocities. It is the interference pattern produced by two such waves that determines where, and with what velocity, the energy in the composite wave will travel. This is what happens when we modulate a wave and it introduces the concept of "group velocity" which, for our present purposes, may be regarded as the velocity with which the modulation envelope travels or the velocity of the energy. It should be realized that this concept is applicable only when the modulation envelope retains its shape. It is not applicable under conditions of severe distortion as can occur in highly dispersive media. For a more detailed discussion of this subject the reader should consult Stratton [4, sec. 5.17].

For our present purpose it will suffice to consider the superposition of two harmonic waves ψ_1 and ψ_2 of equal amplitude which differ slightly in frequency and wave number.

$$\psi_1 = \cos(kx_1 - \omega t), \tag{a}$$

$$\psi_2 = \cos\{(k+\delta k)x_1 - (\omega + \delta \omega)t\},\tag{b}$$

$$\psi = \psi_1 + \psi_2 = 2 \cos \frac{1}{2} (x_1 \delta k - t \delta \omega) \cos \left[\left(k + \frac{\delta k}{2} \right) x_1 - \left(\omega + \frac{\delta \omega}{2} \right) t \right].$$
 (c)

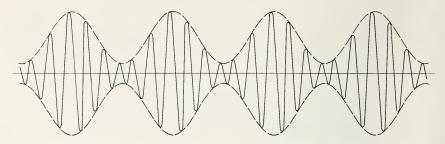


FIGURE 2.16. Interference pattern produced by two waves of equal amplitudes and slightly different frequencies.

This is shown diagrammatically in figure 2.16. The superposition produces a "beat" signal, the envelope of which is given by

$$A = 2 \cos \frac{1}{2} (x_1 \, \delta k - t \, \delta \omega). \tag{2.113}$$

It follows from (2.113) that the velocity of propagation of the envelope (i.e., the group velocity u) is given by

$$u = \frac{\delta\omega}{\delta k} \,. \tag{2.114}$$

This contrasts with the phase velocity v given by

$$v = \frac{\omega}{k} \,. \tag{2.115}$$

For a non-dispersive medium, in which ω/k is constant, u=v. In the limit as $\delta\omega\to 0$ and $\delta k\to 0$ we obtain the differential form

$$u = \left(\frac{d\omega}{dk}\right)_{k_0},\tag{2.116}$$

where k_0 is the value of k at which the gradient $(d\omega/dk)$ is evaluated.

It is convenient to define a group refractive index μ' in a manner similar to a phase index namely,

$$\mu' = \frac{c}{u} = c\frac{dk}{d\omega} = c\frac{d}{d\omega} \left(\frac{2\pi}{\lambda}\right) = \frac{d}{d\omega}(\mu\omega) = \mu + \omega\frac{d\mu}{d\omega} = \mu + f\frac{d\mu}{df}. \quad (2.117)$$

It is important to remember that the group velocity as defined above is the component in the direction of phase propagation. Furthermore, under normal dispersion conditions, its magnitude is always less than the velocity of light. Substituting $\mu = \sqrt{1 - (f_N/f)^2}$ in (2.117) we find that

$$\mu' = \frac{d}{df}(\mu f) = \frac{1}{\mu}. \tag{2.118}$$

In the presence of an imposed magnetic field the group refractive index $\mu'(\pm)$ is given by substituting the expression for μ from (2.77) in (2.117). This gives

$$\mu'(\pm) = \mu(\pm) + \{(1-\mu^2(\pm))\}^2$$

$$\times \left[\frac{1}{X\mu(\pm)} + \frac{Y_T^2}{2\mu(\pm)(1-X)^2} \pm \frac{2(1-X)^3 Y_L^2 - X Y_T^4}{2X\mu(\pm)(1-X)^2 \sqrt{Y_T^4 + 4 Y_L^2(1-X)^2}} \right], \tag{2.119}$$

where the + and - signs refer to the ordinary and extraordinary waves respectively. The more complete expression, involving collisions, is given by Budden [11, ch. 12].

2.5. PROPAGATION IN ANISOTROPIC MEDIA

2.5.1. Meaning of Anisotropy

A homogeneous medium is said to be isotropic if the phase velocity at any given point in the medium is independent of the direction of propagation. A two-dimensional illustration of this is seen in figure 2.17. Consider a disturbance, originating at the origin O; after a time t the wavefront will be a circle of radius r=vt. At a point P on the wave the wavefront is tangent to the circle and hence the wave normal n_p , which is perpendicular to the front, is radial. Now, since the disturbance is traveling out from O in all directions, it is not hard to see that the direction of energy flow (ray direction) is always radial. Hence, in an isotropic medium, the direction of phase propagation and of energy propagation coincide.

Now consider a magneto-ionic medium. Equation (2.77) shows that the refractive index μ depends upon Y_T and Y_L , that is, upon the direction

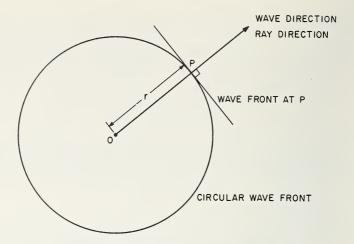


FIGURE 2.17. Wavefront in an isotropic medium.

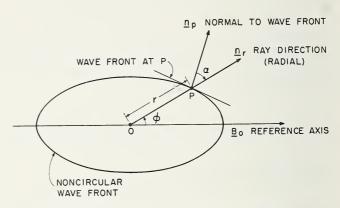


FIGURE 2.18. Wavefront in an anisotropic medium.

of phase propagation with respect to the magnetic field. A medium such as this, in which the phase velocity at a point is a function of direction, is said to be "anisotropic." Again consider a disturbance originating at a point O in such a medium as illustrated in figure 2.18. Since the phase velocity is a function of the angle ϕ made with the reference axis, the wavefront at a time t is not circular but shaped somewhat similar to that shown in figure 2.18. As before, the wavefront at a point P is tangential to the surface of constant phase and so the wave normal \mathbf{n}_p is no longer radial. Since the energy is radiating from the point O, the ray direction \mathbf{n}_r is still radial. Hence, in an anisotropic medium, the direction of phase propagation differs, in general, from that of energy propagation.

2.5.2. Angle Between Phase and Ray Directions

Let α be the angle measured from the wave normal n_p to the ray n_r , i.e., in same sense as θ , as shown in figure 2.18. Our next step is to find a relationship for α in terms of the refractive properties of the medium. Referring to the geometry in figure 2.19 we see that

$$\tan \alpha = -\frac{1}{r}\frac{dr}{d\phi}\,, \qquad (2.120)$$

and

$$\phi = \theta - \alpha. \tag{2.121}$$

It is now necessary to introduce the concept of ray velocity v_r . The distance OP = r, in figure 2.18, is proportional to the velocity of P in the ray direction \mathbf{n}_r , whereas the phase velocity v is measured in the direction of phase propagation \mathbf{n}_p . By letting the wavefront advance a short distance it can be seen that the relation between v and v_r is

$$v = v_r \cos \alpha. \tag{2.122}$$

Solution of (2.120), (2.121), and (2.122) gives

$$\tan \alpha = -\frac{1}{v}\frac{dv}{d\theta} = +\frac{1}{\mu}\frac{d\mu}{d\theta}.$$
 (2.123)

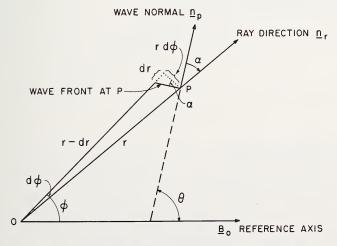


FIGURE 2.19. Derivation of formula $\tan \alpha = (1/\mu)(d\mu/d\theta)$.

The sign convention used here is important because some authors use (2.123) with a reversal of sign. The convention used here is that angles measured in the same direction as θ (i.e., from wave normal to magnetic field) are positive. It is important to remember also that in the above derivation of $\tan \alpha$, it was tacitly assumed that the medium was homogeneous, that is the wave velocity in a given direction is independent of position in the medium. Hence no distortion of the wavefront is brought about by variations in the medium due to position.

2.5.3. Phase and Group Paths

For some purposes, it is convenient to use the concepts of phase and group paths which may be defined with reference to the transit times of a surface of constant phase and of a wave packet, respectively, between a sender and a receiver. It must be remembered that these are not paths in space but are distances which would have been covered if the wave (and wave packet) had traveled with the free space velocity.

Referring to the ray path between sender S and receiver R in figure 2.20, the time dT_p required for a surface of constant phase (see fig. 2.20b) to travel from P to Q is given by

$$dT_p = \frac{PM}{v} = \frac{PQ}{v_r} = \frac{ds \cos \alpha}{v} = \frac{1}{c}\mu \cos \alpha \, ds. \tag{2.124}$$

The total transit time

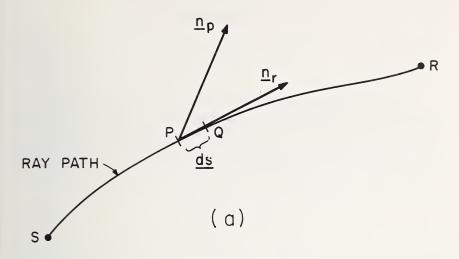
$$T_p = \frac{1}{c} \int_S^R \mu \cos \alpha \, ds = \frac{P}{c} \,, \tag{2.125}$$

where

$$P = \int_{s}^{R} \mu \cos \alpha \, ds, \qquad (2.126)$$

is defined as the phase path.

The quantity $K = (2\pi/\lambda_0)P$ is called the angular phase path length. It is simply the number of radians of phase between sender and receiver. If K changes with time, either because of a change of real distance and/or a change in refractive index, the angular frequency of the received wave will differ from that transmitted by an amount $\Delta\omega$. If K increases then the received frequency decreases because more radians are needed in the



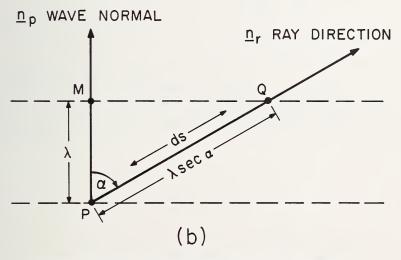


FIGURE 2.20. Phase and group paths in an anisotropic medium.

medium between S and R. Therefore the angular Doppler frequency $\Delta \omega$ is

$$\Delta\omega = -\frac{dK}{dt} = -\frac{2\pi}{\lambda_0} \frac{dP}{dt}.$$
 (2.127)

In terms of linear frequency the Doppler shift Δf is given by

$$\Delta f = -\frac{1}{\lambda_0} \frac{dP}{dt} = -\frac{f}{c} \frac{dP}{dt}. \qquad (2.128)$$

The group path P' may be defined in terms of the time of flight of a pulse. It will be recalled that in section 2.4.2 we defined the group velocity u in the direction of phase propagation. In an anisotropic medium the wave packet will, in general, have a velocity component parallel to the wavefront. The time dT_g for the packet to travel from P to Q (fig. 2.20) is given by

$$dT_g = \frac{ds \cos \alpha}{u}.$$
 (2.129)

The quantity $u \sec \alpha$ is called the *ray group velocity* and represents the velocity of the wave packet along the ray path.

The total time of flight between sender and receiver is:

$$T_g = \frac{1}{c} \int_{S}^{R} \mu' \cos \alpha \, ds = \frac{1}{c} P',$$
 (2.130)

where

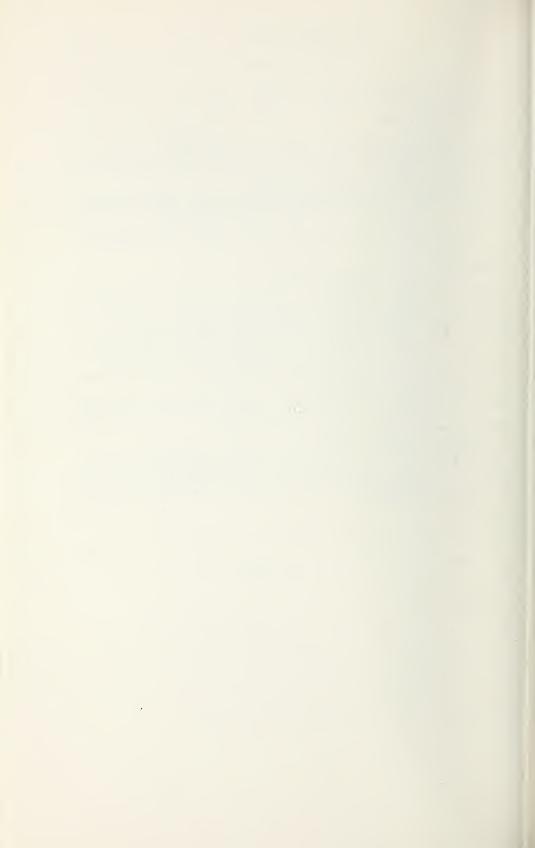
$$P' = \int_{S}^{R} \mu' \cos \alpha \, ds \tag{2.131}$$

is called the group path. Another useful relationship between these quantities is

$$T_{g} = \frac{d}{d\omega}(\omega T_{p}), \qquad (a)$$
or $P' = \frac{d}{d\omega}(\omega P).$ (b)

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CHAPTER 3

Synoptic Studies of the Ionosphere

3.1. WORLDWIDE SOUNDINGS

For purposes of radio communications, it is necessary to have information about the ionosphere on a global scale. Since the spatial and temporal fluctuations in the ionosphere are so great, geographic coverage may be much more important than accuracy of measurement. This point should be borne in mind whenever one is judging the value of ionospheric data. For instance, the lack of accuracy to which a critical frequency can be measured may make it of little value to the scientist, yet it may be of value to the radio operator.

Before World War II, there were only a few sounding stations in existence, e.g., Slough, England; Washington, D.C., U.S.A.; Huancayo, Peru; Watheroo, Australia; and Slutsk, U.S.S.R. The need for more reliable high-frequency communications led to the installation of many more stations during the war (40 or 50). During the International Geophysical Year (IGY) still more stations were added, making a total of about 150. The distribution of stations during the IGY is shown in figure 3.1. During this latter period considerable uniformity was introduced into the scaling and reporting of ionospheric data [1], which has turned out to be valuable from the point of view of both the radio communicator and the scientific worker.

Much of the impetus for ionospheric research has come from certain international organizations such as the International Scientific Radio Union (URSI) and the Consultative Committee on Ionospheric Radio (CCIR). These organizations have encouraged investigations into the spatial and temporal variations in the electron distribution in the ionosphere, the measurement of ionospheric absorption of radio waves, ionospheric movements, noise, and the scattering of radio waves from ionospheric irregularities.

¹ Figures in brackets indicate the literature references on p. 156.

IONOSPHERIC VERTICAL SOUNDING STATIONS

• = 1959 DATA IN WDC-A

= 1961 DATA IN WDC-A

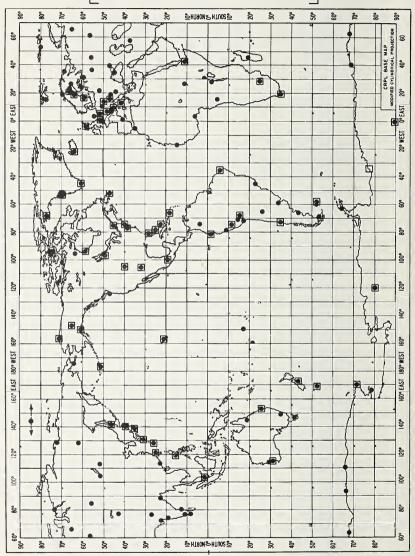


FIGURE 3.1. Map of world distribution of sounding stations.

In the present chapter, we shall consider some of the techniques used in ionospheric investigations and a few of the results obtained.

When making measurements on a medium such as the ionosphere it is necessary to distinguish clearly between controlled experiments, such as can be carried out in a laboratory, and those over which we have no control. Except for certain modeling techniques involving laboratory plasmas and microwaves, ionospheric research must be carried out in its own environment and, hence, any control must be "remote control."

3.2. EXPERIMENTAL TECHNIQUES

There are many possible ways of classifying radio techniques for investigating the ionosphere. For instance, we can divide them into pulse versus continuous wave (CW) techniques, or into fixed frequency versus sweep frequency, or again into intermittent versus continuous methods and so on. In the present treatment, we shall start by studying the most widely used technique (the ionosonde) and follow in order of decreasing usage, such as the techniques for measuring absorption, phase, etc. It is not to be construed that this order is in any sense one of relative importance.

3.2.1. Height Recorders

3.2.1.1. The lonosonde

The ionosonde is essentially a pulsed radar device in which the exploring frequency can be varied over a wide range from 1 Mc/s, say, up to 25 Mc/s. Of course the entire sweep may have to be covered in a series of frequency bands. A detailed description of ionosondes is given by Wright, Knecht, and Davies [2]. The equipment is designed to measure directly the time t taken for a pulse of radio waves to travel up to the ionosphere and back as a function of frequency. That is, it measures the group height h' of the ionosphere, where

$$h' = \frac{1}{2}ct = 0.15t, (3.1)$$

t being in microseconds. This group height is also known as equivalent height and virtual height. The transmitter and receiver are kept in tune by suitable electronic or mechanical linkage and the receiver output is

displayed on a cathode ray oscilloscope together with suitable frequency and time (height) markers. These signals are usually applied in the form of narrow blanking pulses which interrupt the sweep-trace every $\frac{1}{3}$, $\frac{2}{3}$ or $6\frac{2}{3}$ msec corresponding to group heights of 50, 100, and 1000 km, respectively. In addition, as the frequency of the transmitter is varied, the entire sweep-trace may be blanked for a short interval as the frequency passes through each megacycle (or 0.1 Mc/s). Thus a grid of reference lines is produced with which the group height at any frequency can be determined.

An ionosonde embodying these principles is the NBS C-4 Ionosonde. Essentially it consists of a pulse transmitter (of peak power about 10 kW) and a wide-band receiver as shown in the block diagram in figure 3.2. The pulse transmitter is composed of a heterodyning CW oscillator, sweeping from 31 to 55 Mc/s; a pulsed oscillator on a frequency of 30 Mc/s; a balanced mixer producing the difference frequency of the two (variable-frequency oscillator VFO and fixed-frequency oscillator FFO); and a power amplifier of the broadband video-coupled type. Note that the difference frequency varies by a factor of 25 to 1, although the sweeping oscillator variation is less than 2 to 1. The receiver uses the same heterodyning oscillator as the transmitter in another balanced mixer which converts the frequency of incoming echoes to 30 Mc/s. This frequency is constant throughout the band and is amplified and detected in a straightforward way. Antennas are usually vertical deltas or vertical rhombics which, although they possess fairly constant and resistive impedance, are not very efficient at the low frequency end of the sweep. Log periodic antennas, which are better in this respect, are coming into

A pulse generator provides pulses for triggering the transmitter and display, and employs a stable crystal at 1.0 Mc/s together with frequency-dividing circuits to obtain frequencies of 3 kc/s from which, by suitable shaping, the 50 km height markers are obtained. Further division to 1500 c/s and 300 c/s yields 100 km and 500 km markers respectively.

The frequency calibration marks are obtained as the receiver is tuned through the harmonics of the 1.0 Mc/s oscillator.

Various types of display are used:

A scan: This is illustrated in figure 3.3a. The time base of the cathode ray oscilloscope is synchronized with the pulse repetition frequency of the transmitter, and a stationary pulse pattern is obtained. The time base is applied to the x plates and the receiver output is applied to the y plates, together with the height marker pips. For photographic recording a screen is placed in front of the tube. The motion of the film past the slit provides the frequency base. As the frequency increases, the time delay

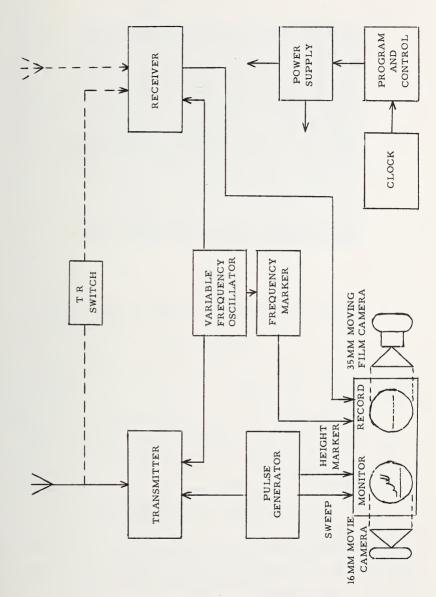
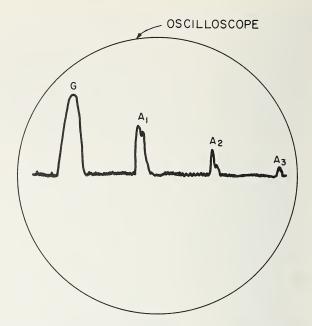


FIGURE 3.2. Block diagram of a typical ionosonde.



G=DIRECT PULSE, A₁, A₂, A₃ = ONCE, TWICE, THRICE REFLECTED SIGNALS

(a) A-SCAN

FIGURE 3.3a. Types of ionosonde display—A scan.

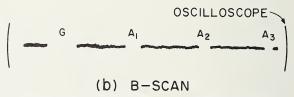
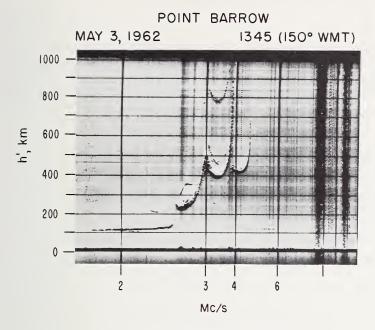


FIGURE 3.3b. Types of ionosonde display—B scan.

generally increases and the echo breaks in the time base move to the right. The cams controlling the frequency of the transmitter and receiver are suitably shaped so as to give the desired frequency scale on the film (e.g., linear or logarithmic).

B scan: This is similar to the A scan except that the receiver output and height pips are applied as blanking pulses to the oscilloscope and the γ plates are grounded. The output is as shown in figure 3.3b.



(C) PANORAMIC DISPLAY

FIGURE 3.3c. Types of ionosonde display-panoramic.

Panoramic displays: The B scan is used with the time base applied to the y plates and a voltage applied to the x plates which is a function of transmitter frequency. The whole h'-f picture is photographed on a single frame of 16 mm movie film as illustrated in figure 3.3c.

The ionosonde is a versatile equipment and, in one form or another, is used at every ionospheric observatory. It has the advantage that the quantity measured (virtual height) does not depend upon the output of the transmitter or the gain of the receiver, which means that it can be operated by relatively inexperienced operators. It is programmed, automatically, to make sweeps at certain intervals (e.g., every 15 min). The duration of a sweep depends on the mechanical design of the ionosonde but there are practical limits. If the sweep is too fast, the receiver is out of tune with the echo which has been reflected from the ionosphere. Sweeps of duration less than about 15 sec suffer from this. On the other hand, if the sweep takes too long, the ionosphere itself may have changed appreciably between the beginning and end of the sweep. Furthermore, the ionosonde may produce excessive interference with other radio systems.

3.2.1.2. The Virtual Height-Time Recorder

This is a fixed-frequency device using a B scan display which operates continuously. Provided that the signal does not penetrate the ionosphere, this system has the advantage of continuous monitoring of the ionosphere and is useful in detecting "one-shot" events such as the effect of a solar flare. It has the added advantage of extreme simplicity.

3.2.2. Absorption Measurements

The ionosonde gives very little information about the D region because reflections from this region tend to be of the partial type rather than the refractive type. Also, the lower frequencies are heavily absorbed in the lower ionosphere because of the high collision frequency there. This absorption is, of course, very important to the radio operator because it sets a lower limit to the power and/or the frequency with which he can operate. Thus absorption measurements are of practical importance and, in addition, they give information on the total electron content of the D region. Some of the methods used will be discussed below. These methods have been described, in more detail, by Piggott, Beynon, Brown, and Little [3].

3.2.2.1. The Pulse Reflection Method

This method has been used extensively in England [4] and elsewhere and involves the measurement of the amplitudes of successive echoes with an A scan display. The amplitudes are usually read off visually, either by noting the gain required to bring the tops of the oscilloscope traces to a fiduciary mark or else by calibrating the face of the oscilloscope.

It is convenient to express the amplitude ratios in terms of an apparent reflection coefficient ρ . This parameter is the ratio of the amplitude I of a wave which is reflected once in the ionosphere to the amplitude I'_0 which would have been received in the absence of dissipative attenuation

$$I = I'_0 \exp\left(-\int \kappa \, ds\right) \tag{3.2}$$

$$\int \kappa \, ds = -\ln \, \rho. \tag{3.3}$$

In practice, the absorption is usually measured in terms of a loss in decibels, L, where

$$L = -20 \log \rho = -8.7 \ln \rho. \tag{3.4}$$

In the absence of absorption, the amplitude I of a wave reflected from a group height h^\prime is given by

$$Ih' = I_0 h_0 \tag{3.5}$$

where I_0 is the amplitude which would have been received if reflection had occurred at a standard height h_0 . When absorption is present the amplitudes of the first I_1 , second I_2 , and rth order I_r reflections are given by

$$I_1h' = \rho I_0h_0 = \rho G, \qquad (a)$$

$$2I_2h' = \rho \rho_g I_1h' = \rho^2 \rho_g G, \qquad (b)$$

$$rI_rh' = \rho^r \rho_g^{r-1}G, \qquad (c)$$
(3.6)

where ρ_{θ} is the apparent reflection coefficient of the ground and $G(=I_0h_0)$ may be regarded as a calibration constant.

The calibration factor, G, can be found by measuring the amplitudes of multiple reflected signals when the absorption is low (at night) and can then be used to measure ρ when the absorption is high, i.e., when there is one reflection only.

When G is known, ρ can be found from the group height and amplitude of the reflected echo.

The chief practical problem in the measurement of absorption by this technique is that introduced by the continuous fading of the reflected signal. This question is too complex to be considered here but it requires that a suitable statistical sample be used to derive a mean amplitude. For vertical incidence measurements in the HF band, periods between 15 and 20 min are common, and it is desirable to average over such periods. Of course, if the averaging period is excessive, the absorption itself may have changed during the interval.

The chief disadvantage of this system is that the measurements are tedious to make and/or reduce to L values. Furthermore, inaccuracies arise because of noise and interference, polarization, pulse dispersion, partial reflection, and scattering (see ref. [3]).

3.2.2.2. Continuous-Wave Field-Intensity Recordings

In this method a continuous wave sender is used. A communicationstype receiver is fed by a calibrated antenna and the output is registered on a pen recorder.

The CW recording method of measuring ionospheric absorption has the advantage of continuous recording, but it suffers from the disadvantage of not being able to separate the various echoes. The total field received at any instant is the resultant of different order echoes and of ordinary and extraordinary waves, all fading independently of each other. Approximately, the resultant median field intensity is the square root of the sum of the squares of the median values of all of its components. From a knowledge of the differential absorption of the ordinary and extraordinary waves, and using the root-sum-square rule, the field intensity of the ordinary wave, first echo, can (in principle) be obtained.

If transmitter and receiver are close together, so that the incidence is essentially normal, it is possible to calibrate the equipment (roughly) by assuming that the nighttime signals are not absorbed in the ionosphere.

3.2.2.3. The Riometer Method

The riometer (rio=relative ionospheric opacity) is simply a receiver that measures the intensity of the random noise which impinges on the earth from deep space. The use of cosmic radio noise for the measurement of ionospheric absorption has been developed by Little [3] and his coworkers. The principle is as follows:

The radio noise power incident at a point *outside* the earth's atmosphere from a given direction in space is assumed to be constant with respect to time. The noise power received on a fixed receiving system at the earth's surface should, therefore, be a function of sidereal time only, since each day the aerial beam will explore the same strip of sky as the earth rotates. The transparency of the atmosphere at a particular instant of time is, therefore, given by the ratio of the signal strength actually received to that received at the same sidereal time under conditions of little ionospheric absorption.

The simplest equipment capable of measuring cosmic noise consists of a gain stable receiver connected to an antenna (input) and a pen recorder (output), as illustrated in the block diagram in figure 3.4, together with a noise diode, for calibration purposes, and stabilized power

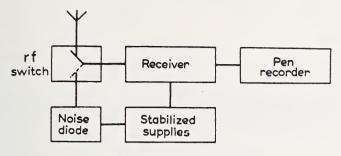


FIGURE 3.4. Block diagram of riometer.

(After C. G. Little, 1957, in The Measurement of Ionospheric Absorption, Annals of the IGY, Vol. III, Part II, Pergamon Press.)

supplies. The calibration is carried out, automatically, by periodically disconnecting the antenna and feeding into the receiver, a known quantity of noise power from the diode.

To understand how the method works, consider an antenna looking at the sky, the temperature of which is T_s . If the bandwidth of the receiving system is B, the available power is

$$P_1 = k T_s B. (3.7)$$

If now some absorbing medium (such as the ionosphere) with a power transmission coefficient α and temperature T_i is inserted over the whole of the antenna beam, the power received from the sky would be reduced to $\alpha k T_s B$. The absorbing medium would, however, itself radiate noise in proportion to its temperature and its effectiveness as an absorber. The antenna would receive an additional signal $P_2 = k(1-\alpha) T_i B$ from the absorbing medium.

In the case where the signal is transferred to the receiver via a transmission cable, the power transmission coefficient of which is E, the transmission line itself will act as an attenuator and a generator of radio noise P_c . The noise reaching the receiver will be given by:

$$E[\alpha k T_s B + k(1-\alpha) T_i B] + (1-E)k T_c B,$$

where T_c is the temperature of the transmission line. It is assumed that the antenna and receiver are both matched to the transmission line, and that the power transfer from the antenna to the receiver is complete, apart from the effect of absorption within the transmission line.

This received power will add to the noise generated within the

receiver, which is given by

$$P_r = (F-1)kTB, (3.8)$$

where T is the room temperature and F is the noise factor of the receiver. If the above system receives cosmic radio noise, the output power P_0 of the receiver may be written as

$$P_0 = G(P_s + P_i + P_c + P_r + I) \tag{3.9}$$

where P_s = noise power from the sky = $E\alpha T_s kB$,

 P_i = noise power from the ionosphere = $E(1-\alpha) T_i kB$,

 T_s , T_i = effective temperatures of sky and ionosphere,

 P_c = noise power from cable = $(1-E) T_c kB$,

 P_r = noise power from receiver = (F-1) TkB,

I = interference,

G = power gain of the receiver.

The problem introduced by interference can be partially removed by recording the minimum signal received while the receiver frequency is swept over a small frequency range (but many bandwidths). Various other refinements are discussed in reference [3].

It should be realized that the riometer is of use on frequencies above the penetration frequency only. A typical frequency is about 30 Mc/s. The disadvantage of such high frequencies is that the ionospheric absorption is low and it is necessary, therefore, to measure small changes in absorption. A riometer can usually measure absorption changes down to about 0.1 dB.

3.2.2.4. Minimum Frequency Observations

In (2.99) it was shown that non-deviative absorption varies inversely as the square of the wave frequency. Thus, when sounding the ionosphere with a conventional ionosonde, the minimum frequency observed, f_{\min} , is roughly, a function of the ionospheric absorption. The characteristic f_{\min} has been used quite widely as an index of ionospheric absorption and its use is justified provided that the absorption changes are large compared with the other variable characteristics of the ionosphere.

3.2.3. Phase Measurements

3.2.3.1. Relative Phase Changes

Although it is not possible to determine the absolute phase of a reflected signal it is possible to measure, accurately, changes in phase, This can be done by mixing the incoming signal of frequency f_e with a local oscillator signal of frequency f_r of about the same amplitude and differing from it in frequency by a small amount $(f_e - f_r)$. The phase of the signal from the reference oscillator must be highly stable or else must be locked to that of the radiated signal. With the advent of portable stable crystal oscillators and atomic frequency standards the former alternative is possible. The echo and the reference signal beat together in the detector stage of the receiver and give a beat signal of frequency $(f_e - f_r)$. This gives a sinusoidal trace on the screen of an oscilloscope when the output of the receiver is applied to the y plates and a linear time base is applied to the x plates. The movements of the sinusoidal trace depict the varying phase of the echo. Such a method has been described by Findlay [5]. Suitable modification of this arrangement enables the phase changes to be tracked electronically and displayed on a pen recorder instead of on photographic paper.

3.2.3.2. Frequency Changes

When the changes of phase with time are slow, the above method is very suitable; on the other hand, if the phase changes rapidly with time, there is a Doppler change in the received frequency and it is often convenient to measure frequency changes rather than phase changes. The technique is essentially the same as that described above; the beat frequency signal may be recorded directly on a pen recorder and the frequency changes determined by inspection. In a slight modification used by Ogawa [6] and by Fenwick and Villard [7], the beat frequency is fed to a frequency meter the output of which is recorded on an inked chart.

One disadvantage of both the above presentations is that they give the frequency variation of the composite sky wave. An improvement on this is the technique developed by Watts and Davies [8] which is of interest also in that it provides one solution to a data storage problem. This method involves the spectral analysis of the beat signal. The beat signal is fed directly to the recording head of a magnetic tape recorder

the speed of which is 0.02 ips (inches per second). At this speed an 1800-ft roll of tape can store data continuously for more than one week, at the end of which the tape is played into an audio spectrum analyzer at a speed of 30 ips, say. This results in a frequency multiplication of 1500 and so converts the beat frequency of a few cycles per second into an audio tone. A commercial 420 channel analyzer having a total bandwidth of 10.5 kc/s and a channel bandwidth of 32 c/s is used for analysis; the output is displayed on a continuously fed facsimile attachment. With such a system the frequency resolution is about 0.2 c/s and the time resolution is less than 1 min. This method of recording is suitable for studying transient phenomena such as the ionospheric effects associated with solar flare and sudden magnetic commencements. A sample record taken during a solar flare is shown in figure 3.5.

3.2.4. Angle of Arrival

3.2.4.1. Direction Finding

Ionospheric tilts and irregularities give rise to radio rays which lie outside the great circle path through the transmitter, the receiver, and the center of the earth. Various techniques have been developed for measuring the azimuthal angles of arrival of signals and an account of the modern techniques used can be found in reference [9].

3.2.4.2. Vertical Angle

There are three principal methods of measuring vertical angle of arrival: (1) the phase measurement method, (2) the use of "musa" or multi-unit steerable antenna, and (3) the use of two antennas having different radiation patterns in the vertical plane.

The most common system is (1) and depends on the fact that when a radio wave (of wavelength λ) from a given direction arrives at two receiving antennas, separated by a known distance d, the phase angle ϕ between the induced voltages is

$$\phi = \frac{2\pi \ d}{\lambda} \cos \Delta \cos \psi \tag{3.10}$$

where Δ is the vertical angle measured from the horizontal and ψ is the

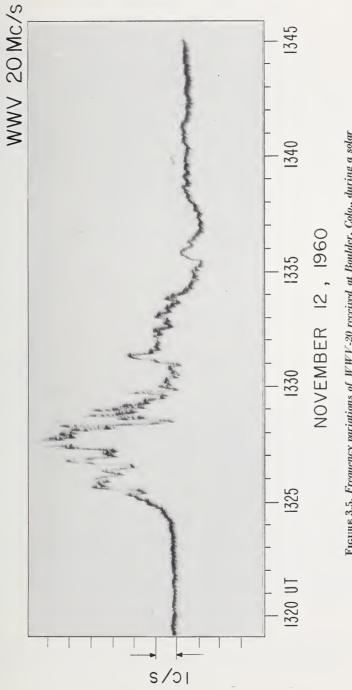


Figure 3.5. Frequency variations of WWV-20 received at Boulder, Colo., during a solar flare, November 12, 1960.

azimuthal angle, measured from a line joining the centers of the two antennas.

In practice the antennas are oriented with their centers in the great circle plane passing through the transmitter and receiver so that $\psi \approx 0$. For accurate measurements it is necessary to correct for the variation of ψ .

The musa system for measuring a vertical angle consists of an antenna array having a very sharp lobe which can be steered up and down in the vertical plane. The vertical angle is determined by the position of the lobe at which the received signal is a maximum.

In the third system the antennas may be a pair of identical ones at different heights above ground or one can be a horizontal and the other a vertical. In either case the antenna patterns must be known. One useful application of this method is in normal incidence sounding where dipoles are located at such heights as to give (1) a maximum, (2) a null in the zenith direction. This arrangement enables a determination to be made of whether echoes are returned from overhead or scattered obliquely.

3.2.5. Rockets and Satellites

In recent years it has become possible to explore the ionosphere by sending up radio equipment in rockets and satellites. In particular, electron density profiles have been deduced from measurements in rockets of the differential absorption [10] between ordinary and extraordinary waves. In 1961 an h't recorder was flown in a rocket to study the topside of the F region [11] and more recently an ionosonde has been flown in a satellite [12] to study the same region.

By moving the observing stations to artificial satellites three important advantages are gained:

- 1. Probes can be used to measure some ionospheric parameters in situ, thereby checking previous radio measurements and adding new ones.
- 2. Radio soundings can be obtained from above the level of maximum density, thereby extending our knowledge greatly.
- 3. Geographic scanning of these parameters can be achieved to an extent and degree of detail never possible with scattered ground stations.

3.3. THE QUIET IONOSPHERE

3.3.1. Purpose

The purpose of this section is to describe the principal observational features of the ionosphere. These features will include the interpretation of ionograms—h'(f) curves—and the geographical and temporal variations in the electron density distributions.

3.3.2. lonograms and Their Interpretation

An ionogram is the photographic output of an ionosonde. The simplest ionogram (nighttime) is of the type shown in figure 3.6. It will be seen that the group height h' increases with frequency until penetration occurs and that there are two distinct traces. The trace having the lower penetration frequency f_0F is the ordinary wave trace and the other having the higher penetration frequency f_xF is due to the extraordinary wave. The penetration frequencies are frequently referred to as the critical frequen-

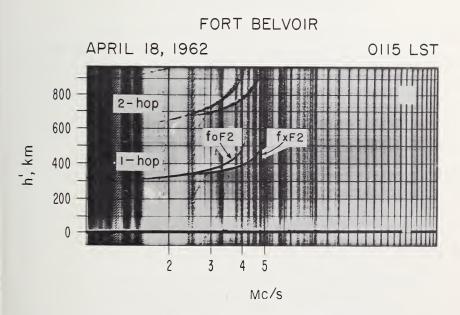


FIGURE 3.6. Ionogram on a quiet night in middle latitudes.

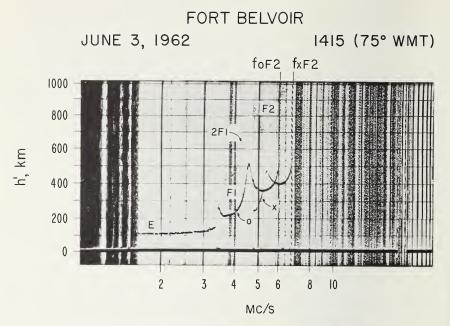


FIGURE 3.7. Ionogram on a quiet summer day in middle latitudes.

cies. An ionogram taken in middle latitudes during a summer day (fig. 3.7) indicates reflections from the E, F_1 , and F_2 layers for both ordinary and extraordinary waves. Note that just above the critical frequencies of the E and F_1 layers the group height decreases with increase of frequency. This arises because the retardation below the level of reflection is decreasing with frequency more rapidly than the retardation near reflection is increasing with frequency. The minimum heights of the ordinary wave traces are called the minimum virtual heights of the respective layers [1]. Figure 3.8 shows an example of a high-latitude ionogram which has an additional z trace which can occur at high values of magnetic dip. Notice also the trace near the 120 km level marked E_s . This is believed to be a reflection from a thin layer, at about the same height as the normal E layer, which varies in an unpredictable manner and, hence, is called sporadic E. Sometimes this layer is sufficiently thick to give rise to well-defined critical frequencies (f_0E_s and f_xE_s).

The relationship between the z, o, and x critical frequencies can be obtained from the fact that they are reflected at the levels X=1+Y, X=1, and X=1-Y, respectively. If $f_{N \text{ max}}$ is the value of the plasma

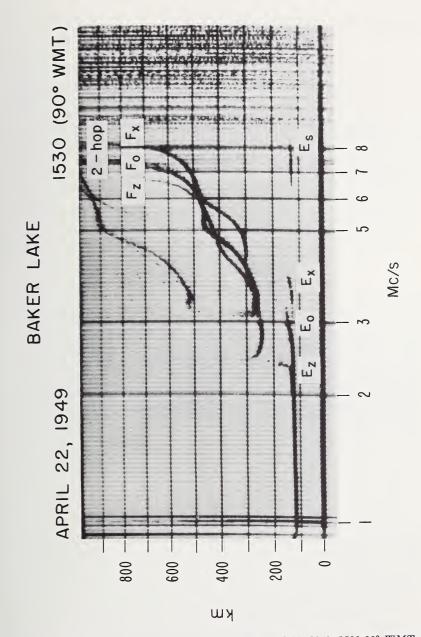


Figure 3.8. High-latitude ionogram, Baker Lake, April 22, 1949, 1530 90° WMT.

(By permission of the Chief Superintendent, DRTE, Ottawa, Canada.)

frequency at the peak of the layer, we have:

$$f_{N \max}^{2} = f_{z}^{2} + f_{z} f_{H}, \qquad (a)$$

$$f_{N \max}^{2} = f_{0}^{2}, \qquad (b)$$

$$f_{N \max}^{2} = f_{x}^{2} - f_{x} f_{H}, \qquad (c)$$
(3.11)

from which we get

$$f_0^2 = f_x^2 - f_x f_H,$$
 (a) and $f_x - f_z = f_H.$ (b)

Equation (3.12a) can be solved for f_x in terms of f_0 and f_H . If f_0 and f_x are much larger than f_H , however, so that $f_x+f_0\approx 2f_x$ we obtain

$$f_x - f_0 \approx \frac{1}{2} f_H. \tag{3.13}$$

We see that, for a given f_H (given altitude and geographic location), the difference between f_x and f_z is independent of critical frequency and the difference between f_x and f_0 is approximately so. Hence, from measurements of the separations of the critical frequencies of a given layer we can, in principle, determine the magnetic field strength (from f_H) at the height of the layer peak. The f_x-f_0 separation as a function of frequency is shown in figure 3.9.

Most ionosondes have a lower frequency limit of about 1.0 Mc/s or 1.5 Mc/s for practical reasons such as high daytime absorption, broadcast interference, antenna limitations, and lack of height resolution (at the lowest frequencies the radio frequency period is comparable to that of the pulse duration; for instance, a 50- μ sec pulse would contain only five cycles at 100 kc/s). Low and medium frequency ionograms have been made by several workers, notably by Watts [13, 14], at the CRPL.

An example of a nighttime low-frequency ionogram is shown in figure 3.10, which shows reflections from heights of about 90 to 100, 120 to 150, and 220 to 230 km. The layers, or ledges, which produce these reflections will be referred to as E_s , E, and F respectively. The reason for calling the "150 km" echo E rests on the observed continuity

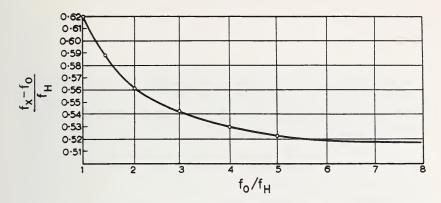


FIGURE 3.9. Critical frequency separation between ordinary and extraordinary traces.

(After J. W. Wright, R. W. Knecht, and K. Davies, 1957, Annals of the IGY, Vol. III, Part I,
Pergamon Press.)

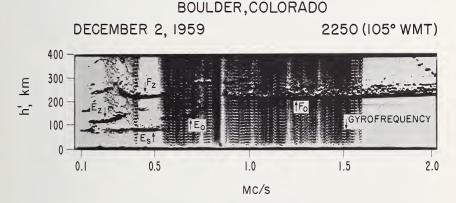


FIGURE 3.10. Low-frequency ionogram.

with the daytime E echo over the sunrise period. The E_s layer appears to be patchy (transparent) and must be fairly thin because no group retardation is evident at its upper frequency limit. Note that the critical frequency of the extraordinary Z trace is less than that of the ordinary, which is to be expected on the theory given in sec. 2.3.3.2.

Ionograms vary in appearance depending upon the geographic location of the station. A great many more ionograms are available for study in the IGY Atlas of Ionograms [15] and in the Annals of the IGY [2].

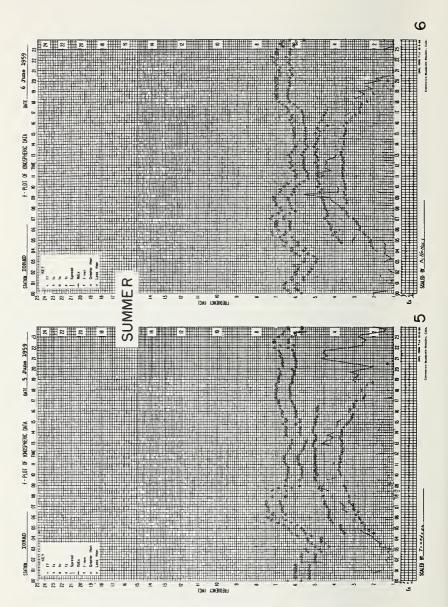


FIGURE 3.11a. Sample f plot for Adak, Alaska—summer.

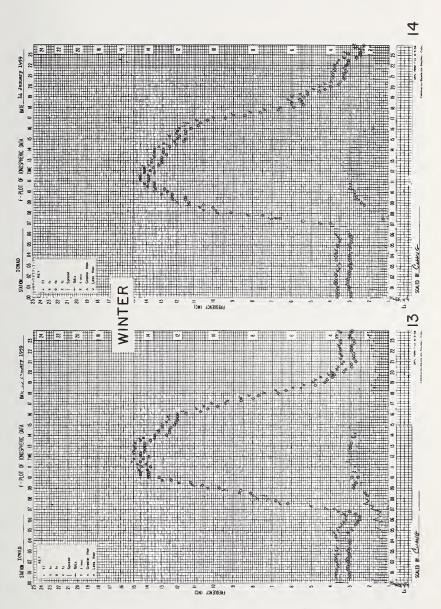


FIGURE 3.11b. Sample f plot for Adak, Alaska-winter.

Ionospheric data are available, in several different forms, in one of the four World Data Centers. These forms may be the original ionograms or scaled hourly values of the various parameters (e.g., critical frequencies and minimum virtual heights) or simply monthly median values of these parameters as published in the CRPL F Series, Part A [16]. The latter publication contains monthly medians of ionospheric parameters from about 80 stations in tabular and graphical form. Another form of presentation (due to J. H. Meek) is the f plot. The f plot is a daily graph of the frequency characteristics of the ionograms as a function of time, using internationally agreed conventions for interstation comparison. It was originally developed to enable the complicated and rapidly changing ionograms from high latitudes to be reduced with the minimum of interpretation by the scaling individual. It was also introduced to obviate the necessity of repeated plotting from tabulated data. Its use has now become worldwide. Some sample f plots are shown in figure 3.11.

3.3.3. Electron Density Profiles

3.3.3.1. Real Height Analysis

Conventional ionograms contain a direct measure of the electron densities of the ionosphere within a range determined by the lowest and highest radio frequencies employed in the sounding. The total retardation depends upon the unknown electron density profile. However, it is not immediately obvious how the actual height of reflection of each frequency is to be determined, for the reason that the apparent (virtual) height depends in an involved way on the group retardation imposed on the probing pulses at each point below the level of reflection.

The group height h' is given by the integral of the group refractive index μ' along the ray path. In the case of vertical propagation this is given by

$$h' = \int_0^{h_r} \mu' \ dh = \int_0^{h_r} \mu' \frac{dh}{d\phi} \ d\phi \tag{3.14}$$

where h_r is the real height of reflection and ϕ is an arbitrary monotonic function of the electron density distribution; for instance, in Budden's method [17] ϕ is f_N , whereas in King's method [18] ϕ is $\log f_N$. It is not possible to solve this integral analytically, except under certain limiting conditions (transverse and longitudinal). However, a solution can be

found by dividing the range of integration into n small intervals within each of which $dh/d\phi$ is assumed constant. Equation (3.14) can then be replaced by

$$h' = \sum_{m=1}^{n} \left(\frac{dh}{d\phi} \right)_{m} \int_{\phi_{m-1}}^{\phi_{m}} \mu' \ d\phi. \tag{3.15}$$

Since the integrals are now dependent on μ' and ϕ and the interval width, they may be evaluated once and for all as a set of coefficients. Equation (3.15) then represents a set of linear equations in $dh/d\phi$. By dividing the observed h'f curve into intervals of equal ranges of ϕ , this system of equations can, in principle, be solved and the real height intervals obtained.

In the above theory, it was assumed that ϕ increased monotonically with height. It does not give us any information about a "valley" which may exist in the profile between the E and F layers, say. Some information on the existence of a valley can be inferred from the extraordinary wave trace [19, 20]. Another limitation on the experimental data is that conventional ionograms give no information on frequencies below about 1.0 Mc/s. Once again the extraordinary trace can sometimes be used to give information concerning unobserved ionization [19, 21]. A good review of this subject has been made by Thomas [22].

3.3.3.2. Diurnal Variations

Sample day and night N(h) profiles for middle latitudes are shown in figures 3.12a and b respectively. Large diurnal changes occur particularly in the lower ionosphere. The daytime structure may be thought of as a single bank of electrons beginning around 100 km and having a peak density around 300 km. The various lower "layers" E and F_1 may be only inflections, or ledges, in the electron distribution.

At night, all vestige of the F_1 layer disappears and the E-layer densities drop by a factor of 100 or so, thus producing a simpler structure. The electron density in the D region is not directly observable by the conventional ionosonde and probably falls from about 10^3 per cm³ at 80 km at noon to less than 10^2 per cm³ at night. Some tentative N(h) profiles (obtained from cross modulation experiments) for the D region are shown in figure 3.13.

Additional features of the diurnal variation in ionospheric structure are illustrated in figure 3.14. Note that the E layer appears promptly at

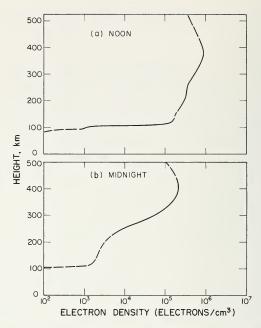


FIGURE 3.12. Sample electron density profiles at White Sands, New Mexico, April 1961.

(a) Noon; (b) midnight. (After R. W. Knecht, unpublished.)

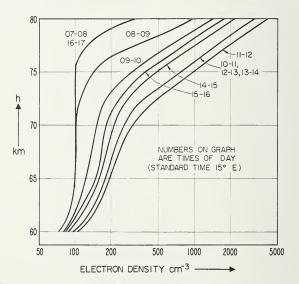


FIGURE 3.13. D-region profiles.

(By permission of the Norwegian Defense Research Establishment.)

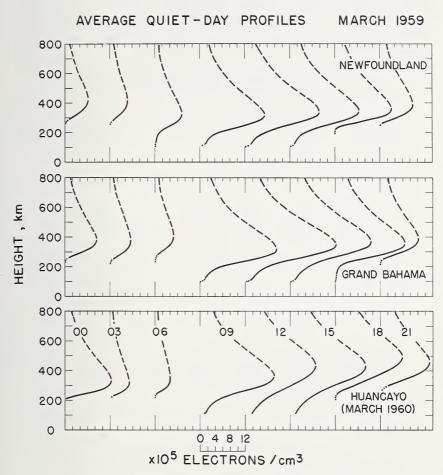


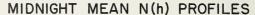
FIGURE 3.14. Diurnal changes in ionospheric profiles.

(After J. W. Wright, unpublished.)

sunrise and disappears promptly at sunset (except for the residual nighttime ionization). The electron densities are greater at all heights by day than by night except at Huancayo, where the density continues to increase for a few hours after sunset.

There is a general tendency for the height of the F_2 peak, $h_m f_2$, to fall at dawn, and then to rise during the afternoon or evening. In low latitudes, $h_m f_2$ reaches a very high level by about 1900 and then falls such that at midnight it is about 100 km lower than at noon. In middle latitudes, $h_m F_2$ rises after sunset and is 50 to 100 km higher at midnight than at noon. This height variation is especially noticeable at Huancayo where at 1900 to 2000 the F region may rise to very great heights indeed.

At the highest latitudes, the ionosphere may be in continuous sunlight or darkness for long periods, depending upon the season. In these circumstances the ionosphere will be typical of daylight or nighttime conditions, respectively. A moderate diurnal variation may be due to small variations of the solar zenith angle, but a diurnal variation is still detectable at the south pole, where the solar zenith angle is diurnally



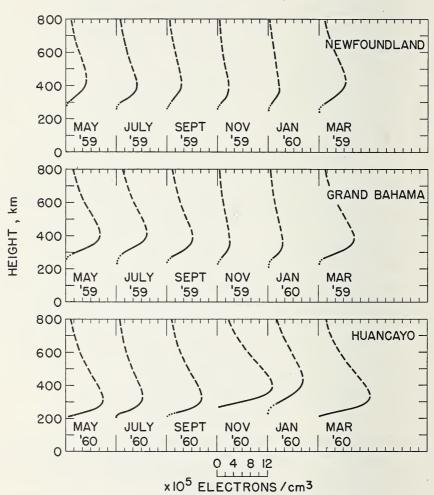
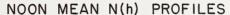


Figure 3.15. Seasonal changes in midnight N(h) profiles (After J. W. Wright, unpublished.)

constant [24], confirming that, at high latitudes at least, other factors besides solar illumination play a role in determining the diurnal variations of the ionosphere. The topside profiles, represented by the broken lines, figures 3.14 through 3.17, are extrapolated on the basis of a Chapman type distribution (1.32).



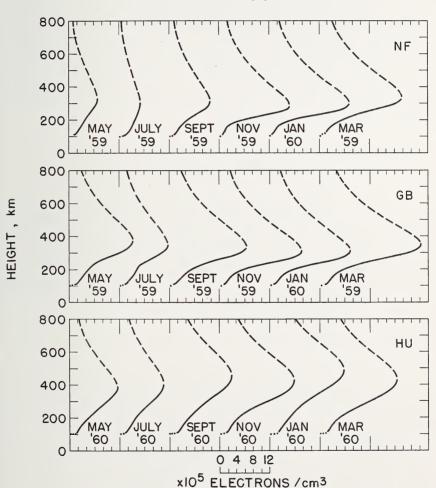


Figure 3.16. Seasonal changes in noon $N(\mathbf{h})$ profiles. (After J. W. Wright, unpublished.)

3.3.3.3. Seasonal Variations

The seasonal variation in N(h) profiles is illustrated in figures 3.15 and 3.16 for midnight and noon conditions respectively. The nighttime F layer tends to be at higher heights in summer than in winter, the tendency being accentuated in lower latitudes. The nighttime F layer tends to be thicker when higher. In general, the maximum electron density and the total electron content of the nighttime F region are greater in summer than in winter. Turning to the noon profiles, the most distinctive feature is that the peak density is considerably larger in winter than in summer; this is called the seasonal anomaly. It is more evident at high latitudes than at low latitudes. In the summer months, in middle latitudes, the F layer bifurcates into the F_1 and F_2 layers. Under these conditions the F_2 peak density is fairly small and is located at a relatively great altitude. The F_1 layer is not so much a distinct layer but rather a minor inflection in the profile at about 200 to 220 km.

3.3.3.4. Solar Cycle Variations

In sec. 1.7.3 we discussed the long-term variation in sunspot activity. This variation has a profound effect on the noon electron distribution, as can be seen from figure 3.17. The graphs are arranged to show increments in ionization corresponding to increments of 100 in sunspot number. The electron densities above the peak are extrapolated. A striking feature of this variation is that the most significant increases in electron density occur at successively higher heights.

3.3.3.5. Geographical Variation

The expense of reducing all ionograms to N(h) profiles has meant that the worldwide distribution is not yet available. Some idea of the latitudinal variations can be obtained from the iso-ionic contours obtained at CRPL [24], examples of which are shown in figure 3.18. Profile data taken near the 75° west geographic meridian were used and the iso-ionic contours are for fixed values of plasma frequency. The height of the F_2 maximum is shown by a dotted line. The following features are important:

(1) The F layer is much thicker near the magnetic equator than elsewhere.

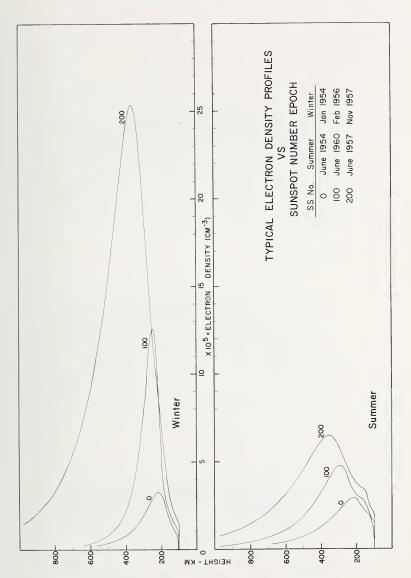
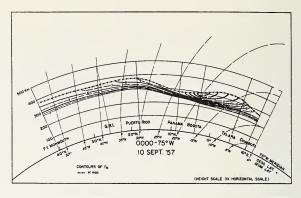
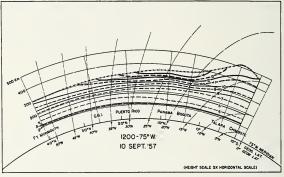


Figure 3.17. Solar cycle changes in noon N(h) profiles.

(After J. W. Wright, 1962, Dependence of the ionospheric F region on the solar cycle, Nature 194, 461.)

(2) There are regions of high electron concentration at geomagnetic latitudes of about $\pm 20^{\circ}$ during the afternoon and early evening. This distortion of the ionosphere is of importance in transequatorial radio propagation, and will be considered later.





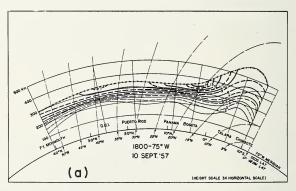


Figure 3.18. Ionospheric sections along the 75th geographical meridian.

(After J. W. Wright, 1959, Note on quiet-day vertical cross sections of the ionosphere along 75° west geographic meridian, J. Geophys. Res. 64, 1631.)

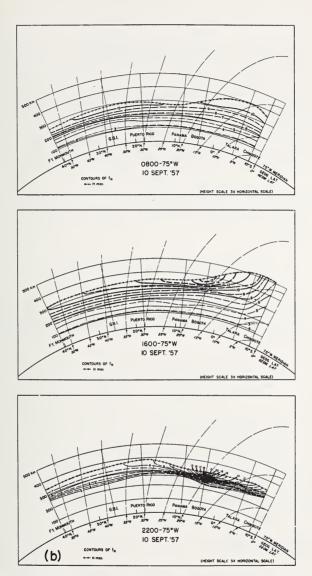


Figure 3.18—Continued. Ionospheric sections along the 75th geographic meridian.

3.3.4. Model Layers

For many purposes, particularly computational purposes, it is convenient to approximate the N(h) profile by analytical expressions which are amenable to integration, differentiation, etc. Various models can be used as approximations to the Chapman layer; for instance, near the peak the distribution is approximately parabolic, whereas high up in the layer the distribution is roughly exponential. Over short ranges of height it is often sufficiently accurate to assume a linear variation of N with h. Some relevant formulas derived from certain models are given below.

3.3.4.1. Chapman Layer

From (1.32) we have

$$N=N_0 \exp \frac{1}{2}\{1-z-\sec \chi \exp (-z)\}.$$

The total non-deviative absorption suffered by a wave of angular frequency ω in one complete vertical transit through the layer (in which $\omega^2 \gg \nu^2$) is given by

$$L = \int_{-\infty}^{+\infty} \kappa \, ds = \frac{N_0 H \nu_0}{\epsilon_0 m c} \sqrt{2\pi \, \exp \, (1)} \frac{\cos^{1.5} \chi}{(\omega \pm \omega_L)^2} \,. \tag{3.16}$$

Here N_0 is the electron concentration at the level of maximum electron production when $\chi=0$ (i.e., at z=0), ν_0 is the collision frequency at the same height, and H is the constant scale height. It is assumed that the propagation conditions are quasi-longitudinal, ω_L being the gyrofrequency corresponding to the component of the earth's magnetic field in the direction of phase propagation.

3.3.4.2. Parabolic Layer

When χ and z are very small (1.32) reduces to

$$N = N_0 \exp \frac{1}{2} \left\{ \frac{1}{2} z^2 \right\} = N_0 \left\{ 1 - \left(\frac{z}{2} \right)^2 \right\} = N_0 \left\{ 1 - \left(\frac{h - h_0}{2H} \right)^2 \right\}, \quad (3.17)$$

which is the equation of a parabola with semithickness (i.e., distance

from base to level of maximum density) of $y_m = 2H$:

$$N = N_0 \left\{ 1 - \left(\frac{h - h_0}{y_m} \right)^2 \right\}. \tag{3.18}$$

This can be written in terms of plasma frequency:

$$f_N^2 = f_p^2 \left\{ 1 - \left(\frac{z}{2}\right)^2 \right\},$$
 (3.19)

where f_p is the penetration frequency of the layer.

In the absence of an imposed magnetic field, the refractive index within the layer is given by

$$\mu = \frac{1}{\mu'} = \left(1 - \frac{f_N^2}{f^2}\right)^{\frac{1}{2}} = \left\{1 - \left(\frac{f_p}{f}\right)^2 \left(1 - \left(\frac{z}{2}\right)^2\right)\right\}^{\frac{1}{2}}.$$
 (3.20)

The group height for reflection within the layer is given by

$$h' = \int \mu' dh = h_0 - y_m + \frac{1}{2} y_m \frac{f}{f_p} \ln \frac{f_p + f}{f_p - f}, \qquad (3.21)$$

and the phase height for the same conditions is

$$h_p = \int \mu \, dh = h_0 - \frac{1}{2} y_m - \frac{1}{4} y_m \left(\frac{f_p}{f} - \frac{f}{f_p} \right) \ln \frac{f_p + f}{f_p - f}. \tag{3.22}$$

Note that $h' = h_0$ for a frequency $0.834 f_p$. This shows that the height of the maximum electron density is equal to the group height on a frequency of $0.834 f_p$.

For transmission through a layer, the contributions to the group and phase heights are

$$h' = h_0 - y_m + \frac{f}{f_p} y_m \ln \frac{f + f_p}{f - f_p}, \qquad (3.23)$$

$$h_p = h_0 + \frac{y_m}{2} \left(\frac{f}{f_p} - \frac{f_p}{f} \right) \ln \frac{f + f_p}{f - f_p}.$$
 (3.24)

3.3.4.3. Linear Layer

If N increases linearly with height h from a base at h_0 above ground, since N is proportional to f_N^2 , we have

$$f_N^2 = a(h - h_0), (3.25)$$

where a is the constant height gradient of f_N^2 . The virtual and phase heights are given by

$$h' = h_0 + \frac{2}{a}f^2 \tag{3.26}$$

$$h_p = h_0 + \frac{2}{3a}f^2. (3.27)$$

3.3.4.4. Exponential Layer

The equation for this layer can be written:

$$f_N^2 = F^2 \exp (az) \tag{3.28}$$

where $z = (h - h_R)/H$ and F is the plasma frequency at the level h_R . Note that, for propagation in the medium, the wave frequency must be greater than F. The group and phase heights are given by

$$h' = \frac{2}{a} \ln \left[\frac{f}{F} + \left\{ \left(\frac{f}{F} \right)^2 - 1 \right\}^{\frac{1}{4}} \right],$$
 (3.29)

and

$$h_p = h' - \frac{2}{a} \frac{F}{f} \left\{ \left(\frac{f}{F} \right)^2 - 1 \right\}^{\frac{1}{2}}.$$
 (3.30)

3.3.5. Critical Frequency Variations

3.3.5.1. General Features

For many purposes, including radio communication, the most important characteristics of the ionospheric layers are their critical fre-

quencies and virtual heights. In this section we shall consider the temporal and geographical variations in critical frequencies.

In figure 3.19 are shown the monthly mean noon critical frequencies of the E, F_1 , and F_2 layers as observed at Slough, England, over a 30-

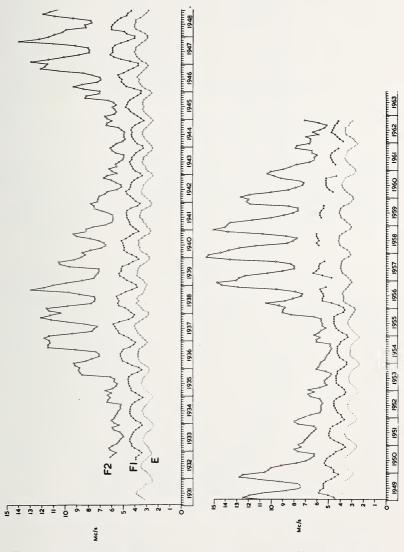


Figure 3.19. Monthly mean noon critical frequencies at Slough, 1932-1962.

(Reproduction is by permission of the Controller of Her Brittannic Majesty's Stationery Office and is by arrangement with the Director of Radio Research.)

yr period. These graphs bring out some important features, namely:

- (a) The seasonal variation of f_0E and f_0F_1 are in phase with solar zenith angle χ whereas f_0F_2 is in antiphase (winter anomaly).
 - (b) The F_1 layer disappears in some winters.
- (c) There is a marked increase in the critical frequencies in sympathy with the 11-yr sunspot cycle.

3.3.5.2. The *E* Layer

To a first approximation the critical frequencies of the E layer are given by

$$f_0E = 0.9[(180 + 1.44R) \cos \chi]^{0.25},$$
 (3.31)

where R is the Zürich sunspot number. The exponent may vary between 0.1 and 0.4 for the diurnal variation but (3.31) is a reasonably good fit for seasonal and diurnal variations. Values of f_0E determined from (3.31) are usually within 0.2 Mc/s of the observed values. During the night f_0E reaches a minimum of about 0.5 Mc/s at sunspot maximum or about

fo E - 1958 FORT BELVOIR

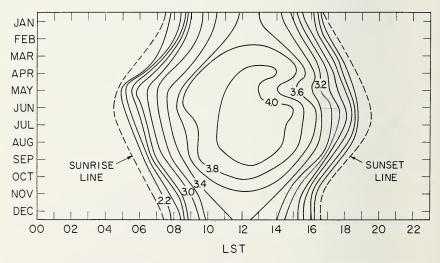
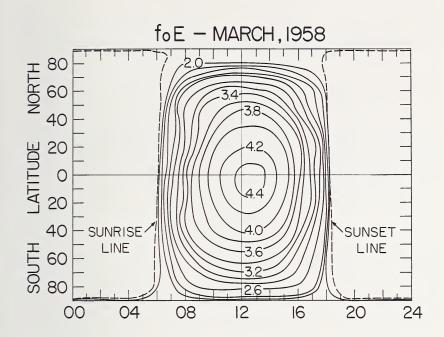


FIGURE 3.20. Diurnal and seasonal variations of f₀E at Fort Belvoir, 1958.

Contours in Mc/s. (After R. W. Knecht, unpublished.)



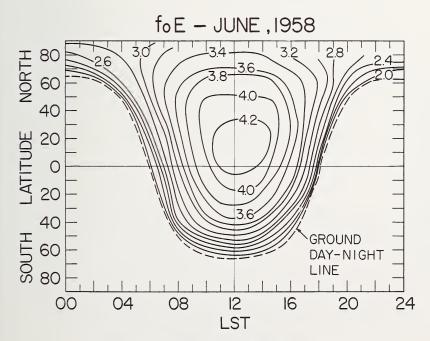


FIGURE 3.21. Maps of f₀E, March, June 1958.

(After R. W. Knecht, unpublished.)

0.25 Mc/s at sunspot minimum. The temporal variation of f_0E during 1958 at Fort Belvoir is shown in figure 3.20. The local time variations of f_0E with latitude for March and June 1958 are shown in figure 3.21.

3.3.5.3. The F_1 Layer

The F_1 layer is observed only during the day; it is more pronounced during the summer than during the winter, and at high sunspot number, and during ionosphere storms, i.e., when f_0F_2 is low.

To a first approximation:

$$f_0 F_1 = (4.3 + 0.01R) \cos^{0.2} \chi.$$
 (3.32)

Here again the exponent varies from place to place and with season. For example, at Fort Belvoir it is about 0.18 in summer and about 0.25 in winter. Furthermore, it appears to be lower at sunspot minimum than at sunspot maximum. The diurnal and seasonal variations in f_0F_1 at Fort Belvoir are shown in figure 3.22 and the latitude variation is illustrated in figure 3.23.

fo E-1958 FORT BELVOIR

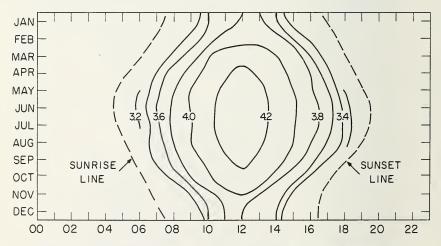


FIGURE 3.22. Diurnal and seasonal variations of f_0F_1 at Fort Belvoir, 1956. (After R. W. Knecht, unpublished.)

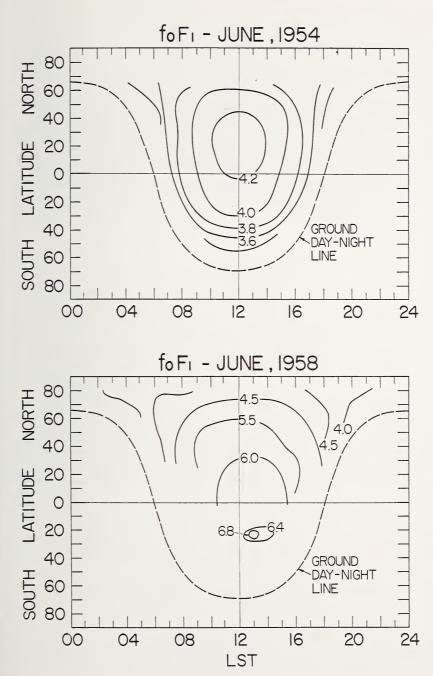


FIGURE 3.23. Maps of f_0F_1 . (After R. W. Knecht, unpublished.)

3.3.5.4. The F_2 Layer

The F_2 layer is by far the most important layer from the point of view of HF radio communications and it is also the most variable. Unlike the E and F_1 layers, the F_2 does not follow a $\cos \chi$ law either diurnally or seasonally. This is illustrated in the f plots of figure 3.11 for Adak. Although during January the sun is at a low elevation ($\cos \chi = 0.291$) compared with June ($\cos \chi = 0.877$), the January noon f_0F_2 is more than twice the summer value. This implies a peak electron density ratio of more than four to one. Notice that this "winter anomaly" occurs in the daytime only. In summer the f_0F_2 shows remarkably little diurnal variation. Note also the presence of a consistent F_1 layer during the summer day and its complete absence in the winter day.

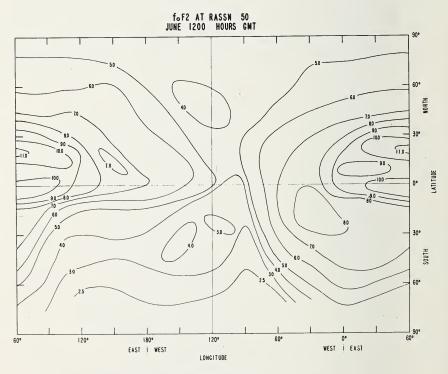


FIGURE 3.24a. World map of foF2, June.

(After D. H. Zacharisen, 1959, World maps of F2 critical frequencies and maximum usable frequency factors, NBS Tech. Note 2 (Apr. 1959), and NBS Tech. Note 2/2 (Oct. 1960).

The geographical distribution of f_0F_2 is characterized by marked geomagnetic control which is revealed by the worldwide maps shown in figures 3.24a and b [25]. These maps are constructed from data for many years which are reduced to a mean sunspot number of 50. The most distinctive features on these maps are the two regions of high f_0F_2 lying around $\pm 20^{\circ}$ dip latitude. These "highs" lag behind the subsolar point but move around with the sun. Because of the geomagnetic control, the critical frequencies of the F_2 layer exhibit a marked longitudinal effect. The "highs" move not only from east to west but also vary in latitude, tending to remain at constant dip angles.

Turning to the solar cycle variation of f_0F_2 , in figure 3.25 are plotted the 12-month running average values of noon f_0F_2 at Fort Belvoir, Va., as a function of the 12-month running average \bar{R} of R (Zürich relative sunspot number). (Note that the 12-month running average for a given

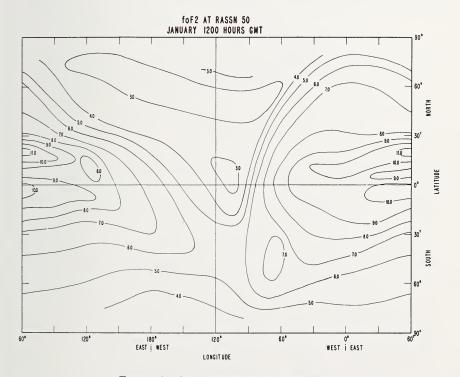


Figure 3.24b. World map of f_0F_2 , January.

(After D. H. Zacharisen, 1959, World maps of F2 critical frequencies and maximum usable frequency factors, NBS Tech. Note 2 (Apr. 1959), and NBS Tech. Note 2/2 (Oct. 1960).)

month is the mean for the preceding 6 months and the succeeding 6 months.) The corresponding data for f_0E and for f_0F_1 are shown for completeness. If a straightedge is alined along the plotted data, it can be seen that, for sunspot numbers between 0 and about 150, the relationship between f_0F_2 and \bar{R} is approximately linear. For values of \bar{R} greater than about 150 there appears to be a certain amount of "flattening" of the curve which has to be taken into account when using sunspot numbers to predict critical frequencies.

3.3.6. Variations in Ionospheric Absorption

3.3.6.1. Introductory Remarks

To a first approximation the variations in the ionospheric absorption of radio waves represent the variations of electron density in the D region.

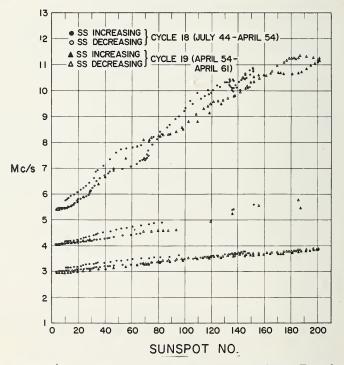


FIGURE 3.25. Variation of noon critical frequencies $(f_0E, f_0F_1, and f_0F_2)$ with sunspot number at Fort Belvoir.

(After R. W. Knecht, unpublished.)

This is particularly the case for waves reflected obliquely from the F_2 layer for which the absorption near the top of the trajectory is small. For waves reflected from the E layer with essentially vertical propagation, the absorption near the level of reflection may be comparable with that suffered lower down.

The most extensive series of absorption measurements in existence are those made at the Radio Research Station, Slough, England, and which have been discussed by Appleton and Piggott [4]. These particular measurements were made using the pulse technique with normal incidence. Absorption measurements using the CW technique have been made at CRPL [26]. In the analyses of these data attempts have been made to separate out the non-deviative and the deviative types of absorption, or the *D*- and *E*-region absorptions, with only limited success. The results discussed below are based on the assumption that the absorption is of the non-deviative type.

3.3.6.2. Frequency Dependence of Absorption

It was shown earlier (sec. 2.3.3.4) that the non-deviative absorption L taking place in a region where $\nu^2 \ll \omega^2$ is given

$$L = \int \kappa \, ds = \frac{A}{(f \pm f_H)^2} \,, \tag{3.33}$$

where the + and - signs refer to the ordinary and extraordinary waves respectively, f_H is the gyrofrequency, and A is a constant depending, however, on the electron density and collision frequency in the D region.

Hence a plot of $L^{-\frac{1}{2}}$ versus frequency should result in a straight line with slope $A^{-\frac{1}{2}}$ and intercept $-f_H$ on the frequency axis. This law has been verified, under certain specific conditions, by Appleton and Piggott [4], but the law does not appear to hold under all conditions [27] because of the influence of deviative absorption and absorption at levels where ν and ω are comparable.

The variation of ordinary wave absorption with frequency is shown in figure 3.26. From this we see the overall decrease of L with frequency. Superimposed on the general trend are two departures due to increased deviative absorption in the neighborhood of the critical frequencies of the E and F_1 layers. When the frequency of the exploring wave is near a critical frequency, the wave spends a relatively long time near the level where μ is small and, consequently, is heavily absorbed. In order to study

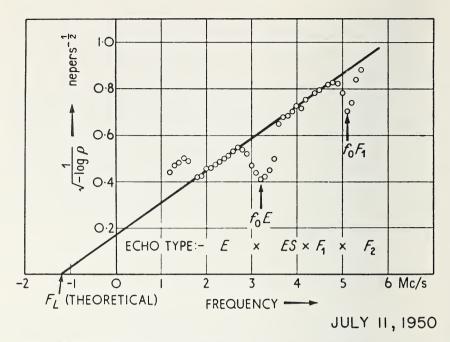


FIGURE 3.26. Variation of absorption with wave frequency (vertical propagation.)

(From E. V. Appleton and W. R. Piggott, 1954, Ionospheric absorption measurements during a sunspot cycle, J. Atmospheric and Terrest. Phys. 5, 141.)

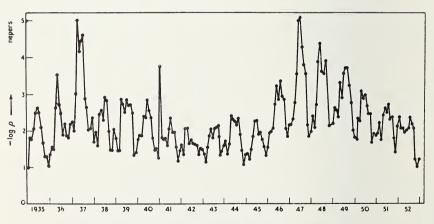


FIGURE 3.27. Noon absorption on 4 Mc/s (Slough).

(From E. V. Appleton and W. R. Piggott, 1954, Ionospheric absorption measurements during a sunspot cycle, J. Atmospheric and Terrest. Phys. 5, 141.)

the D-region absorption, it is necessary first to remove from the total absorption that due to the upper layers. To a first approximation this can be done by taking a parabolic model of electron density as the E layer and an exponential height variation of collision frequency [28]. The total ordinary wave absorption is expressed in the form

$$L = \frac{A}{(f + f_L)^2} + B\phi(f_0 E/f), \qquad (3.34)$$

where ϕ represents some function of the ratio (f_0E/f) , and f_L is the longitudinal gyrofrequency.

The quantity A is the D-region absorption on an "effective" frequency $f+f_L$. With oblique propagation the refractive index never falls to near zero (Snell's law) and the last term in 3.34 is then generally small.

3.3.6.3. Solar Cycle Control

The ionospheric absorption, on 4 Mc/s, measured at Slough over the period 1935 to 1952 (fig. 3.27) exhibits a marked 11-yr solar cycle variation. The values plotted in figure 3.27 indicate a factor of about 2 between sunspot minimum and maximum. The dependence of absorption on sunspot number is roughly linear, that is, of the form

$$L = a(1 + bR). (3.35)$$

Although the value of b appears to vary from one location to another, the best experimental value seems to be about 0.004.

3.3.6.4. Diurnal Variations

For transmission through a Chapman-type layer which is situated at a level of low pressure, so that ν^2 is very much less than $(\omega \pm \omega_L)^2$, the dependence of absorption L on solar zenith angle χ is given by

$$L = C \cos^{3/2} \chi, \tag{3.36}$$

where C depends on the wave frequency, the peak electron density, and the collision frequency (see (3.16)).

Although (3.36) has been verified by Best and Ratcliffe [29] in

middle latitudes, a much better fit to the experimental data is given by

$$L = C \cos^n \chi, \tag{3.37}$$

where C depends on season, magnetic disturbance, etc., and where in middle latitudes the exponent n lies between 0.7 and 1.0. For large values of $\chi(>80^\circ$ say) the cosine function should be replaced by the inverse of the Chapman function $Ch(x, \chi)$ —see (1.42)—but for most practical purposes this is unimportant. From (3.37) we have

$$\log L = \log C + n \log \cos \chi. \tag{3.38}$$

The slope and intercept of this line give the values of n and $\log C$ respectively.

In table 3.1 are listed some mean values of n for various locations. It will be seen that n falls sharply in high latitudes. While there is some evidence for a decrease in n in low latitudes, this cannot be considered conclusive.

Although (3.37) holds reasonably well around midday, it often breaks down near sunrise and sunset and so an alternative expression was developed at the CRPL, namely,

$$L = A + B\cos\chi,\tag{3.39}$$

which represents the diurnal variation somewhat more closely than (3.37). Some theoretical justification for including the term A is provided by photodetachment processes (see fig. 1.4, z=4). At first sight it might

Table 3.1. Solar control of ionospheric absorption $L = C \cos^n \chi$

| Location | Geographic latitude° | n |
|---|--|--|
| Ibadan (Nigeria) Ahmedabad (India) Delhi (India) Sydney (Australia) Tokyo (Japan) Washington, D.C. (U.S.A.) Genoa (Italy) Freiburg (Germany) Slough (England) Prince Rupert (Canada) Churchill (Canada) Baker Lake (Canada) Resolute Bay (Canada) | 7 23 28 -34 35 39 45 48 52 54 59 64 75 | 0.63 0.73 0.62 0.83 0.87 0.83 0.97 0.63 0.75 0.50 0.27 0.18 |

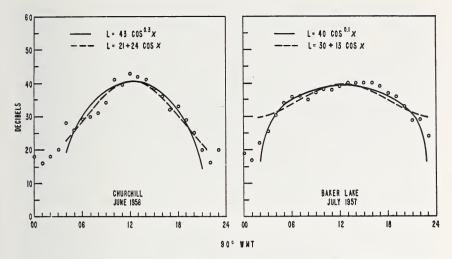


Figure 3.28. Comparison between observed absorption and the formulas $L = C \cos^n \chi$ and $L = A + B \cos \chi$.

appear that (3.37) and (3.39) would give very different variations but, as illustrated in figure 3.28, the differences are, generally, smaller than the scatter in the data. The sensitivity to solar control is determined by the value of B which falls off in high latitudes [30]. The empirical factor K used at the CRPL is

$$K = 0.142 + 0.858 \cos \chi.$$
 (3.40)

To get the total absorption, K has to be multiplied by other factors representing the seasonal, sunspot, and geometrical (path) variations.

3.3.6.5. Seasonal Variations

If monthly mean noon values of L are plotted against $\cos \chi$ it is found that whereas the summer (and equinox) values tend to obey a linear law, the winter months exhibit unexpectedly high absorption, which is known as the "winter anomaly." The increased absorption does not occur uniformly over all days, but appears in the form of high absorption on certain groups of days. It appears primarily to be a middle latitude effect since it vanishes in polar regions where, in winter, the D region is in prolonged periods of darkness [30]. From a comparison between Europe and America, or America and Western Russia, Thomas

[31] has shown that days of enhanced anomalous absorption in one sector correspond to days of reduced anomalous absorption in the other. Days of anomalous absorption are also associated with reflections from the D region [32]. Fortunately, the winter anomaly is not a serious factor from the point of view of radio communications because the critical frequencies of the F_2 layer are also higher in winter than in summer, so that higher frequencies can be used. The decrease of absorption due to the use of the higher frequency more than compensates for the higher absorption on a fixed frequency so that, in general, radio communications are better on winter days than on summer days.

3.3.7. Sporadic E

In addition to the regular layers of the ionosphere there are several of transient or irregular nature. The most important of these is the sporadic-E layer, often designated as E_s . Some examples of sporadic-E reflections on standard ionograms are shown in figure 3.29. It will be seen that the maximum frequency returned from the layer can be much greater than that from the normal E layer and, indeed, from any of the normal layers. Sometimes the E_s traces show retardation near the maximum frequency, indicating a relatively thick layer with a well-defined maximum of electron density. Under other conditions the echoes exhibit no retardation, suggesting that the layer is extremely thin or else due to a sharp change in electron density gradient. On some occasions the E_s layer is opaque and blankets the upper layers; on other occasions the upper layers can be seen through the E_s , which suggests that the E_s is patchy and that the radio waves are penetrating through the gaps. Sometimes magneto-ionic splitting is evident; at other times there is none.

Sporadic-E echoes can occur over a range of heights from about 90 to 120 km or more, and evidence has been advanced by Helliwell for preferred heights [33]. There is some evidence also for believing that one type of E_s is due to ionization by meteors. It is almost certain that several different physical phenomena are lumped together under the general heading of sporadic E. For the scaling of E_s characteristics see reference [1].

Because of its variable nature, sporadic E has been studied largely by statistical means [34], usually by computing the fraction of time that the maximum frequency fE_s exceeds some reference value. Some results obtained in this way are shown in figure 3.30. Close to the equator, E_s is essentially a daytime phenomenon with little seasonal variation. On the

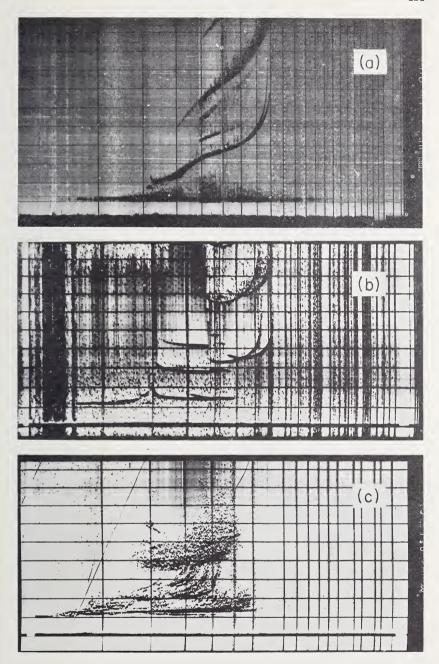


FIGURE 3.29. Examples of sporadic E echoes.

(a) Equatorial—Huancayo, 1457 LST, May 20, 1961. (b) Middle latitude—White Sands, 1604 LST, May 8, 1961. (c) High latitude, night—South Pole, 2055 UT, Aug. 1, 1960.

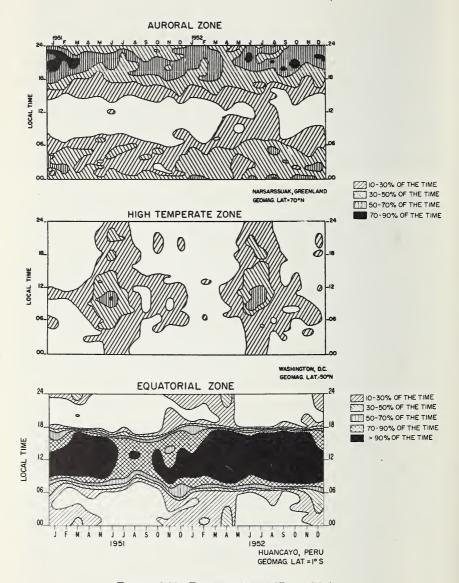


FIGURE 3.30. Fraction of time $fE_s > 5$ Mc/s.

(After E. K. Smith, 1957, Worldwide occurrence of sporadic E, NBS Circ. 582.)

other hand, in the auroral zone, E_s is most prevalent during the night hours but again there is little seasonal variation.

In middle latitudes fE_s is less than elsewhere and the occurrence is subject to diurnal and seasonal variations. In general, E_s is more frequent in local summer than in winter and by day more than by night. Data on the occurrence of E_s are published monthly in the CRPL F Series, Part A.

3.3.8. Spread F

3.3.8.1. Description of Spread F

It is often observed that the echo pulse reflected from the F_2 layer has a much longer (10 times) duration than the transmitted pulse and this phenomenon is called spread F. Undoubtedly, spread F is caused by the scattering of the signal from irregularities embedded in the ionosphere both in depth and away from the zenith. Some examples of ionograms with spread-F echoes are presented in figure 3.31 from which it is seen that the phenomenon occurs in high and low latitudes. A survey of the existing knowledge of spread F has been compiled by Glover [35]. The rules for scaling spread F are discussed in references [1], [2], and [36]. It should be noted that spread F is generally defined in terms of the appearance of an ionogram rather than in terms of the physical mechanism operative.

Several classifications for types of spread F have been suggested, such as high-, medium-, and low-latitude spread F [15], but this method is not entirely satisfactory. An alternative division into "range type" and "frequency type" has been suggested [37]. Frequency type spread refers to diffuseness near the critical frequency of the F_2 layer, whereas the range type refers to diffuseness near the horizontal part of the trace.

Some ionograms, such as that shown in figure 3.32a, exhibit spread only on the multiple echoes. This type is believed to be due to ground scatter, as illustrated in figure 3.32b.

3.3.8.2. Diurnal Variations

Spread F occurrence is essentially a statistical phenomenon, and maps have been prepared showing the probability of occurrence [38]. It is essentially an evening and nighttime phenomenon. In low geomagnetic latitudes the most likely time of occurrence is between about 2100 local

time and about 0100, being earlier at sunspot maximum. In middle latitudes, there is a tendency for spread F to occur most frequently after midnight.

3.3.8.3. Seasonal Variations

In low latitudes the occurrence of spread F is greater during local summer than during local winter. In higher magnetic latitudes the occurrence is more frequent in winter than in summer. However, a number of high-latitude stations exhibit the equational seasonal variations [39].

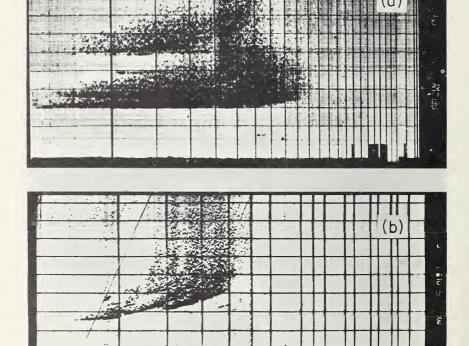


FIGURE 3.31. Spread F ionograms.

(a) Low latitude—Huancayo 0257 LST May 20, 1960; (b) high latitude—South Pole 2245 UT Aug. 1, 1960.

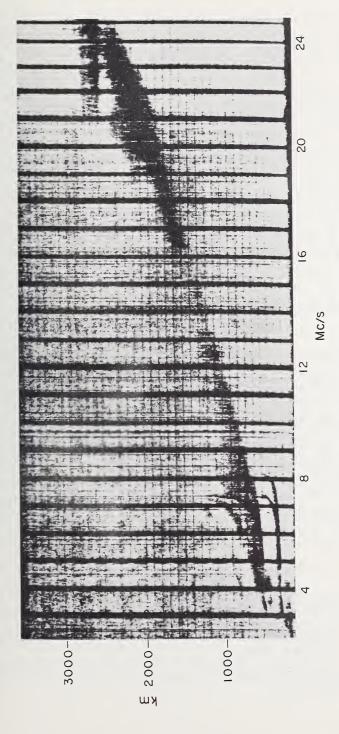


FIGURE 3.32a. Spread F due to ground scatter—ionogram.
(By permission of R. Silberstein, 1954, IRE Trans. Ant. Prop. 2, 56.)

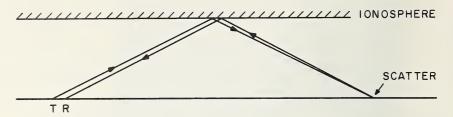


FIGURE 3.32b. Spread F due to ground scatter—path.

3.3.8.4. Solar Cycle Variations

In geomagnetic latitudes above about 60° the occurrence probability of spread F increases with sunspot number, whereas in low latitudes the dependence is inverse [40].

3.3.8.5. Correlation with Magnetic Activity

One of the more interesting features of spread F is its dependence on magnetic activity. In equatorial regions it occurs on magnetically quiet days and disappears with the onset of a magnetic storm [41, 42]. In middle latitudes the occurrence is essentially a storm phenomenon. In magnetic latitudes above 60° the correlation again becomes negative (magnetic storm—no spread). This may be more apparent than real, however, as in such latitudes magnetic storms are associated with high absorption which prevent F echoes being observed.

Spread F occurrence seems to depend on other parameters. It is greater when the virtual height is larger and is smaller when the critical frequency is greater; it is associated also with the scintillations of radio signals from radio stars.

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CHAPTER 4

Oblique Propagation

4.1. CHARACTERISTICS OF HF PROPAGATION

High-frequency (3 to 30 Mc/s) radio waves have been and still are one of the basic vehicles for long-distance transmission of information. The reasons for this may be summarized as follows:

- (a) Low cost of terminal equipment,
- (b) Low power requirements,
- (c) Adequate bandwidths,
- (d) Adequate signal strengths.

In contrast with the above, it may be noted that medium wave frequencies (300 kc/s to 3 Mc/s) suffer very heavy absorption during the day, while on lower frequencies there is insufficient bandwidth for more than a few voice channels. Frequencies much above 30 Mc/s are not, normally, reflected from the ionosphere. For propagation over long distances the F_2 layer is of fundamental importance.

The disadvantages in using high frequencies are:

- (1) The variability of propagation conditions which, for optimum results, requires frequent changes in the operating frequency. Even on the optimum frequency, communications are often subject to interruption by ionospheric storms.
- (2) The large number of possible propagation paths and the resulting time dispersion of a single signal.
 - (3) The large and rapid phase fluctuations.
 - (4) The high interference.
 - (5) Wide-band signals suffer from frequency distortion.

In the lower part of the high-frequency spectrum, refraction in and reflection from the E region (particularly E_s) contribute to the complexity of the echo structure.

The range of high frequencies useful for medium and long distance radio communications is limited, on the upper end, by the height and maximum electron density in the controlling layer and, on the low-frequency end, by absorption in the D region.

In this chapter we shall be concerned with methods of calculating the maximum frequency and with the identification of the structure of signals both by experiment and by means of ray tracing.

4.2. EQUIVALENCE RELATIONSHIPS

4.2.1. Plane Earth and Plane Ionosphere

4.2.1.1. The "Secant Law"

In this section we shall consider the relationships that exist between the frequencies, virtual paths, and absorptions of two waves, one reflected with oblique incidence and the other reflected with normal incidence from the same *true* height. For this purpose consider a ray incident on a plane ionosphere at an angle ϕ_0 , as shown in figure 4.1, in which the electron density is increasing with height so that total internal reflection takes place.

In the absence of both collisions and an imposed magnetic field, the refractive index μ for a wave of frequency f, at a level where the plasma

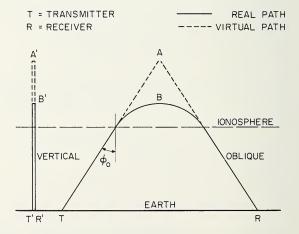


Figure 4.1. Equivalence theorem for plane earth and plane ionosphere.

frequency is f_N , is given by (2.78):

$$\mu^2 = 1 - \left(\frac{f_N}{f}\right)^2 \tag{4.1}$$

Application of Snell's law ($\mu = \sin \phi_0$) gives, at the level of reflection,

$$f_N = f \cos \phi_0$$
.

Now if f_v is the frequency which is reflected with normal incidence from the same true height (i.e., same plasma frequency) as the frequency f with oblique incidence, then $f_v = f_N$.

Therefore

or
$$f_v = f \cos \phi_0, \qquad (a)$$

$$f = f_v \sec \phi_0. \qquad (b)$$

The frequency f_v is called the "equivalent vertical-incidence frequency," corresponding to f. Equation (4.2b) is the so-called secant law. It shows that, with oblique incidence, the ionosphere can reflect much higher frequencies than with normal incidence.

4.2.1.2. Breit and Tuve's Theorem [1]

Another relationship of importance is known as Breit and Tuve's theorem. It states that the group (or equivalent) path P' (see (2.130)), for transmission between a transmitter T and a receiver R (fig. 4.1), is given by the length of the equivalent triangle TAR. That is,

$$P' = TA + AR, \tag{4.3}$$

which can be proved by the following argument:

$$P' = \int_{TRR} \frac{ds}{\mu} = \int \frac{dx}{\mu \sin \phi} = \frac{1}{\sin \phi_0} \int dx = \frac{TR}{\sin \phi_0} = TA + AR.$$

Note that the true height of reflection (at B) is always less than the equivalent height at A.

¹ Figures in brackets indicate the literature references on p. 214.

It should be remembered that (4.3) applies only when sender and receiver are situated outside the ionosphere. If the transmitter and receiver are located within the ionosphere at a level where the refractive index is μ_1 , the right-hand side of (4.3) must be divided by μ_1 in order that P' is still to mean the group propagation time multiplied by the free space velocity.

4.2.1.3. Martyn's (Equivalent Path) Theorem [2]

If f and f_v are equivalent frequencies of waves reflected obliquely and vertically from the same real height, then the virtual height of reflection of f_v is equal to the height of the equivalent triangular path for the oblique signal.

Consider the refractive indices μ_{ob} and μ_{v} for the oblique and vertical waves, respectively, at the same real height at which the plasma frequency is f_N ; we have

$$\mu_{\rm ob}^2 = 1 - \left(\frac{f_N}{f}\right)^2, \qquad (a)$$

$$\mu_{\rm v}^2 = 1 - \left(\frac{f_N}{f\cos\phi_0}\right)^2, \qquad (b)$$

and by Snell's law $\mu_{ob} \sin \phi = \sin \phi_0$. Combining these equations we get

$$\mu_{\rm ob}\cos\phi = \mu_v\cos\phi_0. \tag{4.5}$$

Now the group path for the oblique signal is

$$P' \! = \! \int_{TBR} \! \frac{ds}{\mu_{\rm ob}} \! = \! 2 \int_0^{h_r} \! \frac{dh}{\mu_{\rm ob} \cos \phi} \! = \! \frac{2}{\cos \phi_0} \int_0^{h_r} \! \frac{dh}{\mu_v} \! = \! \frac{2}{\cos \phi_0} \, h_v',$$

$$h_{v}' = \frac{1}{2}P'\cos\phi_0 = \frac{1}{2}(TA + AR)\cos\phi_0 = AD.$$

Hence

$$P'(f) = h'(f_v) \sec \phi_0.$$
 (4.6)

This theorem expresses the important relationship that the virtual height of reflection of an obliquely incident wave is the same as that of the equivalent vertical wave.

4.2.1.4. Martyn's (Absorption) Theorem [2]

If $[L_0]_{\phi_0}^f$ is the absorption suffered by a wave of frequency f incident on the ionosphere at an angle ϕ_0 and $[L_v]_0^f$ cos ϕ_0 is the absorption suffered by the equivalent vertical wave, then

$$[L_0]_{\phi_0} = \cos \phi_0 [L_v]_0^{f \cos \phi_0}.$$
 (4.7)

This may be proved as follows: From (2.100) we have that

$$L_0 = \int_{TBR} \frac{\nu}{2c} \left(\frac{1}{\mu_{\rm ob}} - \mu_{\rm ob} \right) ds = \int_0^{h_r} \left(\frac{1}{\mu_{\rm ob}} - \mu_{\rm ob} \right) \frac{dh}{\cos \phi} \; . \label{eq:loss}$$

Where h_r is the height of reflection together with (4.5) we have

$$L_0 = \int_0^{h_r} \frac{\nu}{c} \left(\frac{1 - \mu_{\text{ob}}^2}{\mu_{\nu} \cos \phi_0} \right) dh = \frac{1}{\cos \phi_0} \int_0^{h_r} \frac{\nu}{c\mu_{\nu}} \left(\frac{f_N}{f} \right)^2 dh$$

$$= \cos \phi_0 \int_0^{h_r} \frac{\nu}{c\mu_{\nu}} \left(\frac{f_N}{f_{\nu}} \right)^2 dh = \cos \phi_0 \int_0^{h_r} \frac{\nu}{c} \left(\frac{1}{\mu_{\nu}} - \mu_{\nu} \right) dh$$

$$= L_{\nu} \cos \phi_0.$$

It is interesting to note that Martyn's equivalent path theorem applies even when collisions are present, provided that ω^2 is very much greater than ν^2 . In this case the angular frequency equivalence is given by

$$\omega_{\text{ob}}^2 + \nu^2 = (\omega_v^2 + \nu^2) \sec^2 \phi_0$$
 (4.8)

and (4.5) is still valid.

The above theorems do *not* apply in the presence of the earth's magnetic field or in a curved ionosphere.

4.2.2. Effect of the Curvature of the Ionosphere

In a curved ionosphere Snell's law takes the form

$$\mu r \sin i = \mu_0 r_0 \sin i_0, \tag{4.9}$$

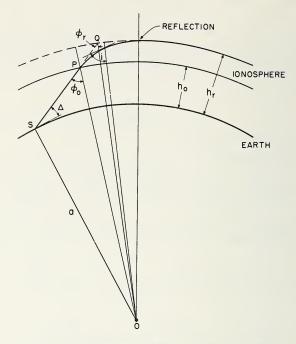


FIGURE 4.2. Ray geometry with oblique incidence.

where r is the length of the radius vector from the center of the earth to the level where the refractive index is μ and the angle between the radius vector and the ray is i, as shown in figure 4.2.; μ_0 , r_0 , and i_0 are arbitrary reference values. Let us take ground level as reference so that $\mu_0 = 1$, $r_0 = a$, and $i_0 = (\pi/2) - \Delta$ where Δ is the angle of elevation. Then

$$\mu r \sin i = a \cos \Delta. \tag{4.10}$$

The relationship between a frequency f and the equivalent vertical frequency f_v which is reflected from the same real height h_r is given by substituting (4.1) into (4.10) and replacing f_N by f_v . This gives

$$\left(\frac{f_v}{f}\right)^2 = 1 - \left(\frac{a\cos\Delta}{a + h_r}\right)^2. \tag{4.11}$$

Now let ϕ_r be the angle between the continuation of the unrefracted ray and the radius vector at the level h_r as shown in figure 4.2. From the ge-

ometry we have that

$$(a+h_r)\sin\phi_r = a\cos\Delta. \tag{4.12}$$

Hence

$$f_v = f \cos \phi_r. \tag{4.13}$$

From (4.11) and (4.13) it will be seen that the equivalent frequency depends not only on Δ but also on the height of reflection h_r .

Instead of defining f_v in terms of the height of reflection, it can be defined in terms of (4.6) or (4.7) but, unlike the plane ionosphere case, the values of f_v will depend on the definition.

4.3. CALCULATION OF MAXIMUM FREQUENCIES

4.3.1. Plane lonosphere

The theorems of Breit and Tuve and of Martyn stated above show that, for a plane ionosphere, the reflection process is equivalent to mirror-type reflection at a height equal to the virtual height h' of reflection of the equivalent vertical frequency. The variation of the latter with frequency can be determined experimentally by means of a conventional sounder.

The relationship between oblique and equivalent-vertical frequencies, in the case of a plane reflector at an equivalent height h', for transmission over a distance D, is given by

$$f_{\text{ob}} = f_v \sec \phi_0 = f_v \sqrt{1 + \left(\frac{D}{2h'}\right)^2}.$$
 (4.14)

In the case of a curved earth and a plane ionosphere ϕ_0 is given by

$$\tan \phi_0 = \frac{\sin \frac{1}{2}\theta}{1 + (h'/a) - \cos \frac{1}{2}\theta}, \qquad (4.15)$$

where a is the earth's radius (6370 km) and θ is the angle at the center of the earth subtended by the transmission path.

To obtain f_{ob} for a given value of f_v we need to know h' as a function of f_v —from an ionogram—and the relationship between $\sec \phi_0$ and h'

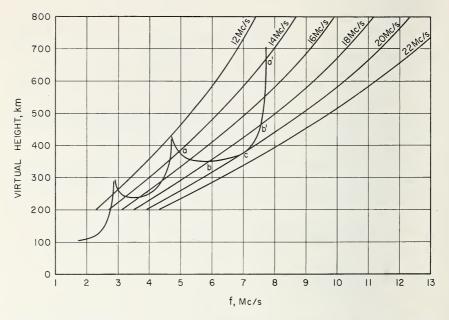


Figure 4.3. Family of transmission curves parametric in frequency for a fixed distance of 2000 km superimposed on an h'f curve.

A flat earth and flat ionosphere are assumed.

which, when presented graphically, is called a transmission curve, which was introduced by Newbern Smith [3]. The application of a transmission curve to an h'f curve is, essentially, a graphical solution of these two equations. A family of such transmission curves for a distance of 2000 km is shown in figure 4.3 and is plotted on the same h'-f grid as a conventional h'f curve. The intersections of a transmission curve, for a given (oblique) frequency f, with the vertical $h'(f_v)$ curve give the virtual heights of reflection of the transmitted waves. In figure 4.3 the three sections of the $h'(f_v)$ curve would correspond to reflections from the E, F_1 , and F_2 layers. A frequency of 14 Mc/s, for example, propagating over a distance of 2000 km could travel by several different paths, two of which would be reflected from the F_2 layer at heights corresponding to the intersections marked a and a' on the $h'(f_v)$ curve with the transmission curve marked 14 Mc/s. The same transmission curve also intersects the F_1 section in two places and the E section in one place.

The corresponding ray paths are shown in figure 4.4; the path corresponding to the lower virtual height of each pair is called the low-angle ray, whereas the path corresponding to the higher virtual height is known

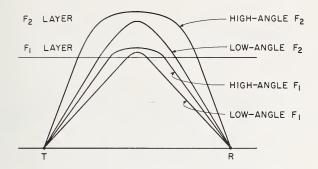


Figure 4.4. Ray paths corresponding to intersections of transmission curves and ionograms.

as the high-angle or Pedersen ray. There would be five different ray paths for a 14 Mc/s wave. The 18 Mc/s transmission curve intersects the F_2 and E layers, but misses the F_1 section; thus no reflection from the F_1 layer is possible on this frequency.

As the frequency f of the parametric curves increases, the points of intersection (bb') come closer together, merging in a tangent contact at one point c. At this point only one ray path would be possible, and 20 Mc/s is the highest frequency which could propagate over 2000 km under these ionospheric conditions. The frequency of the tangent curve is called the maximum usable frequency (MUF). At this point, where the high and low waves merge, focusing takes place and the received signal will be enhanced.

For values of f above 20 Mc/s there is no value of f_{ν} sec ϕ_0 that will satisfy (4.14) and hence no level of reflection. Therefore, the signal is said to skip at the distance concerned (2000 km). The distance for which a given frequency is the maximum frequency is called the "skip" distance for that frequency. Within this distance no signals are received from the ionosphere by the regular process of ionospheric refraction.

In figure 4.5 are shown the paths for various frequencies in the case of a single (F_2) layer. Note that, as the operating frequency is increased, the real height of reflection of the low-angle ray increases, whereas the height of the high-angle ray decreases until they coalesce at the maximum frequency.

In figure 4.6 we see what happens to the ray path (on a given frequency) as the angle of elevation (takeoff) slowly increases. For low angles the propagation path 1 is long. As the elevation increases, the ground range (path 2) decreases until the skip is reached (path 3), after which the range increases rapidly as shown by paths 4 and 5. Eventually

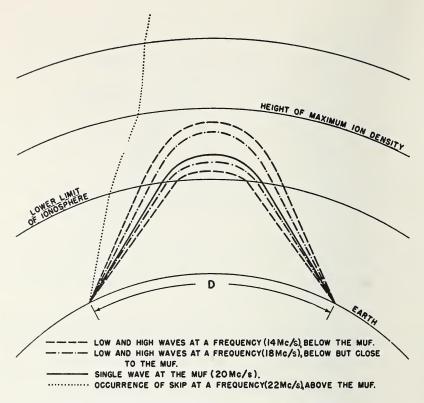


FIGURE 4.5. Ray paths for fixed distance, for different frequencies.

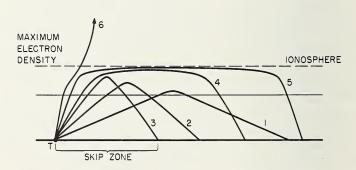


FIGURE 4.6. Ray paths for fixed frequency, with varying elevation.

penetration occurs as shown by path 6. Paths 1 and 2 are the low-ray paths and 4 and 5 are the high-ray paths. The variation of ground range D with angle of incidence ϕ_0 for a parabolic layer is sketched in figure 4.7

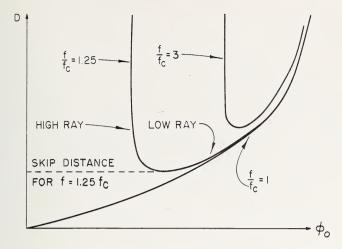


Figure 4.7. Variation of range D with angle of incidence ϕ_0 for a plane parabolic layer.

for various ratios of the operating frequency to the penetration frequency. Note that for a given distance there are two values of ϕ_0 , one corresponding to the low-angle path and the other to the high-angle path. The minimum distance is the skip distance. Note that the high-angle ray is very sensitive to changes in ϕ_0 .

4.3.2. Curved lonosphere

The breakdown of the equivalence theorems in the case of a curved layer requires a modification of (4.15) for obtaining $\sec \phi_0$. The complete modification is very complicated due to the fact that it depends on the electron density profile and, therefore, differs from one set of ionospheric conditions to another. For many practical purposes it is sufficiently accurate to amend the Secant law to

$$f_{\text{ob}} = k f_v \sec \phi_0. \tag{4.16}$$

The correction factor k depends upon the distance and has values ranging from 1.0 to about 1.2 for most practical purposes. The quantity k sec ϕ_0 is often referred to as "sec ϕ_0 corrected."

The value of k is a function of the distance and real height of reflection and is very difficult to calculate. For a given virtual height, it is possible to calculate this factor for the limiting case of two different

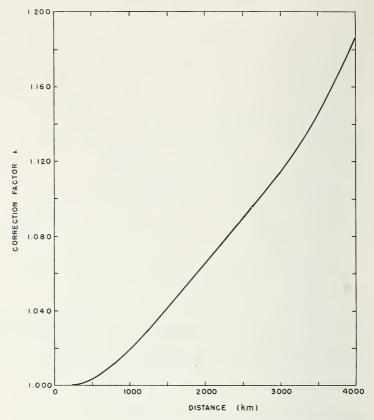


FIGURE 4.8. Variation of correction factor k with distance.

(After B. Wieder, 1955, Some results of a sweep-frequency propagation experiment over a 1100 km east-west path, J. Geophys. Res. 60, 395.)

types of electron density profile, one for which the ray path penetrates deep into the layer, the other for which the wave is reflected from the lower boundary [3]. From a curve drawn between these two limiting values it is possible to obtain a reasonably good empirical correction factor. The variation of this correction factor with distance is shown in figure 4.8.

The primary purpose of transmission curves is the determination of maximum frequencies for a given radio circuit. For this purpose it is possible to construct a type of transmission curve whereby a single curve suffices for each distance and a family of curves parametric in distance can be drawn on a single transparent overlay for use with standard ionograms. This is done by making the frequency scale logarithmic, and requires that the frequency scale of the vertical ionogram be logarithmic also.

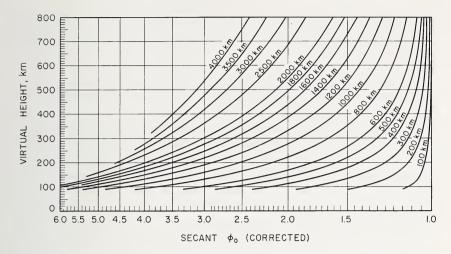


FIGURE 4.9. Logarithmic transmission curves for curved ionosphere.

A family of such standard curves is shown in figure 4.9, in which the factor k sec ϕ_0 is plotted on the same logarithmic scale as the ionogram but with the numbers increasing in the opposite direction to the frequency of the ionogram. The virtual height h' is the same as that on the ionogram. These curves are plotted on a transparent overlay and placed over the ionogram so that the height scales coincide and the curves will, in general, intersect in two places. Opposite the abscissa 1.0 will appear the values of product kf_v sec ϕ_0 or $f_{\rm ob}$. As the overlay slides along the horizontal axis, different values of $f_{\rm ob}$ will be obtained. Note that because of the logarithmic frequency scale, the same number, except for the decimal point, will appear on the transparency opposite the 1.0 index on the logarithmic ionogram scale. The transmission curve for a given distance can be slid along the abscissa until it is just tangent to the h'f curve. The product, as then read at the 1.0 index, is the value of the maximum frequency.

For many purposes, the maximum-usable-frequency factor (M factor) is desired, that is, the ratio of the maximum frequency to the critical frequency of the layer. This may be found directly from the logarithmic scale on the transparency opposite the critical frequency cusp when the transparency is set to read the maximum frequency (i.e., tangent condition).

The transmission curves given in figure 4.9 are most accurate for F_2 layer heights because the factor k is based on typical F_2 layer profiles. Over short distances they will be accurate for any layer because, as the

distance approaches zero, k approaches the value 1.0. The effects of the earth's magnetic field have been neglected in constructing the transmission curves. The errors introduced because of this procedure will be discussed below.

4.3.3. The Parabolic-Layer Method

Instead of calculating maximum frequencies by the use of a vertical h'f curve and a transmission slider, it is possible to fit a parabolic model to the nose of the F_2 layer and, from this, to calculate the maximum frequencies on the basis of analytical formulas [4]. The height h_0 of the bottom of the parabola and its semi-thickness (see sec. 3.3.4.2) are determined from the ionogram. The ground range D cannot be determined for the parabolic layer, but by neglecting small terms [4] it is given by

$$D = \frac{a}{a+h_0} \sin \phi_0 x y_m \ln \frac{1-x^2 \left[y_m/(a+h_0) \right] \sin^2 \phi_0 + x \cos \phi_0}{1-x^2 \left[y_m/(a+h_0) \right] \sin^2 \phi_0 - x \cos \phi_0} + 2a \cot \phi_0 - 2a \sqrt{\cot^2 \phi_0 - (2h_0/a)}, \quad (4.17)$$

where $x = f/f_c$ and ϕ_0 is the angle of incidence.

The maximum frequency and the skip distance can be evaluated from the condition that $dD/d\phi_0=0$. Hence families of curves can be constructed showing the variation of x(M factor) with distance for a range of values of the height of maximum electron density $h_m(=h_0+y_m)$ and for different values of the ratio y_m/h_0 as depicted in figure 4.10. If these

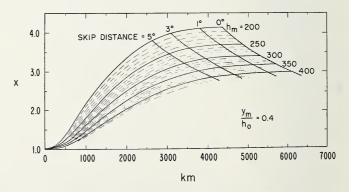


FIGURE 4.10 M factors for a parabolic layer.

(After E. V. Appleton and W. J. G. Beynon, 1940, The application of ionospheric data to radio communication problems, Proc. Phys. Soc. 52, Pt. I, 518; 1947, Proc. Phys. Soc. 59, Pt. II, 58.)

parameters are known, together with f_c , it is possible to determine the maximum frequency by interpolation between curves. To get the most reliable estimate of the factor at any time, it is desirable that h_0 and y_m should be determined directly from ionograms at the midpoint of the path. Such a course is, however, rarely practicable, and it is necessary to predict the most probable values of y_m and h_0 from past history. From the network of ionospheric sounding stations the diurnal, seasonal, and sunspot cycle variations of these parameters are known over most of the world. Comparisons have shown that the results obtained by the parabolic method and by Smith's transmission curves are essentially the same. For two-hop propagation it is necessary to calculate the factor for half the distance.

The transmission theory presented above applies to the case of a spherically stratified ionosphere only. Now, over long transmission paths, the ionospheric parameters may vary appreciably and so the various hops will be of unequal length. The parabolic layer theory has been extended by Kift [5] to include such variations and will be considered later.

4.4. OBLIQUE IONOGRAMS

4.4.1. Experimental Technique

The most convenient way of determining the echo structure of signals transmitted obliquely is by the ionosonde technique but with transmitter and receiver at different ends of the path. From the technical point of view this introduces two problems:

- (a) The repetition frequencies at the sender and at the receiver must be very nearly the same; otherwise the received pulse will "drift" along the time base of the display oscilloscope.
- (b) The frequency of the receiver, as a function of time, must be kept in tune with the sender.

Pulse synchronization (a) is achieved by employing signals from independent stable crystal oscillators. The frequencies of such oscillators are normally in the range 100 kc/s to 5 Mc/s, and electronic frequency dividers are used to obtain the desired repetition frequency. The oscillators can be adjusted (in frequency) either independently with reference to an external standard (e.g., WWV), or else the oscillator at the receiver can be adjusted periodically until the drift of the pulses from the sender is reduced to a minimum. Other synchronization methods used have in-

volved fixed-frequency pulses transmitted from the sender to receiver via a cable [6] and also by the transponder technique in which the received pulses are used to trigger the display time base. Neither of the latter methods has been particularly successful.

The tuning of the transmitter and receiver can be accomplished in several ways. The two most commonly used are

- (1) the accurate shaping of the cams which determine the frequency sweep [7];
 - (2) the synthesis of the frequency from a set of crystal oscillators [8].

With this technique studies of oblique transmission via the ionosphere have been carried out in Canada [9, 10], Germany [11], Great Britain [5, 12], Japan [6], and the United States [13].

4.4.2. Conversion from Vertical to Oblique Incidence

This process is illustrated in figures 4.11a and b. Consider points A, B, C, D, E, and F on the vertical ionogram. For a plane ionosphere and a given distance of transmission we can calculate $\sec \phi_0$ corresponding to the various virtual heights. From this we can obtain $f_{ob} = f_v \sec \phi_0$ and so plot the oblique ionogram shown in figure 4.11b. Note that the vertical scale in figure 4.11b can be related to the equivalent oblique path by the

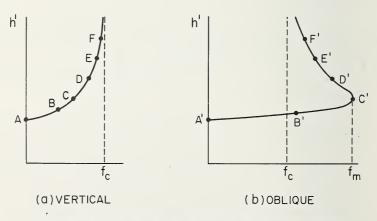


FIGURE 4.11. Corresponding vertical and oblique ionograms.

transformation P'=2h' see ϕ_0 . As we increase the frequency from A to B to C, etc., the virtual height is increasing whereas sec ϕ_0 is decreasing. Between A and C the increase in f_v predominates so that f_{ob} increases, but from C to F the sec ϕ_0 factor predominates and so f_{ob} decreases. The oblique trace A'B'C' represents the low ray, whereas that marked D'E'F' represents the high ray. Notice that the maximum frequency is not reflected from the height of maximum electron density but at a lower height which decreases with increasing obliquity.

4.4.3. Experimental Records

4.4.3.1. Medium Distances

Figure 4.12 shows a sample oblique ionogram taken during magnetically quiet conditions in middle latitudes [14]. The traces are clear, and the maximum frequency of the one-hop F_2 trace is well defined (about 13.5 Mc/s). The high-angle trace (marked H) can be seen for the one-hop trace.

In the description of oblique ionograms it is desirable to eliminate the term maximum usable frequency because of the ambiguity in the meaning of "usable." The following terms will be used:²

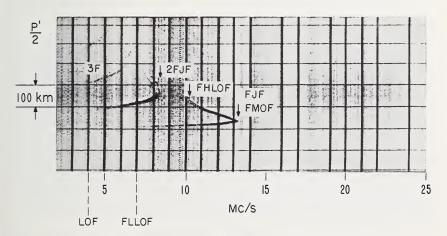


FIGURE 4.12. Ionogram Boulder-Sterling, Sept. 1, 1954, 2012 (90°WMT).

² Recommendations of the Lindau Meeting held in May 1963.

- (1) Maximum observed frequency, MOF, means the highest frequency on which the sounder transmitter signals are *observed* on the ionogram, regardless of the propagation path involved.
- (2) Lowest observed frequency, LOF, means the lowest frequency on which the sounder transmitter signals are *observed* on the ionogram, regardless of the propagation path involved.
- (3) These terms (MOF and LOF) may be used also to describe identifiable modes. For example, $2F_2$ LOF means the lowest frequency, observed on the ionograms, which is propagated by two reflections at the F_2 layer with an intermediate ground reflection. Similarly, $2F_2$ MOF means the highest observed frequency of the two-hop F_2 trace.
- (4) The lowest observed frequency of the high-angle ray may be distinguished from that of the low-angle ray by the letters H and L, respectively. Thus F_2 HLOF is the lowest frequency of the high-angle signal which is propagated via the one-hop F2 path. Likewise, F_2 LLOF is the lowest observed frequency of the corresponding low-angle signal.
- (5) When it is required to distinguish between the ordinary and extraordinary raypaths, an "o" or "x" may follow in parentheses. Thus the F_2 MOF(x) is the maximum observed frequency of the extraordinary wave which is reflected once at the F_2 layer.
- (6) The frequency at which the high- and low-angle rays join will be called the "junction frequency" and will be denoted by JF. Note that this frequency has been called the "classical MUF."

Note that capital letters are used in oblique work in contrast to the small letters agreed upon in vertical soundings.

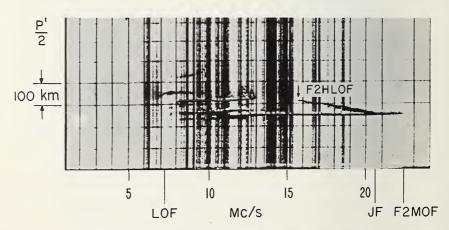


FIGURE 4.13. Ionogram Boulder-Sterling, Nov. 29, 1954, 1321 (90° WMT) showing difference between JF and MOF.

The above terminology is illustrated in figure 4.12 in which the F_2 JF and F_2 MOF are identical. Notice also that LOFs of the multi-hop signals are lower than that of the one-hop. Figure 4.13 shows a case where the MOF is appreciably larger than the junction frequency. This difference is thought to be due to some scattering process in the ionosphere. It ap-

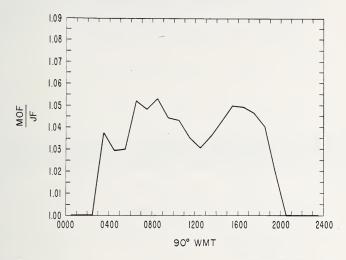
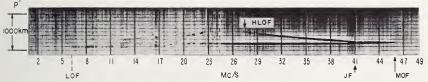


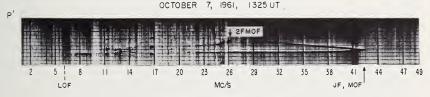
Figure 4.14. Diurnal variation of percent difference between JF and MOF (Boulder-Sterling).

TRIPOLI - ACCRA 3300 km

OCTOBER 3, 1961, 1425 UT



DIFFERENCE BETWEEN MUF AND MOF



IDENTICAL MUF AND MOF

FIGURE 4.15. Ionograms, Tripoli-Accra.

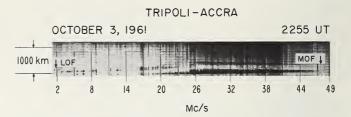


FIGURE 4.16. Ionogram, Tripoli-Accra, showing spread F echoes.

pears to be essentially a winter daytime phenomenon in these latitudes. The diurnal variation of the difference (MOF—JF) for the Boulder–Sterling path is shown in figure 4.14. The two ionograms of figure 4.15 also illustrate that in low latitudes the MOF may be the same as or differ from the junction frequency. The greatest difference between the MOF and the junction frequency occurs during certain equinox evenings on circuits near the magnetic equator. This is illustrated in figure 4.16. The junction, which is obscured by the spread echo, is around 25 Mc/s, whereas the MOF is nearly twice th's value.

It should be realized that the maximum observed frequency and the minimum observed frequency will depend, to some extent, on equipment characteristics.

4.4.3.2. Long Distances

As the transmission distance increases, the complexity of the echo structure tends to increase. Furthermore, signals which may be relatively unimportant over short distances may become determining factors over long distances. An example of this, which has been demonstrated by Canadian workers [15], is the importance of the Pederson ray in determining the maximum frequency. One of their records, reproduced in figure 4.17, shows the one-hop high ray which extends over the approximate frequency range from 42 Mc/s to 48 Mc/s. The occurrence of the Pedersen ray tends to peak near noon at the midpoint when horizontal gradients of electron density along the path are at a minimum.

Some further samples of long-path ionograms are shown in figures 4.18 and 4.19 for the respective paths Delhi–Slough (6730 km) and Ascension Island–Slough (6750 km). The latter illustrates the complexity of the echo structure with long transequatorial paths. See section 4.7 for further discussion of these difficulties.

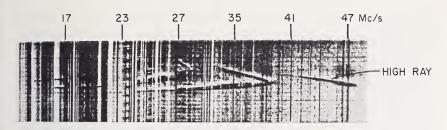


FIGURE 4.17. Ottawa-Slough ionogram, Nov. 14, 1957, 1556 UT.

(By permission of the Chief Superintendent DRTE.)

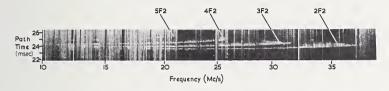


Figure 4.18. Delhi-Slough ionogram, Nov. 7, 1961, 1015 UT.

(Reproduction is by permission of the Controller of Her Brittannic Majesty's Stationery

Office and is by arrangement with the Director of Radio Research.)

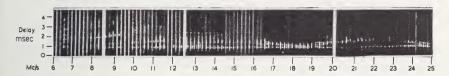


FIGURE 4.19. Ascension Island-Slough ionogram, Mar. 27, 1961, 2118 UT.

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4.5. DEFINITIONS OF MUF

In the early days of ionospheric communications, the term "maximum usable frequency" (MUF) was used without regard to the meaning of "usable." In practice, the maximum frequency usable for a given purpose over a given distance may or may not correspond to the maximum frequency deduced from a vertical ionogram taken at the midpoint of the path. In most cases the practical upper frequency limit is higher than that obtained by the methods described in section 4.3, even when allowance is made for the effect of the magnetic field. The reasons for this involve a number of additional propagation factors, among which are sporadic-E propagation, ionospheric irregularities (large and small), and ground

irregularities in the case of multi-hop propagation over long distances. Such factors also mean that signals may be usable within the nominal skip zone.

In order to clarify and standardize the various meanings of MUF, the International Radio Consultive Committee (CCIR) of the International Telecommunications Union (ITU) adopted the following recommendation (Recommendation No. 318, "Meaning of MUF"):

- 1. That the term "classical MUF" should be used to designate the highest frequency transmitted by ionospheric refraction alone. For the approximation of this value obtained by application of a standard transmission curve or a distance factor, the term "standard MUF" may be used. (For the results of theoretical calculations the term "theoretical MUF" seems to be adequate, and similarly the term "experimental MUF" might be used for the results of special experiments.) If used without reference to a particular mode of propagation, the term "classical MUF" should imply the highest of the classical MUFs of the individual modes.
- 2. That the term "operational MUF" should denote the highest frequency permitting operation at a given time between points under specified working conditions. The operational MUF may be higher than the classical MUF as a result of effects such as ionospheric and/or ground scatter. If known, the modes of propagation involved, including those involving ionospheric and/or ground scatter, should be specified.

4.6. ACCURACY OF MUF CALCULATIONS

4.6.1. Effect of the Earth's Magnetic Field

The sample ionograms in figure 4.20 show clearly the decomposition of the signal into ordinary and extraordinary waves. The wave having the higher junction frequency is the extraordinary wave and the wave

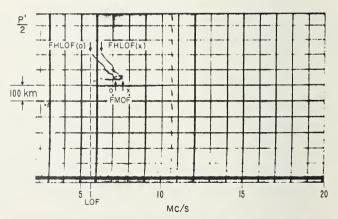


Figure 4.20. Oblique ionogram (Sterling-St. Louis, 1150 km, March 6, 1952, 0901 75° WMT) showing o-x separation of high-angle trace.

with the lower junction frequency is the ordinary wave. Now the transmission curve theory described in section 4.3 ignores the effect of the earth's magnetic field, and the consequence of this is that there is a tendency to underestimate the maximum frequency of the ordinary wave [16]. Of course in the case of east-west propagation along the magnetic equator, where the propagation is transverse, there should be no error in the maximum frequency of the ordinary wave. For quasitransverse propagation, the frequency separation at the maximum decreases with increase of distance of propagation [3]. The variation of this frequency separation with distance for east-west propagation in the United States is shown in figure 4.21, from which we see that the o-x separation falls from 0.8 Mc/s for zero distance to less than 0.2 Mc/s at 3000 km. It must be remembered that this is a statistical result and that the o-x separation depends on the junction frequency itself, the electron density profile, etc. If the propagation is quasi-longitudinal, as in north-south propagation across the magnetic equator, the o-x separation at the junction is independent of distance and is always equal to the gyrofrequency f_H . It is important to remember that the transmission curve should not be applied to the extraordinary trace on the vertical ionogram in order to obtain the maximum frequency of the x wave.

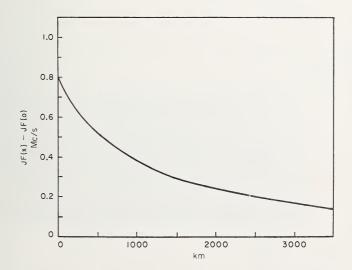


FIGURE 4.21. JF(x)-JF(o) as a function of distance for east-west propagation in the United States.

4.6.2. MUF Extension

It was mentioned in section 4.4.3.1 that for east-west propagation in the United States, and for approximately north-south propagation in Africa, the junction frequency is often ill-defined due to an extension of the trace to higher frequencies. This is sometimes called the MUF extension, and it makes scaling of junction frequencies very uncertain. One way of getting around this difficulty is to define the "junction frequency" as that at which the high- and low-angle traces merge (extrapolated if necessary). Even when this is done it is found that, on the average, measured maximum frequencies defined in this way are about 4 percent higher than the values calculated from midpoint ionograms (standard MUF) for east-west propagation on winter days in the United States. It is of interest to note that the MUFs observed on the Boulder-Sterling path are about 7 percent higher than the calculated values. In summer the difference is about 1 or 2 percent, and this smaller value may be attributed partly due to the absence of the MUF extension on the F_2 trace in summer. The difference (between the junction frequency and the standard MUF) is partly due to errors in the correction factor k (4.16), which is only an average correction over a variety of ionospheric profiles. Still, even this error may not be important in comparison with other factors such as sporadic E, ionospheric and ground scatter, ionospheric distortion (tilts), and so on.

4.6.3. Sporadic E

Figure 4.22 shows that E_s reflections can play a dominant role in determining the maximum frequency. With vertical propagation, re-

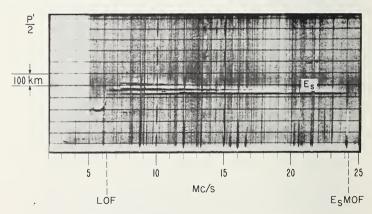


FIGURE 4.22. Ionogram showing E_s reflections.

flections from E_s appear to be essentially specular, in the sense that little or no gradual bending takes place within the layer; this is in contrast to the gradual refraction process involved in reflection from the regular E and F layers. Reflections from E_s are often observed to be only partial, and the reflection mechanism is still in some doubt [17]. From a practical point of view, however, it has been shown that the relationship f_{max} (oblique) = fE_s sec ϕ_0 holds over distances of the order of 1000 km [18]. Over long distances, however, the role of E_s in determining maximum frequencies is not known in detail. Indeed the propagation mechanisms possibly vary with the type of sporadic E. It is relatively rare for E_s to extend over a sufficiently large area of the world to be the sole reflecting layer. It does appear to play a decisive role in modifying the propagation paths involving the regular layers as is illustrated in figures 4.23a and b. For example, the M path involves a reflection at the topside of a sporadic E patch near the midpoint and may be particularly important in high latitudes during periods of high absorption since it avoids a double traverse of the intensely absorbing D region. The occurrence and strength of E_s echoes cannot be predicted with certainty, except near the magnetic equator, so that its value in the design of communications problems is still in an unsatisfactory state.

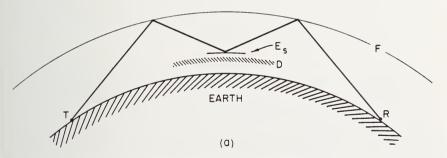


FIGURE 4.23a. M-type reflections.

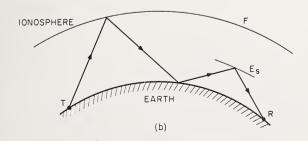


FIGURE 4.23b. N-type reflections.

4.6.4. Ionospheric Scatter

This can play an important part in radio wave transmission. In particular, the presence of spread F raises questions of where, among the confusion of a spread F trace on an ionogram (see sec. 3.3.8.), should a transmission curve be placed in order to give the observed maximum frequency. In middle latitudes the oblique traces are frequently much less spread than those on the corresponding vertical ionogram [13]. This source of error may be much more important than inaccuracies in the transmission curves.

Near the magnetic equator, spread F occurs frequently after sunset and its onset is associated with marked flutter fading on transequatorial circuits. On these occasions the oblique ionograms are characterized by broad traces extending to frequencies much higher than those predicted from vertical ionograms. These traces move in range from one ionogram to the next and are thought to be due to magnetic field-alined irregularities moving from west to east near the magnetic equator [19].

It may also be noted here that ionospheric scatter in the D region, by meteoric ionization and turbulent mixing, plays an important part in the ionospheric transmission of very high frequency waves (30 to 300 Mc/s). (See ch. 8.)

4.6.5. Ground Scatter

Consider the situation illustrated in figure 4.24, in which part of an east-west path is in darkness so that the ionosphere is unable to reflect waves along the path TAR. Because of the higher critical frequencies in the sunlit hemisphere, propagation along the path TCS is possible followed by ground scatter at S. Scattered energy may now be propagated

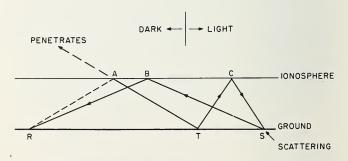


FIGURE 4.24. Importance of ground scatter.

POSSIBLE PROPAGATION PATHS, GREENVILLE-MUNICH

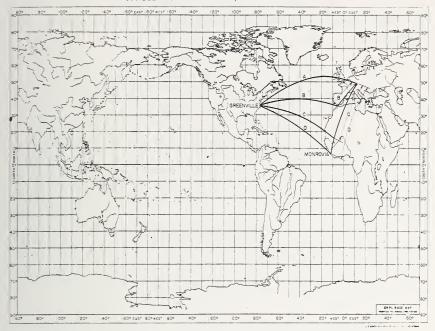


Figure 4.25. Transmission from Europe to the United States via side-scatter over Africa.

(After H. Leighton, unpublished.)

along the path SBR because, although B may be on the dark side of the sunrise line, the angle of incidence (and hence $\sec \phi_0$) is larger than for the path TAR. Alternatively, the signal from T may arrive at R after two reflections in regions off the great circle path where f_0F_2 is higher than along the direct path. This side scatter is illustrated in figure 4.25, which shows how communications can be established between Europe and North America via side scatter in Africa. Such a path gives not only higher maximum frequencies (than the direct path), but also may avoid auroral disturbance effects $\lceil 20 \rceil$.

Ground backscatter can give rise to ionogram records of the type shown in figure 3.32. The signals are reflected from the ionosphere (obliquely), are scattered at the ground, and retrace the same path back to the receiver [21]. The backscatter trace starts off at the vertical-incidence trace of the two-hop extraordinary wave, and it would be expected that the lower edge of the trace gives the maximum frequency corresponding to the equivalent path shown on the ordinate scale, which is related to the skip distance. Such backscatter ionograms provide a convenient means of determining the maximum frequency, over a wide geo-

graphical area, from a single ionosonde. The fact that the echoes can be seen only over a narrow path range is probably due to focusing near the edge of the skip zone.

4.6.6. Ionospheric Tilts

From figure 3.18 we see that the assumption of spherical stratification of the F_2 layer can, under certain circumstances, be invalid. Such distortion of the ionosphere occurs near sunrise and sunset and near the magnetic equator. Clearly, under such conditions, the use of the transmission curves presented above can lead to erroneous conclusions since the ray paths are, in general, asymmetric. In such cases the propagation paths have to be plotted point by point through the ionosphere [22]. When this is done for north-south transmission across the magnetic equator in the 75° west geographic meridian, a path such as that shown in figure 4.26 may be obtained. Some features of this path are:

- (1) There are two ionospheric reflections without an intermediate ground reflection.
- (2) The signal is propagated to long distances with only two transits of the absorbing region, thus giving high signal strength.
- (3) Because the angles of incidence are greater than in the case of a spherically stratified layer the maximum frequencies will be greater.
- (4) There is a marked asymmetry in the path so that the angle of departure (0°) differs from the angle of arrival (about 10).

A complete plot of ground range (D) versus angle of takeoff (Δ) is shown in figure 4.27. This is much more irregular than the single layer plot in figure 4.7 and reveals additional phenomena. For example, owing to a decrease in maximum electron density or to a modification of the angle of incidence, a multi-hop signal may penetrate the ionosphere on one of its hops. Furthermore, when a downcoming ray is just tangent to the earth, a slight increase in takeoff angle may cause the ray to miss the earth and return, after another reflection, at a much greater range. This type of distorted ionosphere gives rise to marked focusing and defocusing of the signals. An instance of focusing can be seen in the two-hop signal between angles of about 13° and 24° . All the energy radiated between elevation angles of about 13° and about 23° is concentrated in a range of a few hundred kilometers.

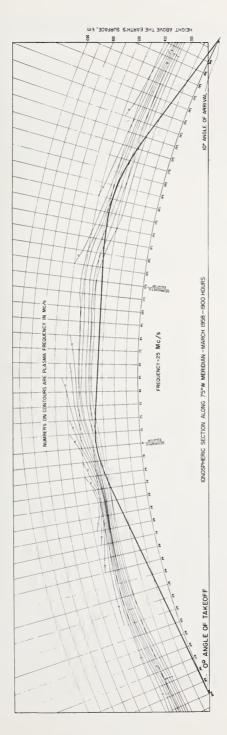


FIGURE 4.26. Transequatorial ray path.

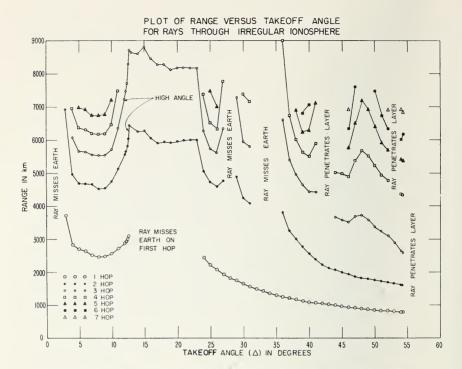


Figure 4.27. Range versus elevation plots for transequatorial propagation.

March 1958, 1900, 75° WMT, 15 Mc/s

4.7. SOME PROBLEMS IN LONG-DISTANCE TRANSMISSION

4.7.1. Path Identification

When the distance of transmission is much greater than 4000 km, considerable difficulties arise in the identification of the propagation paths. We have already seen in figure 4.17 that, for a distance of 5300 km, the high-angle one-hop F_2 path can be important. Also sporadic E may play a vital role in reflecting waves, sometimes to the advantage of the communicator and at other times to his disadvantage since it may cut off a usable signal. It is useful to identify paths by the number of hops and the layers from which the reflection takes place.

The following terminology is suggested for the description of such paths.³

³ Recommendations of the Lindau Meeting, May 1963.

- (1) For propagation paths involving reflections by different layers, the reflections (or hops) should be specified in order of their position with respect to the transmitter.
- (2) A dash will be used to represent a ground reflection. The absence of a dash will then show up M type reflections (fig. 4.23a) and supermodes (fig. 4.26). Thus figure 4.23a and 4.23b, respectively, would be described as $F_2E_sF_2$ and F_2 - E_s . Figure 4.26 is described by F_2F_2 and figure 4.28 by FE_sF - E_s -F. Note that $2F_2$ means a two-hop F_2 path and 3E means a three-hop E path with intermediate ground reflections.

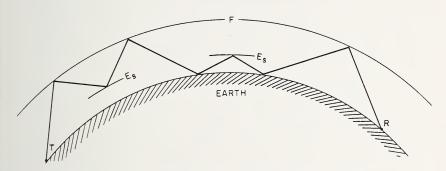


Figure 4.28. Long-distance paths involving F and E_s reflections.

Assuming thick parabolic F_2 layers, the parameters of which are allowed to vary from one hop to another, and a thin E_s layer, Kift [5] has shown how the paths can be deduced from measurements of angle of arrival and of the time delay in excess of that which would be required for the signal to travel around the earth's surface between sender and receiver. Kift plots angles of elevation and excess time against ground range and obtains mode plots, an example of which is shown in figure 4.29 for the path Ascension Island to Slough, distance 6750 km. At this range one sees that the composite signal received at Slough may have traveled along the following paths: $2E_s-F_2$, $M-F_2$, $G-F_2$, $G-2F_2$, $F_2-E_s-3F_2$, F_2 -2 E_s -3 F_2 , 5 F_2 with a possible high angle 5 F_2 , where a G (guided) path is one involving reflections between E and F. It is easy to see that, in general, the composite signal has a very complex structure, and simple inspection of an oblique ionogram is usually insufficient to reveal the actual paths. Even with ray tracing there may be ambiguity because of the close time spacing of the various echoes and takeoff angles. A similar identification can be made with figure 4.26 if equivalent path is plotted against elevation angle.

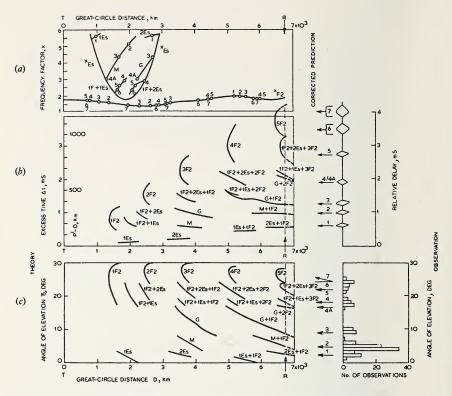


FIGURE 4.29. 19.87 Mc/s mode plots: Ascension Island-Slough, April 11, 1956, 0930-1030 UT.

(After F. Kift, 1960, The propagation of high frequency radio waves to long distance, Proc. IEE 107B, 127.) (a) x plot, hm F₂ fairly constant at 340 to 360 km. (b) Mode-delay plot. (c) Mode-angle plot.

4.7.2. E-Layer Cutoff Frequencies for F_2 Propagation

The ray path of a signal reflected from the F_2 layer penetrates the E layer at one or more points; hence, in order for the signal to traverse the entire path, the frequency must be sufficiently high to penetrate the E layer at each of these points. The lowest such frequency is called the E cutoff frequency.

Referring to figure 4.30, a wave traveling up to the F layer intersects the E layer at P. If the frequency is below the E layer penetration frequency, the wave is reflected and returns to earth at B. This conconstitutes a one-hop E path for the range TB, the radiation angle of

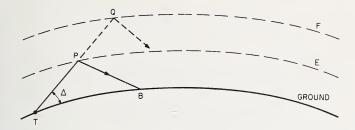


FIGURE 4.30. E layer cutoff.

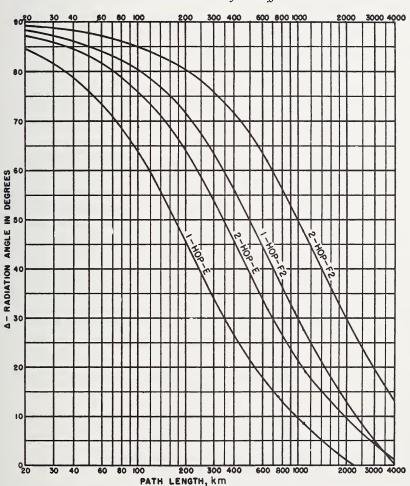


Figure 4.31. Radiation angle versus path length, based on virtual reflection heights. ${\it E}~layer-105~km;~F_2~layer-320~km.$

which is the same as that for the F_2 path. The penetration frequency at the point P is, therefore, equal to the E maximum frequency for the range TB.

To determine the range TB, we need to know the angle of elevation Δ as a function of distance. This is given in figure 4.31 for assumed heights of 105 km (E) and 320 km (F_2) . From the location of the point P, we determine the appropriate E critical frequency and, hence, the corresponding E layer maximum frequency. When this is done at each E layer penetration point, the highest frequency is the E layer cutoff frequency for the particular path.

4.7.3. Optimum Working Frequency

In designing a communications circuit involving F_2 layer transmission, it is desirable to use as high a frequency as possible in order to reduce the ionospheric absorption (which decreases as the square of the operating frequency). The monthly median maximum frequency is unsuitable because it would be reflected 50 percent of the time only. Hence, to allow for day-to-day changes in critical frequency, it is customary to use 0.85 of the monthly median, and it is called the optimum working frequency-FOT from the French initials. It is not necessarily the frequency of maximum signal or minimum time dispersion. It is based on a statistical result that it lies below the maximum frequency 90 percent of the time. That this definition of "optimum" may be misleading in individual cases is illustrated by the oblique ionogram in figure 4.17. The maximum frequency is close to 48 Mc/s so that the 85 percent frequency is 40.8 Mc/s. Thus the "optimum" frequency would fall in the middle of the "dead" space between the maximum frequency of the twohop F signal and the minimum frequency of the one-hop Pedersen ray.

4.8. MULTIPATH PROPAGATION TIMES

The oblique ionograms above show that, as the maximum frequency is approached, the time dispersion of the signal decreases. This time dispersion can be of considerable importance in the transmission of information at high speeds because the maximum rate (in binary units per second) is roughly equal to the reciprocal of the range of multipath propagation times ΔT_m , where ΔT_m is a function of frequency, path length and location, local time and season.

The multipath reduction factor (MRF) is defined as the lowest percent of the MUF for which the range of multipath propagation times is less than a specified value [23]. The MRF thus defines a frequency above which a specified minimum protection against multipath is provided.

From experimental data (oblique ionograms) for a number of paths in different geographic locations, MRF curves have been deduced, statistically, and are presented in figure 4.32. It can be seen, in the ionograms shown above, that the multipath spread approaches zero at the maximum frequency. It can be seen also that the spread may be significantly reduced when operating on lower frequencies using such signals as the high-angle ray in figure 4.17 or on the E_s ray in figure 4.22. It is conceivable that the rate of transmission of information could be increased by a factor of 100 over normal values by a judicious choice of operating frequency.

To illustrate the use of the MRF curves, consider a path length of 2500 km. When operating on a frequency between 1.0 and 0.85 of the maximum, the multipath spread should be less than 500 μ sec. On frequencies between 0.65 and 0.85 of the maximum, the spread will be less than 1 msec, and in the range 0.43 to 0.65 of the maximum, the spread will be between 1 and 2 msec. There is a frequency on which the spread is a maximum. This frequency is given by figure 4.32, and the value of the maximum multipath spread is shown in figure 4.33. For a 2500-km path, the maximum time dispersion is about 3 msec. For a 1000-km path, the maximum dispersion is about 5 msec, and occurs at a value of MRF \approx 56 percent.

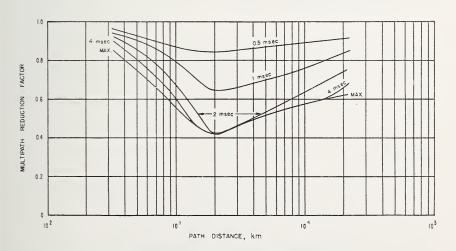


FIGURE 4.32. Multipath reduction factor.

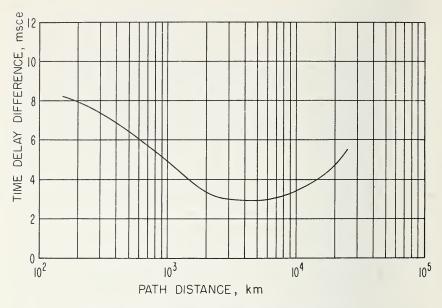


FIGURE 4.33. Maximum expected time delay difference.

4.9. RAY PATHS

4.9.1. Without Magnetic Field

It is sometimes necessary to know the path of energy flow between a transmitter and a receiver. This is particularly important in the analysis of complex pulse-echo patterns observed on oblique ionograms. Ray tracing is often necessary to establish the feasibility of transmission of energy from one point to another, and to predict the extent to which focusing (or defocusing) modifies the distribution (over the ground) of the reflected energy. A knowledge of the ray path is necessary for the calculation of time of flight, signal strength, phase, and polarization of the reflected wave.

It is convenient to think of the ray path as the trajectory of a packet of waves limited in both frequency and in space. Consider the case of such a wave packet having a takeoff angle (at the earth's surface) Δ and incident on a spherically stratified ionosphere in which the refractive index is varying slowly with height as illustrated in figure 4.34. Let x be the range, along the ground, corresponding to a point on the ray path

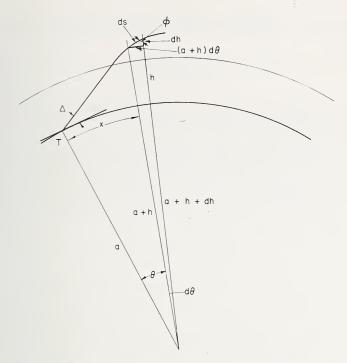


Figure 4.34. Ray path geometry for a spherically stratified ionosphere.

at a height h above ground, and let x subtend an angle θ at the center of the earth. From figure 4.34

$$(a+h) \ d\Theta = \tan i \cdot dh, \tag{4.18}$$

together with Snell's law (see 4.9)

$$\mu(a+h)\sin i = a\cos \Delta, \tag{4.19}$$

this gives

$$\Theta = \int \frac{a \cos \Delta \, dh}{(a+h) \sqrt{\mu^2 - \left(\frac{a}{a+h}\right)^2 \cos^2 \Delta}} \,. \tag{4.20}$$

One solution to the problem of ray tracing is to approximate the electron density profile by a suitable model in order to evaluate, analytically,

the integral for Θ . This is relatively simple to do in the case of a plane earth and plane ionosphere when the ground range x is given by

$$x = \int \frac{\cos \Delta \, dh}{\sqrt{\mu^2 - \cos^2 \Delta}} \,. \tag{4.21}$$

The solutions of (4.21) for some of the more commonly used models are given by Budden [24, ch. 11].

When the curvature of the ionosphere is taken into account, the problem is more difficult. Appleton and Beynon [4] assumed a layer shape which is derived from a parabola by neglecting small terms, and they obtained (4.17) for the ground range. In general, however, it is not possible to find suitable analytic functions which represent adequately the electron density profiles [25, 26]. Under such circumstances the ray path has to be computed by dividing the profile into a number of laminae and postulating an analytic N(h) function within each lamina. As the number of laminae used is increased, the result becomes less and less dependent upon the form of the assumed distribution within each segment.

An interesting graphical method has been developed by Chvojkova [27] which is illustrated in figure 4.35 where, for clarity, the refracting shells are separated by infinitesimal non-refracting shells. From Snell's law ($\mu r \sin i = a$ constant) we see that, outside the ionosphere, the ray direction must always be tangent to the surface of a sphere of radius $r \sin i_0$; and at any point inside the ionosphere at which the refractive index is μ , the ray is tangential to a sphere of radius $(r/\mu) \sin i_0$.

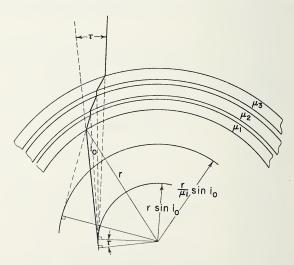


FIGURE 4.35. Chvojkova's construction.

4.9.2. With Magnetic Field (Waves and Rays)

From the point of view of ray tracing, the main effects of the magnetic field are

- (1) Ordinary and extraordinary waves are produced;
- (2) The direction of energy flow (ray direction) differs, in general, from the phase normal;
- (3) The refractive index depends upon the angle of refraction, so that it is not possible to solve Snell's law directly.

The angle α between the directions of phase propagation and energy propagation is given by (2.123), namely

$$\tan \alpha = -\frac{1}{v} \frac{dv}{d\theta} = \frac{1}{u} \frac{d\mu}{d\theta}.$$
 (4.22)

Substituting the expression for $\mu(2.77)$ in (4.22) we obtain

$$\tan \alpha = \pm \frac{(\mu^2 - 1) Y_T Y_L}{\sqrt{Y_T^4 + 4(1 - X)^2 Y_L^2}}.$$
 (4.23)

The + and - signs refer to the ordinary and to the extraordinary rays respectively. Note that α is of opposite sign for the ordinary and extraordinary waves except when the refractive index of one of the rays is greater than unity. Furthermore, the sign of tan α changes as θ goes through 90°.

Bremmer [28] has summarized the ray behavior as follows:

- (a) The wave normal is parallel to the plane of incidence and satisfies Snell's law.
- (b) The ray is situated in the plane through the wave normal and the earth's magnetic field.
- (c) The angle α measured from the wave normal to the ray, is given by (4.23).

Before considering some actual ray paths, it is of interest to consider the implications of these rules. First they imply that, as a wave packet penetrates into the ionosphere, it "slips" sideways in a direction parallel to the magnetic meridian. For upgoing waves the extraordinary ray is (for $\mu < 1$) deflected towards the magnetic equator, whereas the ordinary ray is deflected away from the magnetic equator. Second, let us consider (4.23) in the case of waves propagating vertically. We see that tan α is

zero under the following conditions:

Y=0, no magnetic field $\theta=0^{\circ},\ 180^{\circ}$ propagation at the magnetic poles $\theta=90^{\circ}$ propagation at the magnetic equator $\mu^2=1.$

At the levels of reflection, $\mu=0$ and X=1 for the ordinary wave and $X=1\pm Y$ for the extraordinary waves. This gives

$$\tan \alpha_0 = -\cot \theta, \tag{4.24}$$

$$\tan \alpha_x = \frac{\sin \theta \cos \theta}{\sqrt{\sin^4 \theta + 4 \cos^2 \theta}} = \frac{\sin \theta \cos \theta}{1 + \cos^2 \theta}.$$
 (4.25)

Hence, at reflection, the ordinary ray is perpendicular to the earth's magnetic field. Note that α_x depends on the direction, but not on the magnitude, of the earth's magnetic field.

4.9.3. Some Sample Ray Paths

4.9.3.1. Vertical Propagation

Applying Snell's law in a plane stratified ionosphere, we find that the wave normal is always vertical. The lateral deviation D at a height h is given by

$$D = \int_0^h \tan \alpha \, dh. \tag{4.26}$$

In the general case this expression is too complicated to solve analytically, but D can be found by dividing the electron density profile into a number of slabs and determining the mean value of $\tan \alpha (\tan \alpha \operatorname{say})$ for each slab, then summing, i.e.,

$$D = \sum_{i} \overline{\tan \alpha_i} \Delta h_i, \tag{4.27}$$

where Δh_i is the thickness of the *i*th slab.

Ray paths over Boulder, Colo., which have been calculated by this method, are shown in figures 4.36 and 4.37. Consider first the paths on frequencies greater than the gyrofrequency (=1.5 Mc/s approx.). The

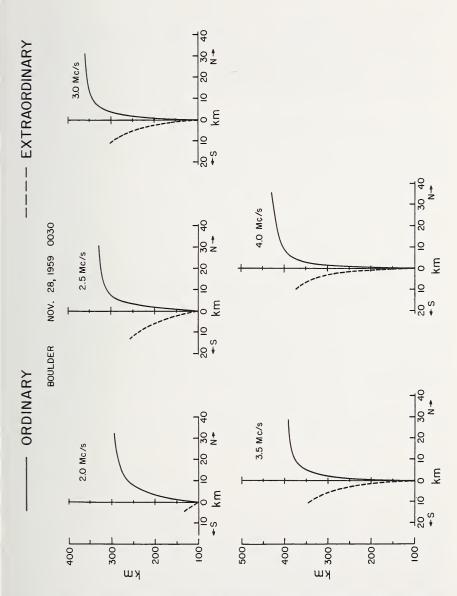
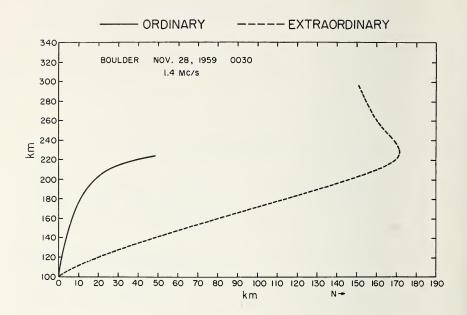


FIGURE 4.36. Some ray paths with normal incidence over Boulder on frequencies above the gyrofrequency.



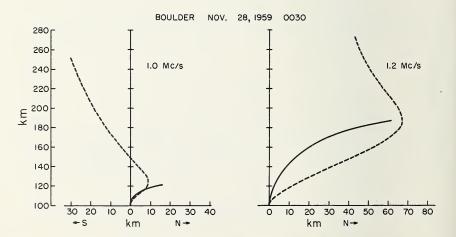


Figure 4.37. Some ray paths with normal incidence over Boulder on frequencies less than the gyrofrequency.

following features are of interest:

- (1) The ray paths lie entirely in the magnetic meridian.
- (2) On a given frequency, less than the penetration frequency, the deviation (to the north) of the o ray at reflection is always greater than that (to the south) of the extraordinary ray at its level of reflection.
- (3) On a given frequency and for the same real height, the deviation of the extraordinary ray is greater than that of the ordinary ray.
- (4) Most of the deviation of the ordinary ray takes place relatively close to the reflection level.

On a frequency less than the gyrofrequency, the situation is a little different. The ordinary wave behaves much the same as before, but the behavior of the extraordinary (z) wave is different. In figure 2.9 we see that, for 0 < X < 1, the refractive index of the extraordinary wave is greater than unity so that in this range $\mu^2 - 1$ is positive and the ray is deflected to the north. For values of X between 1 and 1 + Y (reflection), μ is less than unity and the ray veers to the south. Whether the point of reflection lies to the north or the south of the point of entry will depend on the frequency and on the profile. The path of the downcoming wave is identical with that of the upgoing wave. Owing to electron collisions, these paths will be modified slightly, the modification becoming more pronounced as the wave frequency approaches the gyrofrequency.

On a frequency close to the penetration frequency of the F_2 layer, the ordinary ray may be deviated by 50 or 60 km; however, the deviation within the layer falls off rapidly as the frequency increases above f_0F_2 . For example, with $f_0F_2 = 10$ Mc/s the deviation, with a complete passage through a Chapman layer on a frequency of 40 Mc/s, is of the order of 0.1 km.

Because of the lateral deviations, the ordinary and extraordinary rays, in practice, sample slightly different electron density profiles.

4.9.3.2. Oblique Paths

For fairly short distances of transmission, the plane containing the emergent ray is parallel to, but not necessarily coincident with, the great circle plane containing the incident ray. The incident and emergent planes are coincident for exactly east-west propagation in all latitudes and for north-south propagation in a magnetic meridian. Some ray paths have been calculated in the case of approximately east-west propagation in the United States with a parabolic distribution of electron density with height and the dipole approximation (earth centered) to the earth's

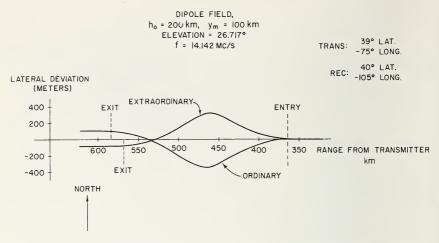


Figure 4.38. Horizontal projection of ray paths in a parabolic layer for geographically east-west propagation in the United States.

magnetic field. The projections of the paths on to a horizontal plane are shown in figure 4.38. The paths are twisted, veering first in one direction and then in the other. The maximum deviations are about 0.3 km, and the net deviations, at the point of exit from the ionosphere, are only about 100 m. Furthermore, the ordinary and extraordinary rays are, roughly, mirror images of each other. The deviation tends to increase with operating frequency because of the increase in depth of penetration of the ray into the layer; however, the deviations with oblique propagation are much less than with vertical propagation.

With propagation in the magnetic meridian (north-south) there is no lateral displacement of the ray, but the point of energy reflection is, in general, displaced from the center of the path. The point of reflection of the ordinary wave is displaced to a higher magnetic latitude than the midpoint and vice versa for the extraordinary wave.

Ionospheric ray paths can be calculated in a variety of ways. Those more commonly used are the Booker quartic [29], the iterative method [30], Haselgrove's equations [31], Titheridge's approximate method [32], and Poeverlein's graphical construction [33].

Poeverlein's method is of interest because it illustrates the existence of the "spitze." It is a graphical method and depends on the fact that, for a refractive index surface,⁴ the radius vector gives the wave normal

⁴ The refractive index surface is the locus of end points of a vector whose magnitude is the refractive index and whose direction is the direction of phase propagation.

direction and the normal to the surface is the ray direction, as shown in figure 4.39. The wave normal direction is known from Snell's law, so the ray direction can be obtained from the construction shown in figure 4.39. From this direction the next point on the ray is determined and the procedure is repeated. Note that the condition for energy reflection is given by a point such as A where the normal to the μ surface is horizontal, but where the wave normal is not, in general, horizontal.

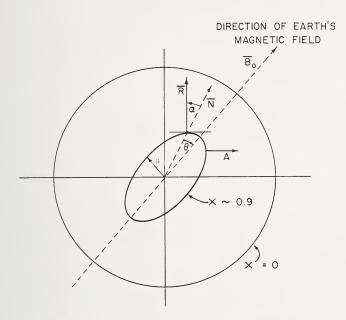


FIGURE 4.39. Illustrating Poeverlein's construction

Direction in which the ray R is normal to the refractive index surface. N, the wave normal, is given by the direction of the radius vector. Curves not drawn to scale.

Using this construction, with oblique propagation in the magnetic meridian, Poeverlein showed that, for angles of incidence less than a certain critical value ϕ_c (where $\sin \phi_c = \sqrt{\lceil Y/(1+Y) \rceil} \cos I$, I = dip), the path of the ordinary ray never becomes horizontal, but has a cusp at the level X=1. This phenomenon, called the "spitze," is illustrated by the ray paths in figure 4.40. An excellent description of the behavior of rays for many special cases is given by Budden [24, ch. 13] where he shows that on frequencies greater than the gyrofrequency the spitze is not exhibited by the extraordinary ray.

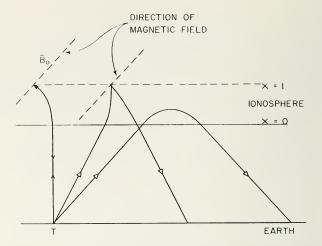


FIGURE 4.40. Sample ordinary ray paths for oblique propagation in magnetic meridian, showing the Spitze.

Not drawn to scale.

4.9.3.3. Topside Soundings

With the advent of artificial earth satellites it is necessary to consider reflections from the topside of the ionosphere and transmission between satellites and ground.

Some ray paths for waves having the vertical direction of phase propagation are shown in figure 4.41 for various heights above the peak of a Chapman layer in the northern hemisphere. Note that the ordinary ray is deviated to the south and the extraordinary ray is deviated to the north. As the height of the satellite decreases, i.e., as the surrounding electron density increases, first the extraordinary wave and second the ordinary wave get "imprisoned" in the satellite because the plasma is overdense to waves of that frequency (e.g., 5 Mc/s). When the satellite is near its reflection level, the ordinary wave energy slides almost sideways. An additional path (the z path) is possible, which may be understood by reference to figure 2.9. For Y < 1 it will be seen that there is a branch of the extraordinary curve lying in the range

$$\frac{1-Y^2}{1-Y_t^2} < X < 1+Y.$$

Normally this wave cannot originate except from a source embedded in

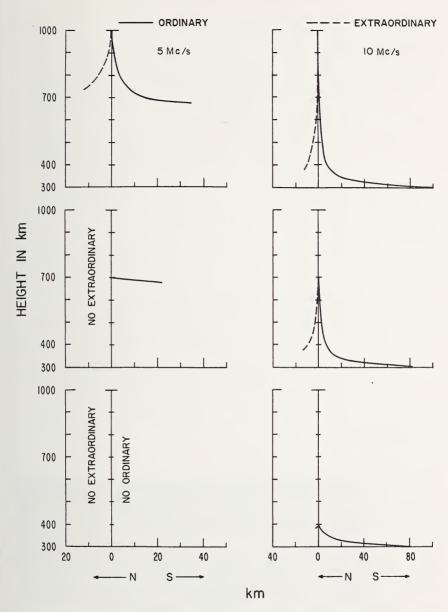


Figure 4.41. Some ordinary and extraordinary ray paths from a topside sounder located at heights of 1000 km, 700 km, and 400 km in a Chapman layer.

Penetration frequency (o wave)=10 Mc/s f_H =0.75 Mc/s Dip=72.9°.

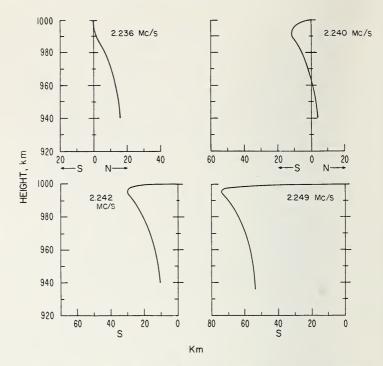


Figure 4.42. Some z ray paths from a topside sounder located at a height of 1000 km in a Chapman layer.

Penetration frequency (o wave)=10 Mc/s $$f_H\!\!=\!\!0.75$ Mc/s Dip=72.9°

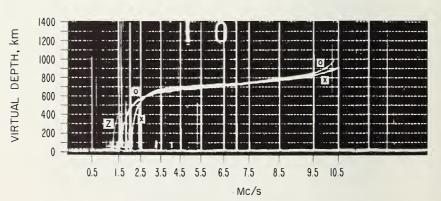


FIGURE 4.43. Topside ionogram, Singapore, Nov. 19, 1962, 0810 UT.

(Reproduction is by permission of the Controller of Her Brittannic Majesty's Stationery Office and is by arrangement with the Director of Radio Research.)

the plasma. To get some idea of what the ray paths may look like we notice that $\mu^2 > 1$ near $X = (1 - Y^2)/(1 - Y_L^2)$ and μ drops below 1 as it approaches reflection. The quantity $(\mu^2 - 1)$ and, hence α , will change sign. The ray path veers first to one side and then to the other, as illustrated in figure 4.42. The existence of the z-wave has been confirmed in recent soundings of the topside—see figure 4.43.

4.9.3.4. Satellite-to-Ground Paths

To a first approximation on very high frequencies, the effective ionosphere exists only within a definite range of heights, and we shall assume (for the sake of discussion only) that the refractive index is unity both above and below this range. Consider a wave of frequency considerably greater than the critical frequency; at very oblique incidence the rays are reflected (see fig. 4.44) but within a cone of semiangle $\phi_0 = \sin^{-1} \mu_m$ all rays will penetrate the ionosphere. The refractive index $\mu_m [= \sqrt{1-(f_c/f)^2}]$ is the value at the height of maximum electron density in the absence of the earth's magnetic field and collisions. This blocking effect of the ionosphere for zenith angles greater than a critical value is sometimes called the "iris" effect.

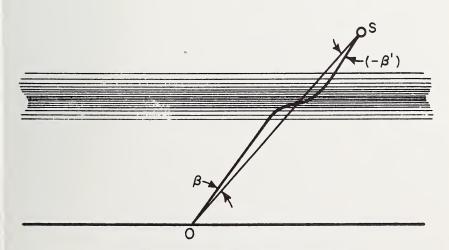


FIGURE 4.44. The iris effect (plane ionosphere).

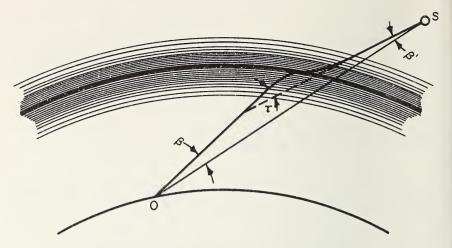


FIGURE 4.45. Effect of ionosphere curvature on angular error.

With angles less than ϕ_0 , the ray is bent in the layer and so the angle of elevation at the ground is increased by an amount β as seen in figure 4.44. The angle β is called the "angular error at the observer" and, in this case, it is equal to $-\beta'$, the "angular error at the source."

The effects mentioned above for a plane-stratified ionosphere are modified slightly by the curvature of the ionosphere. The geometry is shown in figure 4.45 and shows that the total bending (i.e., the difference in direction of the ray at the source and at the observer), $\tau = \beta + \beta'$, is no longer zero. Thus the total bending which occurs in a ray passing through the ionosphere is a second-order effect, since the bending of the ray on entering the ionosphere (from above) is compensated for (actually, overcompensated for) by the bending on leaving the ionosphere. With the exception of the special case of radio astronomy, where the source-observer distance is essentially infinity, the angular error at the observer generally differs from, and may be greater or less than, the total bending.

It can be seen that the overall effect of the refracting iris is to focus rays from a large section of the sky into a relatively narrow cone. From the point of view of signals received at the earth from a satellite, this means a smaller signal/noise ratio (see ref. [28], ch. X, sec. 8).

The effect of the earth's magnetic field is to produce two images of the satellite—ordinary and extraordinary. In the general case of propagation making an angle (non-zero) with a magnetic meridian, the two rays are deviated in opposite direction from the plane of incidence but the lateral deviation is much smaller than the refractive effects in the plane of incidence. Thus we get a good approximation to the actual ray

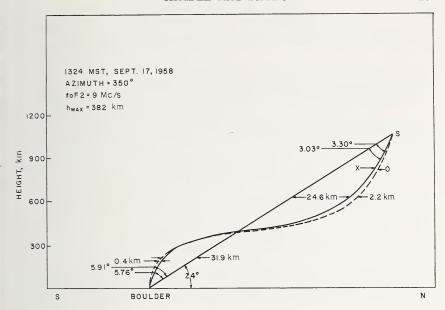


FIGURE 4.46. Ray paths (o and x) from satellite to ground near Boulder, Colo.

(By permission of R. S. Lawrence and D. J. Posakony, 1962, A digital ray-tracing program for ionospheric research, Space Research II, Proc. 2d Intern. Space Sci. Symp., Florence, North Holland Publ. Co.)

path if we project the ray on to the vertical plane of incidence. In figure 4.46 is an example, projected on a vertical plane (not to scale), of ray paths from a 20 Mc/s satellite-borne transmitter near Boulder, Colo. The total bending along the extraordinary ray always exceeds the total bending along the ordinary ray. In figure 4.46, for example, the total bending of the extraordinary wave is 2°.73 while that of the ordinary wave is only 2°.61. Notice that this relationship does not necessarily mean that the angular errors at the observer are similarly related. Several methods are available for estimating the angular error at the observer in the absence of the earth's magnetic field [34, 35].

The above treatment assumes a spherically stratified ionosphere so that horizontal gradients in electron content are ignored. The treatment of refraction in the presence of ionospheric distortion is a complicated process, except in cases of simple models. One such model is that of a "wedge" of electrons. For angles of incidence near the zenith the relationship between the wedge refraction τ and the horizontal gradient of total electron content is given by [36]

$$\tau = \frac{e^2}{8\pi^2 \epsilon_0 m f^2} \cdot \frac{\partial}{\partial X} \int_0^\infty N \, dh. \tag{4.28}$$

Data on ionospheric irregularities can be obtained from measurements on radio-star signals [37, 38], and on satellite radio signals [38].

4.9.4. Propagation Effects Associated With Ray Paths

(a) Phase path P is given by

$$P = \int \mu \cos \alpha \, ds. \tag{4.29}$$

(b) Group path P' is given by

$$P' = \int \mu' \cos \alpha \, ds. \tag{4.30}$$

(c) Total absorption L is given by

$$L = \int \kappa \cos \alpha \, ds, \tag{4.31}$$

where μ and μ' are the phase and group refractive indices respectively and κ (kappa) is the absorption per unit length of path.

It is of interest to note that, when the magnetic field is absent, the relationship between μ , μ' , and L is given by

$$L = \frac{\nu}{2c} (P' - P) \tag{4.32}$$

provided that ν (the collision frequency) is independent of height.

4.9.5. Faraday Rotation

4.9.5.1. Rotation of the Plane of Polarization

A linearly polarized wave can be considered as the resultant of two vectors, of equal amplitude, rotating in opposite senses with the same angular speed. In the case of quasi-longitudinal propagation in the absence of absorption, the two characteristic waves (ordinary and extra-

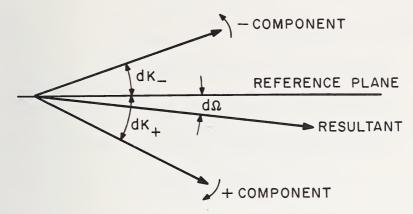


FIGURE 4.47. Faraday rotation.

(Propagation is perpendicular to the plane of the paper.)

ordinary) are essentially circularly polarized. These waves, being characteristic waves, suffer no change of polarization as they propagate through the medium but, because they have different phase velocities, the plane of polarization of the resultant linearly polarized wave rotates gradually. This phenomenon is known as Faraday rotation and its magnitude can be computed as follows.

Consider an element of path length ds in which the rotation of the electric vectors of the o and x waves are dK_+ , dK_- respectively (see sec. 2.5.3.). Figure 4.47 shows the relationship between dK_+ , dK_- and $d\Omega$, the angle through which the plane of polarization rotates in the distance ds. From this figure we have

$$d\Omega = \frac{1}{2}(dK_{+} - dK_{-}),$$

$$\Omega = \frac{1}{2}(K_{+} - K_{-}),$$
(4.33)

where

$$K_{+} = \frac{2\pi}{\lambda_{0}} P_{+} = \frac{2\pi}{\lambda_{+}} ds,$$
 (4.34)

and

$$K_{-} = \frac{2\pi}{\lambda_0} P_{-} = \frac{2\pi}{\lambda_{-}} ds,$$
 (4.35)

where the P's are the phase paths, λ 's are the wavelengths within the ionosphere, and λ_0 is the free space wavelength. Note that we have im-

plicitly set $\cos \alpha = 1$, which restricts the discussion to frequencies well above the plasma frequency.

From (4.33), (4.34), and (4.35) we obtain

$$\Omega = \frac{\pi}{\lambda_0} \int (\mu_+ - \mu_-) ds. \tag{4.36}$$

In the case of quasi-longitudinal propagation we have (sec. 2.3.3.2)

$$\mu_{\pm} = \left(1 - \frac{X}{1 \pm Y_L}\right)^{\frac{1}{2}}.\tag{4.37}$$

On very high frequencies $\mu=1$ and, on expanding this expression, neglecting the high order terms, and reducing, we get

$$\mu_{+} - \mu_{-} \approx X Y_{L} = X Y \cos \theta. \tag{4.38}$$

In terms of the mks units, (4.36) now becomes

$$\Omega = \frac{Q}{f^2} \int_{S} NB_0 \cos \theta \, ds, \tag{4.39}$$

where $Q = 2.97 \times 10^{-2}$.

It is important to remember that several approximations have been made in deriving this expression and its validity becomes questionable as θ increases and it breaks down completely when quasi-longitudinal propagation gives way to the quasi-transverse type. Nevertheless it has proven very valuable in the interpretation of Ω measurements in terms of the total electron content $\int N \, ds$.

Measurements of Faraday rotation Ω have been made on signals from artificial satellites [39] and from radar reflections from the moon [40].

In moon echo experiments the frequencies are usually high enough (several hundred megacycles per second) so that (4.39) is accurate. To find the total electron content in a unit vertical column of the ionosphere it is possible to replace the path element ds by dh sec i where i is the local zenith angle (between the ray and the vertical) and dh is an element of height. In this case (4.39) becomes

$$\Omega = \frac{Q}{f^2} \int_0^h NM \, dh, \qquad (a)$$
(4.40)

where

$$M = B_0 \cos \theta \sec \phi$$
. (b)

It must be remembered that (4.40) applies to one passage through the ionosphere.

Although further restricting the generality of the expression, it is convenient to take M as the constant in that part of the ionosphere (0 to 1000 km, say) in which the bulk of the rotation occurs, and to write

$$\Omega \approx \frac{Q\bar{M}}{f^2} \int_0^{1000} N \, dh, \tag{4.41}$$

for one-half the total rotation of a moon echo. \bar{M} is a weighted average of M $\lceil 41 \rceil$.

In the case of frequencies below about 40 Mc/s, such as those often used for satellite beacon measurements, (4.39) is only approximate and ray tracing methods are required to determine the electron content by a trial and error process.

4.9.5.2. Some Results of Faraday-Rotation Experiments

These measurements have given information about the electron density profile above the height of maximum density of the F_2 layer h_{max} (the so-called topside).

When combined with electron density profile data for the bottom side, they provide a determination of the ratio of total electron content to the content below h_{max} . This ratio appears to vary between about 3

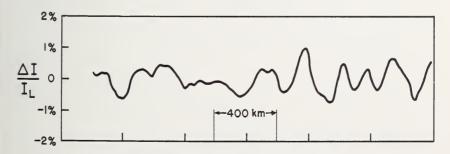


FIGURE 4.48. Irregularities in electron content 0834, 105° WMT, Sept. 4, 1958.

(After C. G. Little and R. S. Lawrence, 1960, the use of polarization fading of satellite signals to study the electron content and irregularities in the ionosphere, J. Res. NBS 64D (Radio Prop.), 335.)

and about 5 from day to night. The daytime peak in electron content is six to eight times greater than the nighttime minimum. Furthermore, the noontime content seems to be somewhat higher in winter than in summer. During magnetically disturbed conditions the total electron content appears to decrease.

Because of the high sensitivity inherent in this method, it is possible to observe the irregular structure in the electron content of the F_2 layer as shown in figure 4.48.

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CHAPTER 5

Signal Strength

5.1. MEANING OF SIGNAL STRENGTH

The instantaneous value of a sine wave function at a point is defined by the peak amplitude and the instantaneous phase at the point. The amplitude of a composite wave signal is given by the vector sum of its components; thus, if the components are in phase, the resultant amplitude will be the algebraic sum of the individual waves. If the phases of the separate components are varying randomly with respect to each other, the resultant signal power, averaged over many fading cycles, is given by the sum of the powers in the component waves. In this chapter the term "signal strength" will be used in a broad sense to mean either the amplitude (field strength) or the power received by an antenna.

The signal strength at any time depends upon absorption along the path, path focusing, polarization, and phase of the waves. In this chapter we shall discuss some aspects of these phenomena.

We shall discuss first the factors affecting the average power received (system loss) and then the factors which produce variations about the average (i.e., fading).

5.2. FACTORS AFFECTING SIGNAL STRENGTH

Consider a radio communications system which consists of a transmitter, a transmission line, a transmitting antenna, the propagation medium, a receiving antenna, a receiver transmission line, and, finally a receiver. It is possible to consider the entire circuit between transmitter output terminals and the receiver input terminals as a "black box" as shown in figure 5.1. If p_t is the power fed into the terminals of the feeder line from the transmitter and if p_r is the signal power available from the terminals of the line from the receiving antenna, then the total system

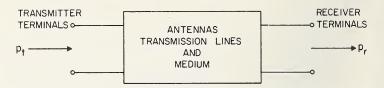


Figure 5.1. Block diagram to illustrate the power loss between transmitter terminals and receiver terminals.

power loss $[1]^1$ L_s , expressed in decibels, is given by

$$L_s = 10 \log \left(\frac{p_t}{p_r}\right) = -10 \log \left(\frac{p_r}{p_t}\right). \tag{5.1}$$

Thus, for a given transmitter output power, as the loss L increases, the received power p_r decreases.

Let us represent the powers by small letters and the logarithms by capital letters so that

$$P_t = 10 \log p_t \qquad (a)$$

$$P_r = 10 \log p_r. \qquad (b)$$
(5.2)

and

Then (5.1) can be written in the form

$$L_s = P_t - P_r \text{ (in decibels)}. \tag{5.3}$$

Let us now consider the losses incurred by the signal as it travels between the transmitter terminals and the receiver terminals, as shown schematically in figure 5.2. First of all there are the ohmic losses in the feeder line and in the transmitting antenna due to the resistance of the wire and to the finite conductivity of the environment (induced earth currents, etc.). The rest of the power is radiated into space, mostly from the antenna, but a small amount from the transmission line. The radiation efficiency of the antenna is given by the ratio of the power radiated to the power absorbed from the source. For high frequencies the efficiency of most antennas is relatively high (e.g., the efficiency of a half wave dipole is generally greater than 90 percent).

For an isotropic radiator the power is radiated equally in all directions and the power radiated in any direction can be taken as a reference. All actual antennas have radiation patterns such that the power flux

¹ Figures in brackets indicate the literature references on p. 255.

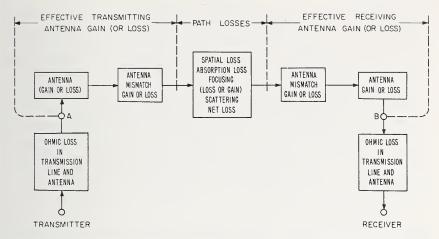


Figure 5.2. Block diagram showing the various sources of power loss as a signal travels from a transmitter to a receiver.

is maximized in certain preferred directions. Of course, when the total power radiated is the same for both the hypothetical and actual antennas, then if there is a power gain in some directions, this must be exactly balanced by a loss in other directions.

After the signal has left the antenna it loses energy density by several processes, such as:

- (1) The spatial spreading of the energy (inverse distance squared dependence).
- (2) Polarization matching (or mismatching). We have seen in chapter 2 that, within the ionosphere, two progressive waves can exist (ordinary and extraordinary). On entry into the ionosphere a wave with arbitrary polarization will excite ordinary and extraordinary waves by different amounts depending on the propagation angle at the bottom of the ionosphere. Thus, from the point of view of a single magneto-ionic wave, there is a loss of power, in general, on entry into the ionosphere.
- (3) Absorption of energy will occur in the D and lower E regions due to electronic collisions, as explained in section 2.3.3.3. The energy in the wave is in fact converted into heat.
- (4) Due to curvature of the ionosphere and/or due to the change of ground range with angle of elevation, the power flux at any point on the earth may be enhanced by focusing or diminished by defocusing. Energy may also be scattered in or out of the main path by ionospheric irregularities, but this problem is too difficult to be considered here.

(5) On leaving the ionosphere the polarization for a particular magneto-ionic wave will have a certain configuration depending on the angle between the wave normal and the earth's magnetic field at the bottom of the ionosphere. Since the angle between the magnetic field and the emergent wave differs from the angle between the magnetic field and the incident wave, the polarization of the emergent wave will, in general, be different from the polarization of the incident wave. Furthermore, the polarization of the wave will not in general match that of the receiving antenna and there will therefore be a loss of received signal due to polarization mismatch. For certain directions there may be a gain due to the antenna pattern; in other directions there will be a loss.

Finally, there are ohmic losses in the receiving antenna and in its transmission line.

The polarization mismatch losses can be included with the antenna gain to give an "effective antenna gain" for the particular angle of takeoff and wave polarization. Our main concern, in this book, is with propagation in the medium between the antennas. The power losses along the propagation path, and which are not associated in any way with the antennas, will be called the "path loss."²

In what follows it will be assumed that the polarizations of the hypothetical isotropic radiators are perfectly matched to the polarizations of the characteristic waves excited in the ionosphere.

Consider a *single* propagation path, with a given characteristic wave, between a transmitter and a receiver. With an actual antenna, let

 L_{ta} = the ohmic loss in the transmitting antenna and its transmission line, in decibels,

 L_{tp} = the polarization mismatch loss of the transmitting antenna,

 G_t = the gain of the transmitting antenna in the desired direction,

 L_p = the path loss in decibels,

 L_{rp} = the polarization mismatch loss of the receiving antenna,

 G_r = the gain of the receiving antenna in the desired direction, and L_{ra} = the ohmic loss in the receiving antenna and its transmission line.

Then the system loss is given by

$$L_s = L_{ta} + L_{tp} - G_t + L_p + L_{rp} - G_r + L_{ra}.$$
 (5.4)

Of course, it sould be remembered that the antenna gains G_t and G_r may be positive or negative depending on the direction of radiation.

² CCIR Recommendation No. 241 defines a quantity called "basic transmission loss" and states that it is sometimes called path loss. It is important to note that our definition of path loss is *not* the same as that of basic transmission loss.

In practice, the total signal arriving at a receiver, after reflection at the ionosphere, is composed of individual signals which have traversed different paths and which have differing characteristic polarizations. To draw an electrical analogy, we can think of the component paths as a set of resistances in parallel. The presence of additional paths, although they involve losses, actually increases the received power and, therefore, diminishes the effective loss of the system. The ohmic losses in the antennas and their transmission lines (see fig. 5.2) are the same for all paths. However, the effective antenna gain will depend on the particular propagation path. Hence, the additional paths must be considered as parallel channels across the terminals A and B in figure 5.2.

Let L_1 represent, for channel 1, the sum of the losses (in decibels) given by (5.4), with the exclusion of the ohmic losses; that is,

$$L_1 = L_{tp1} - G_{t1} + L_{p1} + L_{rp1} - G_{r1}, (5.5)$$

and, similarly, for L_2 , L_3 , etc. To determine the manner in which the net loss between A and B, which we may call L_{AB} , is related to L_1 , L_2 , L_3 , etc., it is necessary to deal with the fraction l of the power which is lost along each path. That is,

$$L_1 = 10 \log l_1$$
, etc. (5.6)

Invoking the analogy of parallel resistances, it will be seen that the net loss l_{AB} is given by

$$\frac{1}{l_{AB}} = \frac{1}{l_1} + \frac{1}{l_2} + \frac{1}{l_3} + \text{etc.},$$

and L_{AB} by

$$L_{AB} = 10 \log l_{AB} = -10 \log \left[\frac{1}{l_1} + \frac{1}{l_2} + \frac{1}{l_3} + \text{etc.} \right]. \tag{5.7}$$

To take a simple example, consider three possible paths for which the losses between A and B are $L_1 = 50$ dB, $L_2 = 50$ dB, and $L_3 = 100$ dB. The corresponding values of the l's are: $l_1 = 10^5$, $l_2 = 10^5$, and $l_3 = 10^{10}$, so that the net loss $l_{AB} = 5 \times 10^4$ and $L_{AB} = 47$ dB. This shows that the contribution to the total signal from path 3 is negligible, and that the contributions from paths 1 and 2 give a net loss which is 3 dB less than that for either path 1 or path 2. Consider the case where $L_1 = 50$ dB, $L_2 = 60$ dB, and $L_3 = 70$ dB, which gives $l_1 = 10^5$, $l_2 = 10^6$, and $l_3 = 10^7$. The net loss $l_{AB} = 10^7$.

 9×10^4 , which gives $L_{AB} = 49.5$ dB. As would be expected, the contributions to the total signal from paths 2 and 3 amount to only 0.5 dB.

5.3. PATH LOSS

5.3.1. Components of Path Loss

In high-frequency propagation via the ionosphere, the received signal usually consists of a number of component waves which have traveled over different paths. The relative phases of individual waves vary rapidly and randomly so that the total received power, averaged over a period (e.g., several minutes) long compared to the fading cycles, is essentially the sum of the powers in the individual waves. It is important to realize that when we talk of path loss we imply an average power loss.

The components of path loss (for a single path) have been enumerated above (in sec. 5.2) and are

- (1) The simple inverse distance or dispersion of the energy in space; we shall denote this loss, in decibels, by L_d .
 - (2) Absorption in the ionosphere, L_a .

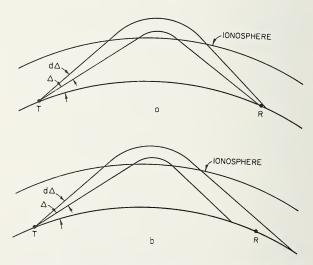


FIGURE 5.3. Illustrating the focusing and defocusing of ionospherically reflected radio beams.

(a) Convergence of rays (focusing). (b) Divergence of rays (defocusing).

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(3) Focusing or defocusing of power, L_f . Note that L_f will be positive for defocusing and negative for focusing.

The path loss, L_p , in decibels, is given by the sum of its components, namely,

$$L_p = L_d + L_a + L_f. (5.8)$$

Let us now discuss these losses in more detail.

5.3.2. Spatial Loss

As a wave travels out from a small source, the power flux falls off inversely as the square of the distance s from the source, therefore,

$$L_d = 20 \log s. \tag{5.9}$$

5.3.3. Focusing

5.3.3.1. Effective Path Length

Focusing is the result of the convergence or divergence (defocusing) of originally neighboring rays (in addition to the divergence responsible for L_d) as illustrated in figure 5.3, for example. In practice it is very difficult to take into account the focusing of ionospherically reflected radio signals. In fact, it is necessary to have a detailed knowledge of the ionosphere along the ray path together with an elaborate ray-tracing program, as already discussed in section 4.6.6. Nevertheless, it is possible to consider the effect of focusing in terms of an effective path length s_e . The physical meaning of this effective path length can be seen from the following argument. In the absence of all other forms of energy loss the power flux at a distance s_e from an isotropic radiator, which radiates a total power p_{ta} , is given by

$$\phi = \frac{p_{ta}}{4\pi s_{\perp}^2}.\tag{5.10}$$

Now let the energy radiated into the same cone by the antenna be defocused as shown in figure 5.4. Let s be the distance from the antenna at which the area covered by the defocused rays is the same as that for

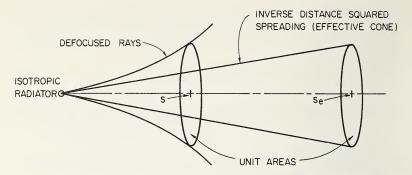


Figure 5.4. Illustration of the concept of effective path length which takes into account the focusing and defocusing of radio beams.

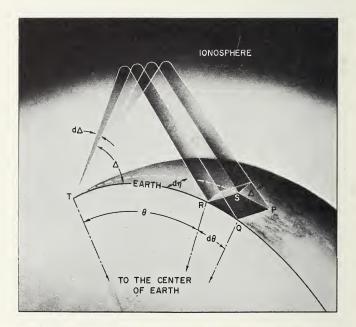


FIGURE 5.5. The divergence of a radio beam for a curved earth.

the original case, so that the power flux is the same for both. Thus the defocusing can be taken into account by replacing the true distance s of the receiver by an effective distance s_e . In this way the spatial loss and the focusing losses can be combined in the expression

$$L_d + L_f = 20 \log s_e.$$
 (5.11)

Note that s_e is greater than s for defocusing and less than s for focusing. By using this effective distance we see that s_e^2 is equal to the ratio of the cross section of the effective cone (fig. 5.4), which is equal to that of the actual defocused cone, to the cross section at unit distance from the source.3 This is illustrated in figure 5.5 in which a rectangular beam of vertical angular width $d\Delta$, of horizontal angular width $d\eta$, and elevation Δ is reflected from the ionosphere. In this figure the ionosphere is assumed to be spherically stratified so that angles of arrival and departure are equal, though this is not always the case in practice. Let θ be the angle subtended at the center of the earth by the path. From the enlargement shown in figure 5.6 we see that the cross section of the beam at unit distance from the transmitter is $d\Delta(d\eta\cos\Delta)$. Referring to figure 5.5, we see that the cross section of the beam at the receiver is given by $RQ \cdot RS$ $\sin \Delta$. Now $RQ = a \ d\theta$, where a is the radius of the earth. The distance RS can be obtained by the construction shown in figure 5.7 in which SP and RP are perpendicular to TO. $SP = RP = a \sin \theta$ and, hence, $SR = a \sin \theta \, d\eta$. The cross section of the beam at R is given by $(a \, d\theta)$

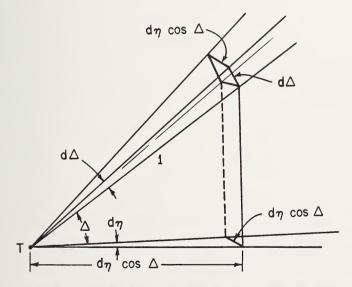


Figure 5.6. Enlarged view of the beam (of fig. 5.5) near the transmitter.

² Provided there is no focusing within a unit distance.

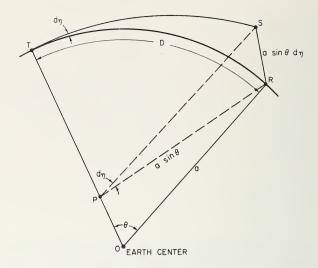


FIGURE 5.7. Spreading of the beam in the horizontal direction.

 $(a \sin \theta \, d\eta) \sin \Delta = a^2 \sin \theta \sin \Delta \, d\theta \, d\eta$ and, hence, s_e is given by

$$\begin{split} s_e^2 &= a^2 \sin \theta \tan \Delta (d\theta/d\Delta) & \text{(a)} \\ &= a \sin \theta \tan \Delta (dD/d\Delta) & \text{(b)} \end{split}$$

where D is the ground range.

For a given value of Δ , θ and $dD/d\Delta$ can be calculated either analytically, in the case of certain model layers, or by means of ray-tracing programs such as those discussed in section 4.9.

5.3.3.2. Skip Distance Focusing

In figure 4.7 we see the variation of ground range D with φ_0 in the case of a parabolic layer. It can be seen that, near the edge of the skip zone (minimum D), $dD/d\varphi_0 (=-dD/d\Delta)$ tends to zero as also does s_e , implying a large signal strength. In fact the above theory breaks down, in detail, near the skip distance, and a more elaborate treatment is necessary to establish the degree of focusing. Bremmer [2, ch. 10] and Budden [3, ch. 11] have shown that, in the vicinity of the skip distance, the rays form a caustic surface in much the same way as when parallel light rays are reflected from a spherical mirror. The resulting variation of signal

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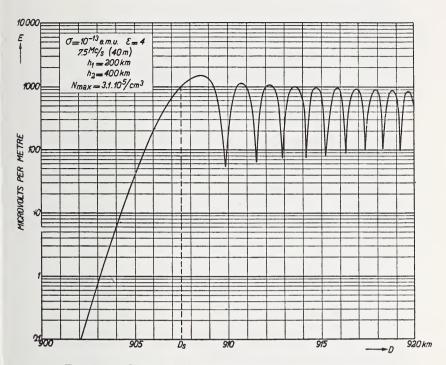


FIGURE 5.8. The rms field in the neighborhood of the skip distance.

(After H. Bremmer, 1949, fig. 72, Terrestrial Radio Waves, Elsevier Publ. Co.).

strength with distance is shown in figure 5.8. This shows that within the shadow the signal falls off rapidly but not sharply. In the illuminated zone oscillations are produced by the interference between high and low rays. A somewhat similar variation of signal strength with frequency is obtained near the MUF for a fixed distance and it is then called MUF focusing. Because of the bandwidths involved, the focusing of short pulses at the skip distance would be less than that of long pulses or continuous waves because the higher sidebands will penetrate the ionosphere. In any case the effect is appreciable only within about 5 km of the skip distance, or within a few kilocycles of the MUF.

Most experimental evidence indicates that the focusing factor is on the order of 6 to 9 dB. An example of such focusing is shown in figure 5.9 in which the transmitted frequency is fixed but the maximum frequency changes with time.

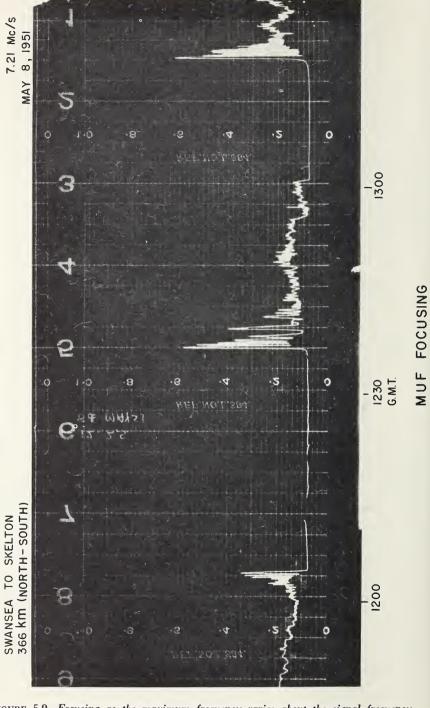


FIGURE 5.9. Focusing as the maximum frequency varies about the signal frequency.

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5.3.3.3. Antipodal Focusing

If the earth and ionosphere were perfectly smooth and concentric, energy could reach the antipode by all possible great circle paths [2]. However, because of the great geographic variations in ionospheric conditions, such focusing does not appear to be of great practical importance.

5.3.3.4. Horizon Focusing

Putting $\Delta = 0$ in (5.12) we see that s_e^2 goes to zero. This type of focusing is called "horizon" focusing.

It is interesting to note that in multi-hop propagation, if the successive hops are all alike, the degree of focusing in the vertical plane is the same as for the first hop. This can be proved as follows: Let S_{Δ} be the effective distance taking account of spreading in the vertical plane only (see fig. 5.5). Then

$$S_{\Delta} = a \sin \Delta (d\theta/d\Delta). \tag{5.13}$$

The degree of focusing in the vertical plane may be denoted by the ratio of S_{Δ} to the actual length of the ray path. If S' denotes the actual length of the ray path for the first hop, the actual ray path length for n hops is nS'. The value of $S_{\Delta n}$ for the n hops is

$$S_{\Delta} = a \sin \Delta \frac{d(n\theta)}{d\Delta} = n S_{\Delta}', \tag{5.14}$$

where S_{Δ}' is the value of S_{Δ} for the first hop. The degree of focusing for the *n* hops is thus $n S_{\Delta}' / n S' = S_{\Delta}' / S'$, which is the degree of focusing for the first hop.

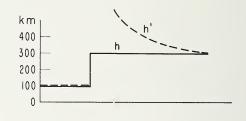
5.3.3.5. Ionospheric Distortion

Focusing (or defocusing) due to ionospheric distortion can be very important, as was seen in section 4.6.6, where ionospheric curvature simulates convex or concave mirrors. This phenomenon is particularly important in transequatorial propagation during the afternoon and early evening because of the existence of a relatively stable deformation. Part of the long-period fading (half to one hour) of high-frequency skywaves

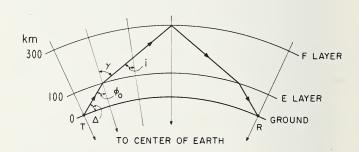
is the result of focusing by transient deformations of the ionospheric layers. In particular, such distortions in the F layer can produce focusing and defocusing of the reflected radio signal amounting to between 5 and $10~\mathrm{dB}$ variation in the path loss.

5.3.3.6. Defocusing Due to Underlying Ionization

Consider an electron density profile, such as shown in figure 5.10a, in which a block of electrons (simulating an E layer) is located below a sharply bounded reflecting F layer. Because of refraction in the lower layer the ray path (for $f \approx 1.5 fE$) will be as shown in figure 5.10b. The effective path s_e to the same range will, therefore, be greater than it would be in the absence of the underlying ionization and, as a result, the path loss is increased.







(b)

FIGURE 5.10. Defocusing due to underlying model E layer in which the electron density is constant over the height range 100 to 300 km.

(a) Profile and ionogram. (b) Ray path for f=1.5 fE

5.3.4. Absorption

5.3.4.1. The Absorption Coefficient

The absorption term L_a which appears in (5.5) is given by

$$L_a = 10 \log \frac{p_r}{p_u} = 20 \log \rho, \tag{5.15}$$

where p_r is the actual power received and p_u is the power which would have been received in the absence of absorption and where ρ is the effective amplitude reflection coefficient as defined in section 3.2.2.1 (see (3.4)). From (3.3) and (3.4) we find that the relationship between L_a and the absorption coefficient κ (see (2.96)) is given by

$$L_a = -8.7 \int_s \kappa \, ds, \tag{5.16}$$

where the integration is carried out over the ray path. In (5.15) we have neglected any differences between the direction of phase propagation and the ray path.

In most problems of radio transmission involving high frequencies or very high frequencies it is sufficiently accurate to use (2.103) for the determination of κ for non-deviative conditions. The higher the wave frequency the better is the QL approximation for a given θ , or the larger is the range of θ for a given degree of accuracy. For deviative absorption (μ small) it is preferable to use (2.100) to obtain κ but in oblique propagation μ never gets very small and in the case of F-layer propagation absorption near the top of the trajectory can be ignored.

During some polar cap absorption events and certain solar flares, the variation with frequency of the absorption does not follow (2.103) because electrons are produced at very low heights (50 to 60 km) in the atmosphere. At these levels it is necessary to use (2.101) to determine κ . However, under such conditions, absorption may be taking place over a range of heights and the exact determination of κ may be a complicated process.

The geographical and temporal variations in $\int \kappa ds$ may be found in section 3.3.6.

5.3.4.2. Martyn's Absorption Theorem

By analogy with (4.7) the absorption L, for a wave incident at an angle ϕ on a plane ionosphere, is related to the absorption L_v of the equivalent vertical wave, as defined in section 4.2.1, by the formula

$$L = L_v \cos \phi. \tag{5.17}$$

This relation is not exact for the actual ionosphere with the earth's magnetic field, but it is a useful guide. An easy way to remember this theorem is to notice that the oblique path length is $\sec \phi$ times the vertical but that the equivalent vertical wave (of frequency $f \cos \phi$) suffers $\sec^2 \phi$ more absorption because the absorption varies inversely as the square of the frequency, (2.99).

5.3.4.3. Variation of Absorption with Distance

Daytime absorption on high frequencies takes place mainly in the D region, between 80 and 100 km. The amount of absorption suffered by a high-frequency wave passing through this region is proportional to the length of the path in the region. Since the thickness of the region is very small compared to its radius of curvature (distance to the center of the earth), the length of the path in the region is very nearly equal to the secant of the angle of incidence ϕ_D at the mean height of the region multiplied by the thickness of the region.

On frequencies sufficiently far above the *E*-layer critical frequency, the ray path may be reasonably well represented by an equivalent triangle like that depicted in figure 5.11. The variation of $\sec \phi_D$ with distance for such a path is shown in figure 5.12 for four combinations of h_D the mean height of the *D* region, and h' the height of the apex of the equivalent triangle. The two values of h_D are 80 and 100 km, and the two values of h' are 250 and 500 km.

Beyond about 1000 km, these curves can be approximated by the straight dashed lines drawn through the origin, at least to the degree of accuracy normally attained in transmission loss determinations. All four curves bend over at the top, but the departure from the straight lines is not serious until the distance is greater than about 2600 km for the h'=250 km curves (departure angle $\simeq 5^{\circ}$) and about 3800 km for the h'=400 km curves (departure angle $\simeq 3^{\circ}$).

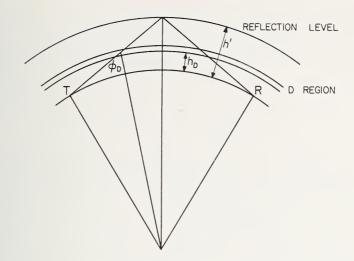


FIGURE 5.11. Angle of incidence in the D region.

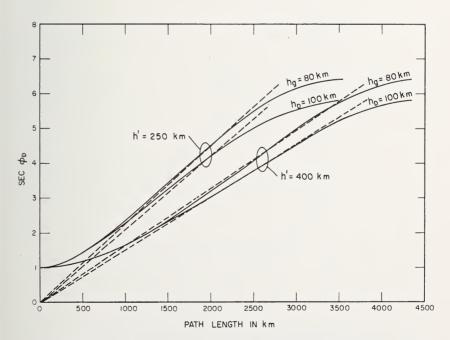


FIGURE 5.12. Variation of sec ϕ_D with ground range for the model shown in figure 5.10. (After T. N. Gautier, unpublished.)

During daytime when there is an appreciable E layer present the ray paths will be modified as sketched in figure 5.10b. In general, the deviation in the E layer will decrease with increase of frequency for a given angle of elevation. It will decrease with increase in elevation on a given frequency.

5.3.4.4. Deviative Absorption

The calculation of deviative absorption is a difficult process depending on the details of ray path, electron density profile, and collision frequency profile. In fact it is impossible, in practice, to determine just what is deviative and what is non-deviative since these terms are defined in terms of limiting conditions. Because the collision frequency ν decreases rapidly with height, absorption tends to be concentrated in the lower regions of the ionosphere. Thus for waves reflected from the F region, deviative absorption tends to be greatest not near reflection but in the

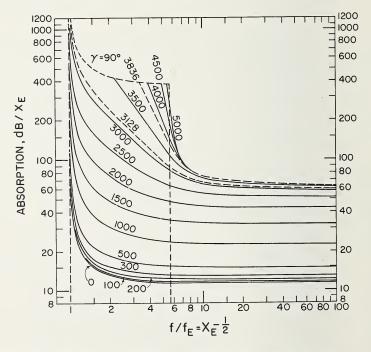


FIGURE 5.13. Variation of deviative absorption with frequency for various ground ranges (in km) and the electron density profile shown in figure 5.10.

 $X_E = (fE/f)^2$. (After T. N. Gautier, unpublished.)

lower part of the E region except, possibly, at night. To determine the deviative absorption it is necessary either to choose suitable ionospheric models of N(h) and $\nu(h)$ so that the integral $\int 2\kappa \, ds$ can be evaluated analytically, or to compute the absorption step by step in an actual N(h) profile with a computer (ray-tracing) program.

With an N(h) profile of the type shown in figure 5.10a and a $\nu(h)$ profile given by

$$\nu = 6 \times 10^4 \exp\left\{-\frac{h - 100}{6.7}\right\},$$
 (5.18)

the variation of absorption with wave frequency for different distances is sketched in figure 5.13. At the right-hand side of the figure (large f/fE) where the curves are flat, the absorption is non-deviative. Deviative absorption is manifested by the upward bending of the curves to the left. The distance 3128 km corresponds to $\mu_E=0$, that is, when a ray incident vertically on the 100 km level is refracted so as to be tangential. Under such conditions the absorption would be large. The 3836 km distance is the maximum one-hop distance achieved with no E layer refraction (i.e., $\mu_E=1$).

5.3.4.5. Geographic Considerations

Middle latitudes. The variations of non-deviative absorption in middle latitudes are fairly well-behaved and may be approximated by a formula given by Rawer [4]:

$$L_a = 430(1 + 0.0035R) \cos^{0.75} \chi \sec \phi_D (f \pm f_L)^{-2},$$
 (5.19)

in decibels per hop. Here R is the sunspot number, χ is the solar zenith angle, and f and f_L are in megacycles per second. The numerical values in this formula are based on analyses of vertical incidence measurements at Slough, England.

The formula does not take account of the winter anomaly—section 3.3.6.5. To get an estimate of the absorption for the winter months, the values given by (5.19) should be multiplied by the factors in table 5.1. These numbers may be used in dipole latitudes of 40° to 70° north and south. It should be kept in mind that these are average values. On individual days the factor may vary from less than 1 to around 2.0. The value of the factor depends somewhat on the degree of geomagnetic activity [5].

| Month | | |
|---|-------------------------------|--------------------------|
| Northern hemisphere | Southern hemisphere | Factor |
| November December January February | May June July August | 1.2 1.5 1.5 1.2 |

Table 5.1. Absorption factors for winter months in northern and southern hemispheres

High latitudes. In high latitudes the most important consideration in radio communications is the onset of radio blackouts rather than the average absorption. This subject will be dealt with in chapter 6.

Low latitudes. These latitudes have been discussed by Piggott [6], who has listed the following characteristic features of low-latitude propagation:

- 1. The relatively great importance of E-layer trajectories.
- 2. The variability of the F-layer profile. This seriously limits the practical value of F-layer propagation at short ranges and makes the angle of elevation and path loss for F reflections at a given range exceptionally variable.
- 3. The absorption of the ordinary wave on a given frequency and trajectory is usually greater than at higher latitudes because f_L is smaller, other factors being the same.
- 4. Interference fading between modes having equal amplitudes is relatively more common since the differential absorption between the ordinary and extraordinary waves is smaller than in higher latitudes.

5.3.5. Polarization Mismatch Factors

When a wave propagates in the ionosphere it is polarized in a manner which depends primarily on the electron density, wave frequency, and direction of propagation relative to the magnetic field. The polarization at the bottom of the ionosphere (where the electron density N=0) is called the limiting polarization.

To illustrate the effect of polarization mismatch on a wave, consider a ray incident at an angle of 45° on a plane ionosphere in the magnetic meridian as shown in figure 5.14a. Let the magnetic dip angle be 45° and the polarization of the transmitting antenna be such that the in-

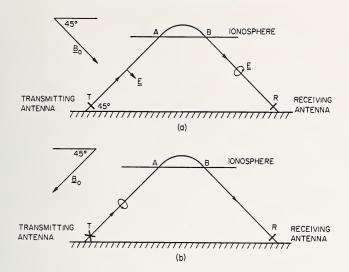


FIGURE 5.14. Path losses due to polarization mismatch.

(a) Transmitted wave linearly polarized. (b) Transmitted wave circularly polarized.

cident wave is linearly polarized with the electric vector parallel to the magnetic field. On entry into the ionosphere at the point A, all the incident power is used in exciting the ordinary wave. Thus, for the ordinary wave, the loss $_{0}L_{tp}$ is zero, whereas for the extraordinary wave $_{x}L_{tp}$ is infinite. Now as the ordinary wave travels through the ionosphere, the propagation angle θ varies continuously so that the wave polarization changes from linear to elliptical until it reaches B, at which point the polarization is circular, because $\theta = 0^{\circ}$. If the receiving antenna is linearly polarized it will pick up half the incident power, so that $_{0}L_{rp}$ is 6 dB.

Next, consider the case in which the transmitting antenna radiates a circularly polarized wave (see fig. 5.14b) such that, on entry into the ionosphere at A, all the power is used in exciting the ordinary wave. Once again $_{\circ}L_{tp}$ is zero for the ordinary wave and $_{\times}L_{tp}$ is infinite for the extraordinary wave. Within the ionosphere the wave polarization becomes elliptical until at B it is linearly polarized with the electric vector parallel to the magnetic field B_0 . Now if the receiving antenna is linearly polarized to pick up the ordinary wave $_{\circ}L_{rp}$ is zero, whereas if it is polarized perpendicular to this direction the loss is infinite. If φ is the angle between the direction of the magnetic field and the direction of linear polarization of the receiving antenna the loss for the ordinary wave is given by 10 log $\cos^2 \varphi = 20 \log \cos \varphi$. Of course if the transmitting antenna emits circularly polarized waves with the opposite sense of rotation, then the

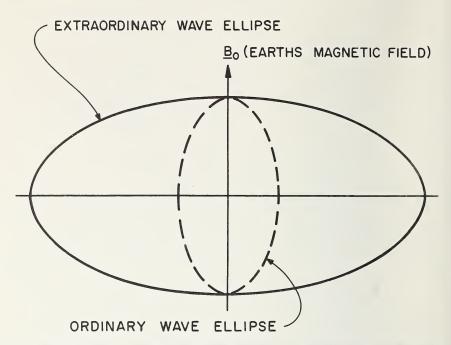


Figure 5.15. Limiting polarization ellipses produced by a horizontally polarized wave incident on the ionosphere in the magnetic meridian.

losses for the ordinary and extraordinary waves are reversed. If the incident radiation, in the case of figure 5.14b, is linearly polarized, then the incident power is divided equally between the ordinary and extraordinary waves so that $_{0}L_{tp}=_{x}L_{tp}=6$ dB. Of course the total power in the composite wave may still be the same. We now have an extra wave to take into account.

To illustrate further what happens when a radio wave enters the ionosphere, consider radiation from a horizontally polarized antenna incident on the ionosphere in the magnetic meridian. On entering the ionosphere the wave is split up into two characteristic waves (see sec. 2.3.3.2) which are, in general, elliptically polarized with opposite senses of rotation. Since the incident wave is horizontally polarized the vertical axes of the two polarization ellipses must just cancel, and so the ellipses must be as shown in figure 5.15. The shapes of the ellipses are given (approximately) by the formula X=0 in (2.74):

$$R = \frac{E_3}{E_2} = \frac{i}{2 Y_L} \left\{ Y_T^2 \pm \sqrt{Y_T^4 + 4 Y_L^2} \right\}. \tag{5.20}$$

Now

$$(E_3)_0 = R_+(E_2)_0,$$

and

$$(E_3)_x = R_-(E_2)_x;$$

$$(E_2)_0 = (E_2)_x$$

hence

$$(E_3)_0 = \frac{R_+}{R_-} (E_3)_x$$
.

Substituting from (2.90) we obtain

or
$$(E_3)_0 = R_+^2(E_3)_x, \qquad \text{(a)}$$

$$(E_3)_x = R_-^2(E_3)_0. \qquad \text{(b)}$$

Equation (5.21) enables us to determine the way in which energy in the incident wave is distributed between the ordinary and extraordinary components. From then on the two components travel essentially independently until they emerge from the ionosphere. However, since the absorptions suffered by the two waves are unequal the emergent waves will not cancel out in the vertical plane and the resultant wave will, therefore, be elliptically polarized.

Substitution of numerical values of Y(0.1, say) and $\theta(45^{\circ}, \text{say})$ in (5.20) shows that $R_{\mp} \approx 1$ so that, except for nearly transverse propagation, the energy is divided almost equally between the two magneto-ionic components. On lower frequencies, however, this is not the case as can be seen by substituting Y=1 and $\theta=45^{\circ}$ in (5.20). This gives $(E_3)_o=2(E_3)_x$.

When the propagation is nearly transverse, $\theta \simeq 90^\circ$, so that $R \simeq (Y_L/Y_T^2) \to 0$ and $R_+ \simeq (Y_T^2/Y_L) \to \infty$. Hence the ellipses are very narrow. In the absence of collisions the major axis of the ordinary wave ellipse is parallel to the magnetic field, whereas that for the extraordinary wave ellipse is perpendicular to the magnetic field. In intermediate and high latitudes the ordinary wave ellipse has its major axis nearly vertical and the extraordinary wave ellipse has its major axis nearly horizontal. Except when θ is within about 15° of the normal to the magnetic field the ellipses are so nearly circular that the differences between ordinary and extraordinary wave ellipses are unimportant on frequencies well above the gyrofrequency.

For east-west propagation along the magnetic equator, antennas should be horizontally polarized so as to excite the ordinary wave, whereas in high latitudes the ordinary wave is excited by a vertically polarized

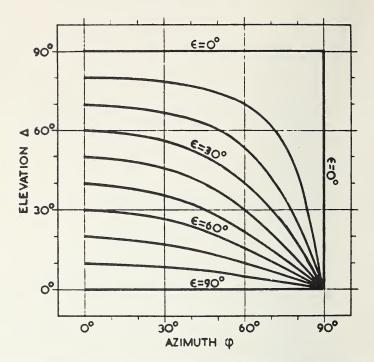


Figure 5.16. Directions for which θ (the propagation angle) = 90° for different angles of magnetic dip ϵ .

The azimuth ϕ is measured from the magnetic meridian. (After W. R. Piggott, 1959, Radio Research Special Report No. 27, Her Majesty's Stationery Office, London.)

wave. The necessary conditions for polarization to be important are (a) that the propagation be quasi-transverse at the point of entry into or exit from the ionosphere (or both), and (b) that the differential absorption between the magneto-ionic waves be large. Polarization effects are, therefore, most important on frequencies in the vicinity of the gyrofrequency that is in the frequency band from 0.3 Mc/s to 3 Mc/s.

For the calculation of path loss it is necessary to know L_{tp} (5.4) and this can be determined by the use of equations such as (5.21) and a knowledge of the polarization of the transmitted wave. Similarly L_{rp} can be determined from a knowledge of the emergent polarization and the antenna polarization, the angles of elevation and azimuth at which the polarization may become important can be seen in figure 5.16, which gives the angles of elevation and azimuth as a function of the dip angle near the transmitter or receiver as appropriate. The critical range of angles falls in the middle of the most important range of angles for practical communications in temperate latitudes. Vertical polarization is preferable to horizontal whenever polarization is important in these latitudes.

For short-range transmissions on the lower frequencies it is often convenient to use polarization as a method of discriminating against noise. Very considerable gains in signal/noise ratio are possible in the daytime by using antennas which are insensitive to vertical polarization on the frequencies where most of the interference is propagated via the ionosphere.

In multi-hop transmission, depolarization of a characteristic wave may occur after a ground reflection, especially if the magnetic dip is different for the two hops so that a downcoming ordinary wave may, after a ground reflection, give rise to ordinary and extraordinary waves.

5.3.6. Antenna Gain

A detailed discussion of antennas is beyond the scope of this book and so a few simple ideas will suffice for our present purposes.

It has become customary to specify the gain of an antenna in a given direction as the ratio of the power radiated in that direction to the power which would be radiated in the same direction by a standard reference antenna. Standard antennas used for this purpose are (1) an isotropic radiator, (2) a half-wave dipole (this has a power gain of 1.64 [2.15 dB] relative to an isotropic radiator), and (3) a short electric dipole which has a maximum power gain of 1.5 (1.76 dB) over an isotropic radiator.

If p_0 is the power radiated in kilowatts, the power p_{Δ} radiated per unit solid angle at an elevation Δ is given by

$$p_{\Delta} = p_0 g_{\Delta} \tag{5.22}$$

where g_{Δ} is the free space gain of the antenna at an elevation Δ over an isotropic radiator. The value of g_{Δ} can be calculated from the geometry of the antenna. Note that p_0 is the actual power radiated (current squared times radiation resistance) and not the power output of the transmitter or the power input to the antenna.

For a short dipole (less than 0.1 wavelength), $g_{\Delta} = 1.5 \sin^2 \Delta$, where Δ is measured from the axis of the dipole. For a short vertical wire, one end of which is on a perfectly conducting ground, the gain is given by $g_{\Delta} = 3 \cos^2 \Delta$. Part of the field intensity near the ground ($\Delta \simeq 0^\circ$) is due to the surface wave, which is negligible when the wave reaches the ionosphere. Consequently, the vertical directional pattern of an antenna, for skywave calculations, may be considerably different from the pattern measured near the antenna.

5.4. FADING

5.4.1. General Characteristics

In the above discussions of path loss we concerned ourselves with the average power received. Now the instantaneous field strength may fluctuate widely about the mean value and amplitude variations of the order of 10 to 1 can occur in the course of a few seconds. Fading may be caused by several different ionospheric phenomena, e.g., movements of the ionosphere causing interference fading, rotation of the axes of the polarization ellipses, time variations in ionospheric absorption, focusing, and skipping of the signal due to MUF failure. In the case of signals transmitted from a moving source—e.g., a satellite—fading will result from the motion of the source relative to ionospheric irregularities. Fading of cosmic radio noise is often referred to as "scintillation."

The period of a fading cycle depends largely on the cause of the fading. Thus the fading period of interference and polarization fading may vary from a fraction of a second to a few seconds, absorption fading may have a period of the order of an hour or longer, whereas focusing may be of the order of 15 to 30 min. Signals can fade in or fade out if the frequency of the signal is near the maximum frequency and the critical frequency is changing with time (see fig. 5.9). It is, therefore, highly irregular as far as period is concerned and may occur only in the early morning and late afternoon (fade in and fade out).

In general, fading is faster on high frequencies than on low frequencies because a given movement in the ionosphere produces a greater phase shift on the shorter wavelengths. The fact that fading is frequency-dependent means that different sidebands in a modulated wave fade differently. This gives rise to a distortion of the modulation envelope which is called selective fading.

5.4.2. Interference Fading

A beam of radio waves incident on the ionosphere is not reflected from a point but from an extended region. Small irregularities in electron density near the level of reflection give rise to individual reflected wavelets and the received signal is the vector sum of the individual signals at the receiving antenna. Movements of ionospheric irregularities give rise to variations in the relative phases of the individual wavelets and thus

produce interference fading. It is not uncommon for a received high-frequency signal to consist of a mixture of high- and low-angle rays, each having extraordinary and ordinary components; each such set may be combined with other sets corresponding to rays having different numbers of hops.

The resultant amplitude can vary over wide limits, the maximum value being when all the individual components are in phase. The root mean square value of the fluctuating signal is equal to the steady value of the field that would have existed had the ionosphere not broken it up into many components. Because it is impossible to determine the resultant amplitude at any given moment, the subject has to be treated on a statistical basis. Such phenomena are said to be "stochastic."

The distribution of amplitude approximates the Rayleigh law when the various components are of approximately the same amplitude and the relative phases are varying randomly. For the Rayleigh distribution, the percentage of time p(A) that the amplitude exceeds the value A is

$$p(A) = \exp(-A^2/A_R^2),$$
 (5.23)

where A_R^2 is the mean square value of A (i.e., proportional to the mean power). Ionospheric signals are, often, better described by a Rice distribution [7] in which a wave of steady amplitude (specular component) is added to the randomly varying signals. If A_s is the steady amplitude the distribution function is given by

$$p(A) = \frac{2}{A_R^2} \int_A^\infty A \exp\left[-\frac{A^2 + A_s^2}{A_R^2}\right] I_0\left(\frac{2AA_s}{A_R^2}\right) dA, \quad (5.24)$$

where I_0 is the Bessel function of zero order and imaginary argument.

For $A_s/A_R \ll 1$, the Rice distribution approaches the Rayleigh law. For $A_s/A_R \gg 1$ it approaches a normal distribution with mean A_s and standard deviation $0.707A_R$.

The amplitude distribution of a continuous wave, and of trains of long pulses, involving several paths, is usually close to Rayleigh. Individual modes resolved by short pulses often have shallower (and slower) fading corresponding to a substantial specular component, $A_s/A_R = 2$ or more.

With a Rayleigh distribution, the median amplitude is equal to 0.832 times the rms value. For such a distribution the lower decile value, or the amplitude exceeded 90 percent of the time, is 0.39 of the median value. The upper decile value, that is the value exceeded 10 percent of the time, is 1.8 times the mean value.

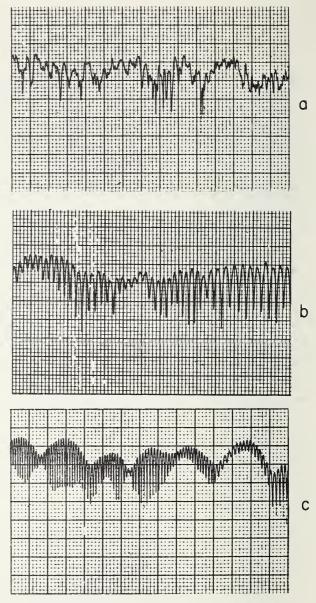


Figure 5.17. Examples of the amplitude fading of WWV-20 received at Boulder, Colo. (2370 km).

⁽a) random; (b) periodic; (c) double periodic. (After J. Auterman, unpublished.)

Some examples of (a) random, (b) periodic, and (c) double periodic fading of WWV-20 as received in Boulder, Colo., are shown in figure 5.17. The periodic fading in figure 5.16b, that is sharp minima and blunt maxima, is the resultant of two sine waves of almost equal amplitude whose phase difference is changing at a constant rate. In figure 5.17c the short-period fading could be due to high and low rays and the long-period fading could be due to beating between ordinary and extraordinary waves.

Very bad interference fading is experienced in cases where the sky-groundwave and skywave amplitudes are comparable. This combination produces much more severe fading than is usually experienced with skywaves alone. A somewhat related type of interference fading is experienced primarily on low frequencies, where radio transmission is relatively stable. Near sunrise and sunset the heights of the reflecting D layer change rather rapidly, and the skywaves arrive alternatively in and out of phase with the groundwaves. This produces fading with a relatively long period.

Flutter fading is experienced near the auroral zone during disturbed periods and often, during normal conditions, in transequatorial propagation. It is also experienced in certain types of scatter transmission. The fading rate is usually in the range of 10 to 100 c/s; indeed it is so fast that normal pen recorders cannot always follow the fluctuations. With such equipment, the fading depth appears to decrease.

5.4.3. The Fading Power Spectrum

The speed of fading can be described in terms of the time auto-correlation function of the amplitude or, equivalently, in terms of the fading frequency power spectrum which is the Fourier transform of the autocorrelation function. If A(t) represents the amplitude as a function of time, such that the average value is constant over the interval t to t+T, the autocorrelation function $\rho(\tau)$ is defined by

$$\rho(\tau) = \frac{1}{T} \int_{t}^{t+\tau} A(t) A(t+\tau) dt. \tag{5.25}$$

If ν represents the fading frequency and if $F(\nu)$ is the Fourier transform

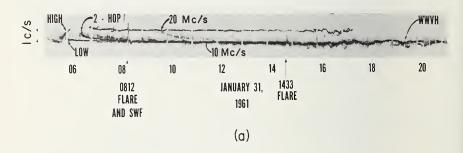
of A(t), that is

$$F(\nu) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} A(t) \exp(-i\nu t) dt,$$
 (5.26)

the power spectrum $P(\nu)$ of the fading is $P(\nu) = |F(\nu)|^2$ which is proportional to $\int \rho(\tau) \exp(-i\nu\tau) d\tau$: the Fourier transform of $\rho(\tau)$.

No matter how irregular the ionosphere the amplitude of the signal at a fixed receiver would be steady if there were no time variations in the ionosphere. The width of the power spectrum (the speed of fading) is in fact related to changes in the ionosphere and/or to changes in the position of the receiver (for a fixed transmitter).

A convenient method of depicting the fading spectrum is that described in section 3.2.3.2, in which the fading frequency is multiplied so as to produce an audio tone which is then analyzed by conventional audio techniques. Some examples of the variations in the spectra, on quiet and disturbed days, are shown in figures 5.18a and b respectively. The frequency spectrum of flutter fading signals transmitted near the magnetic equator is shown in figure 5.19. When the fading speed is high, the spectrum is broad, and vice versa.



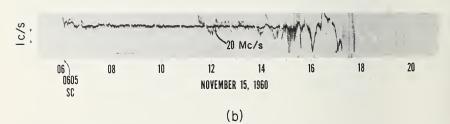


FIGURE 5.18. Frequency spectra of WWV (10 Mc/s and 20 Mc/s) as observed at Boulder, Colo. (2370 km).

⁽a) Magnetically quiet conditions. (b) Magnetically disturbed conditions.

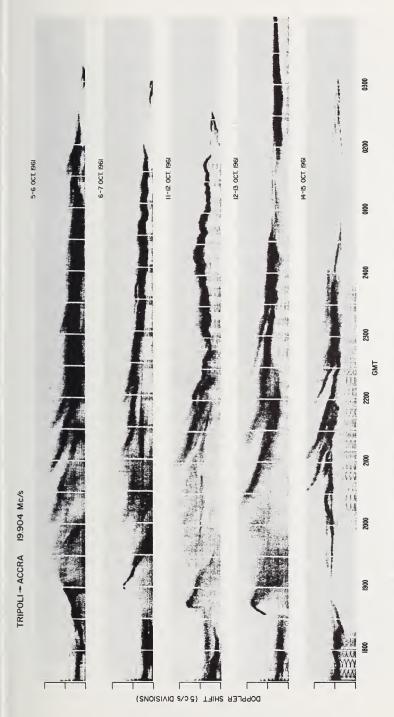


FIGURE 5.19. The frequency spectra of flutter fading signals over the path Tripoli, Libya to Accra, Chana (3300 km) attributed to the motion of spread F irregularities near the magnetic dip equator.

5.4.4. Scintillations4

This refers to the amplitude and phase variations of high-frequency signals transmitted through the ionosphere from outside the earth. The two common sources are cosmic noise from outer space and signals from artificial satellites. When a radio wave travels through an irregular ionosphere the latter behaves as a diffraction grating so that there is a redistribution in the amplitude of the wave with position which results in fading due to ionospheric movement. There are also irregular fluctuations in the apparent position of a radio source viewed through the ionosphere. These two processes are usually described as amplitude and angular scintillations, respectively [8].

The phenomenon can best be treated by reference to a thin phase-changing screen [9, 10]. Let us consider a plane wave incident upon the ionosphere such that no absorption of the wave takes place. Immediately below the region containing such irregularities the surface of constant phase in the emergent wave will be corrugated in an irregular way. The amplitude distribution will, however, still be uniform since no energy is extracted from the wave.

In order to investigate the process by which amplitude variations are built up from the pure phase-modulated wave, it is convenient to consider the angular spectrum of the wave. The angular spectrum of a phase-changing screen is analogous to the frequency spectrum of a phase-modulated carrier wave, the deviation in angle of a particular component being equivalent to the shift in frequency of a particular side band with respect to the carrier wave. For the case of a phase-modulated carrier wave it is well known that the side bands occur not only at all the frequencies in the Fourier analyis of the phase-modulation but also at sums and differences and multiples of these frequencies, and the relative magnitude of these side bands depends on the phase deviation. By analogy it can be shown for the case of diffraction, without specifying the screen in any detail, that the total spread of the angular spectrum depends on the phase deviation as well as on the lateral scale of the phase variations.

Now the phase relationship between the components of the angular spectrum is such as to produce a pure phase modulation at the screen itself. As the wavefront leaves the screen, however, the relative phases will be changed owing to the different directions of propagation within the angular spectrum; and, in this way, amplitude variations will be

⁴ Taken from a lecture by Dr. H. J. A. Chivers.

introduced into the diffraction pattern. The amplitude variations will grow in magnitude as the distance from the screen is increased until the initial phase relationship is entirely destroyed. The more deeply modulated the screen, the wider will be the angular spectrum, and the finer the structure in the diffraction pattern.

As long as the average phase changes introduced by the diffracting screen are less than about 1 rad (radian), then the scale size of the irregularities observed on the ground is the same as the scale of the irregularities in the ionosphere. If the average phase changes are greater than 1 rad, then the scale of the pattern observed at a distant plane is smaller than the scale size in the ionosphere by a factor equal in magnitude to the average phase change in radians.

Hence, in cases where the average phase changes are less than 1 rad, the scale of the irregular structure of the emergent radio wave is the same in all planes below the screen. In this case it has been shown [11] that the amplitude variations become fully developed at a distance where an average irregularity in the ionosphere occupies about the size of the first Fresnel zone radius. For a screen viewed from a distance R, observing at a wavelength λ , the Fresnel zone radius is given by $\sqrt{R\lambda}$.

In the case of a transmitting earth satellite, the radio wave incident on the ionosphere will have a spherical wavefront if the satellite is at a low altitude. Therefore, in the satellite case, we must consider the distance from the satellite to the irregular layer as well as the layer-to-earth distance. When the satellite is located at the bottom of the layer of irregularities, then the Fresnel zone radius is only half the radio wavelength; and, to observe strong scintillations at the ground, there must be substantial phase changes over this order of distance in the ionosphere. Such a situation is unlikely, so scintillations will not be observed. As the distance from transmitter to the screen increases, the Fresnel zone radius increases so that, when the satellite-to-ionosphere and ionosphere-toground distances are equal (say R), then the Fresnel zone radius is $\sqrt{R\lambda/2}$. Hence for a given receiving station, the Fresnel zone distance is smaller for satellite observations than for radio star observations. Since the proportion of fluctuation in the observed signal depends on the average phase changes over distances comparable to the Fresnel zone distance, there will be proportionally smaller fluctuation in a satellite signal than in a radio star signal viewed through the same part of the ionosphere. The average voltage amplitude of the scintillations depends on the square of the average phase changes over the Fresnel zone distance [12]; therefore, the above calculation indicates that, when transmitter and receiver are equidistant from the ionosphere, the amount of scintillation is about

one-half of that to be expected from a radio star observed at the same time and in the same direction.

In order to estimate the magnitude of the irregular component in electron density which is necessary to produce scintillations, we must first compute the total change in phase path length which is imposed on a radio wave in traversing the ionosphere, then consider the fractional variation in this path which will result in phase differences of about one radian in waves emerging at places separated by approximately the Fresnel zone radius.

The total phase path length P from source to receiver is given by

$$\int_0^s \mu \ ds,$$

where μ is the refractive index and s the source distance. Hence, the difference in phase path length introduced by the ionization is

$$\int ds - \int \mu ds = \Delta P.$$

Now, when the wave frequency is high compared with the plasma frequency (f_N) we have, from (2.78),

$$\mu \approx 1 - \frac{1}{2} \left(\frac{f_N}{f} \right)^2, \tag{5.27}$$

and hence

$$\Delta P \approx \frac{1}{2f^2} \int_0^s f_N^2 ds = \frac{40.5}{f^2} \int_0^s N ds.$$
 (5.28)

Taking the typical value 10^{17} electrons/m² column for $\int N \, ds$ and assuming a radio wave frequency of 40 Mc/s (4×10⁷ c/s), we get $\Delta P \approx 2500$ m. This corresponds to about 2000 rad at 40 Mc/s. Now, if we take as a typical value for the distance to the irregularities 400 km, then the Fresnel zone radius $\sqrt{R\lambda}$, for 40 Mc/s observations, is approximately 2000 m.

Since for strong scintillations we require changes in phase of about 1 rad over the Fresnel zone distance, the calculations show that on 40 Mc/s there must be differences in electron density of about 1 part in 2000 over distances of about 2000 m. Such variations can be expected

to be quite common, indicating that scintillations on $40~\mathrm{Mc/s}$ would be observed very frequently. This is, in fact, the case.

A similar calculation for a radio frequency of 400 Mc/s shows that electron density variations of 1 part in 200 are required over distances of about 500 m. Since this distance is of the same order as the mean free path for electrons in the ionosphere, it is unlikely that there would be sufficiently rapid density variations to cause scintillations at 400 Mc/s. Experimental observations support this conclusion; strong scintillations at 400 Mc/s are normally observed only during auroral disturbances or at the magnetic equator, where the horizontal field inhibits vertical diffusion.

Using the above approach, some idea can be obtained of the expected variation of scintillation activity with the elevation angle at which observations are made. With decreasing elevation angles, the effective thickness of the ionosphere increases. In addition, the radius of the first Fresnel zone increases as the square root of the slant range. The two facts combined mean that smaller fractional deviations in electron content occurring over greater distances can cause scintillations at low elevations compared with variations necessary at high elevations. Thus it can be expected that, at low elevations, scintillations will be more common and more intense than at high elevations. Again this is supported by experimental evidence.

Scintillations are apparent in both the amplitude and phase variations of the received signal. Amplitude variations are the more simple to observe and have consequently received the greater attention. In radio star work a moderately directional antenna system is required for straightforward observations of the brightest radio sources. The output of the second detector of a sensitive superheterodyne receiver is amplified and displayed on a pen recorder, and scintillations are revealed as a marked fluctuation of the recorded trace in excess of the smoothed noise fluctuations normally seen at the output. Samples of the output of such a receiving system are shown in figure 5.20. The top trace (a) shows the recorded noise level in the absence of scintillations, the middle trace (b) shows moderate scintillations, while the lower trace (c) indicates very intense scintillations. The records were made using a radio frequency of 80 Me/s by observing the intense radio source in Cassiopeia (23N5A).

In the case of satellite observations, the signal-to-noise ratio is usually higher than that from a radio star; hence a very simple antenna will suffice to give good records. A simple antenna has the advantage of extensive sky coverage, thus avoiding the necessity of steering the antenna to follow the satellite.

Simple amplitude experiments are usually confined to routine observations to investigate the diurnal, seasonal, and other time changes in

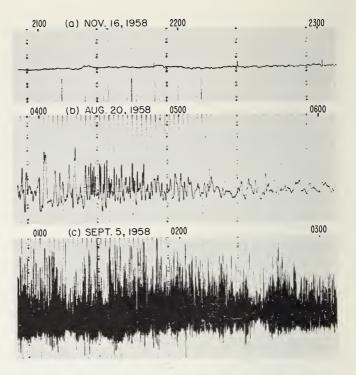


Figure 5.20. Amplitude recordings on 80 Mc/s of Cassiopeia-A showing (a) no scintillations, (b) moderate scintillations, and (c) strong scintillations.

(After H. J. A. Chivers, 1960, J. Atmospheric Terrest. Phys. 19, 54.)

the phenomena. Similar observations at two or more independent sites can be used to assess the size and shape of the electron density irregularities which cause the scintillations, and to indicate their apparent movement.

Phase scintillations can most easily be observed by measuring the irregular variations in the times of lobe crossing in the output from a system using two antennas as an interferometer. Such a system is the analog of the Michelson interferometer in optics. When used in its simplest form, it suffers from the disadvantage that the relative motion of a radio star through the lobes gives a very slow rate of information. For both the radio star and satellite cases, it is common practice to sweep the lobe structure across the sky in order to increase the rate at which phase-scintillation measurements can be made.

The depth of fading falls off with increasing frequency. This is measured by a fluctuation index which is the mean variation in received

power relative to the average power. For normal scintillations, this index varies from about unity at 30 Mc/s to a small value at 300 Mc/s. Scintillations have been reported on frequencies as high as 900 Mc/s, but tropospheric effects cannot be ruled out on this frequency.

The rate of scintillation, in the case of radio stars, varies from about 0.1 per minute to around 10 per minute. The scintillation rate appears to be independent of wave frequency down to about 30 Mc/s. When satellites are used as sources, the scintillation rate depends mainly on the height and speed of the satellite and on the height of the irregularities. Sample values are around 10 fades per second.

The variation in angular position of a radio star is usually a few minutes of arc on 36 Mc/s with an observed upper limit of about 0.5°.

The diurnal variation of scintillations in temperate latitudes at low sunspot numbers shows a peak of occurrence at night but little by day. In high latitudes and during high solar activity the distinction between day and night disappears. The seasonal variation is characterized by peaks during the equinoctial months. It is fairly closely correlated with the occurrence of spread F.

5.4.5. Fading Correlation Bandwidth

Because phase path differences in multipath propagation are a function of the wavelength, the fading on adjacent frequencies tends to be different. As the frequency difference $\delta\omega$ increases the correlation between fading on frequencies of ω_0 and $\omega_0 + \delta\omega$ will decrease and, at a sufficiently large difference, the fading on the two channels will be unrelated. This selective fading can produce distortion in an amplitude modulated wave (double sideband) if the carrier fades to a level below that of the sidebands. This gives an effect similar to overmodulation. On high frequencies, for a CW signal, the bandwidth of correlation is found to be around 3 kc/s and even less under severely disturbed conditions on arctic paths. Single pulse signals without overlapping time may have a correlation bandwidth of 40 kc/s or so.

5.4.6. Reciprocity

A radio signal of given frequency traveling from A to B may be expected to exhibit the same fading as a similar signal received at A from B. Although this is true as far as paths and amplitudes are concerned,

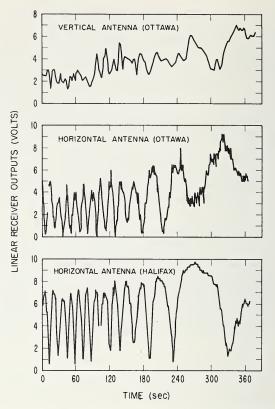


Figure 5.21. Nonreciprocal (polarization) fading over the 960-km path Ottawa-Halifax, Canada.

11.45 Mc/s F layer low-angle ray (o+x), 18:15:20–18:21:20 UT, March 28, 1962. (After G. W. Jull and G. W. E. Pettersen, unpublished.)

Budden [13] has shown that the phases at the opposite terminals can be reversed. This implies a degree of nonreciprocal fading the existence of which has been confirmed by a number of workers [14, 15]. The most important source of nonreciprocal fading appears to be polarization fading. Now reciprocity in polarization fading can be expected only for special orientations of linear antennas at each end of a (magnetically) north-south path. For transmissions along an ionospheric path entirely within either hemisphere, one condition for reciprocal polarization fading is that the antennas at the terminals must take equal and opposite angles with the direction of the earth's magnetic field. Thus for any arbitrary path orientation nonreciprocal polarization fading can be expected [16]. Observations by G. W. Jull (private communication) on signals trans-

mitted over the east-west path Ottawa, Ontario, to Halifax, Nova Scotia (960 km) have shown that time displacements in polarization fading maxima can occur. Time displacements of up to one-half a fading cycle were observed (see fig. 5.21).

5.4.7. Diversity [17]

To minimize the effect of fading on quality of reception, use can be made of the fact that fading is correlated only over relatively small distances, and frequency bandwidths. Also signals from antennas having different polarizations may fade differently.

Space diversity is obtained by mixing signals from antennas separated by distances greater than the correlation distance. This is the distance beyond which the correlation coefficient of the fading falls to some specified value (ϵ^{-1} say).

Frequency diversity is obtained by transmitting and receiving on frequencies separated by more than the correlation bandwidth. This method is not recommended as it is wasteful of the usable frequency spectrum.

Polarization diversity is useful when there are two magneto-ionic waves present with essentially equal amplitudes. As discussed in section 4.9.5.1, the resultant of such waves is, approximately, a linearly polarized wave which rotates steadily so that sinusoidal (Faraday) fading would be observed with a linearly polarized antenna. Deep fading can be avoided by the use of two orthogonal antennas. There is little point in using polarization diversity when only one magneto-ionic component is likely to be present.

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CHAPTER 6

Ionospheric Disturbances

6.1. TYPES OF DISTURBANCE

The term "ionospheric disturbance" is used to cover a wide variety of ionospheric conditions that show some departure from the usual state. Thus slight perturbations in the electron configuration that move with time are called traveling disturbances. These are usually localized in space. From the point of view of radio transmission, these traveling disturbances are not nearly so important as the more (geographically) extensive disturbances which are all associated, in some way or another, with a flare on the sun (see section 1.7.6).

These solar flare associated effects may be classified as follows:

- (1) Sudden ionospheric disturbances,
- (2) ionospheric storms,
- (3) polar cap absorption events (PCAs).

The reason these disturbances are important from the point of view of radio communications is that they often result in interruption of communications. The absorption in the D region is enhanced so much that intelligible radio communications may be impossible for periods lasting from a few minutes to several days. Furthermore, the critical frequencies of the F_2 layer are sometimes depressed (ionospheric storms), resulting in loss of signal due to MUF failure. It is a very difficult matter to predict the onset of an ionospheric disturbance and since the ionospheric conditions can change rapidly from very quiet to highly disturbed, the idea of "average" conditions (e.g., path loss, maximum frequency, etc.) tends to have only limited value. The purpose of this chapter is to outline the effects of these disturbances on radio signals and to discuss some ways of dealing with the problems.

Before discussing these various phenomena in detail, however, it is useful to consider the general pattern a little further. Although all the regular layers (D, E, and F) are affected, the E layer is not strongly affected except for the occurrence of sporadic E in certain ionospheric

storms. The D and F layers are subject to much stronger effects. The D region effects often occur simultaneously with the appearance of an optical solar flare, whereas the F region effects are often delayed by a day or more. These simultaneous and delayed effects are illustrated in figure 6.1.

We have seen (sec. 1.7.6) that the occurrence of a solar flare may be accompanied by the emission of radio waves, ultraviolet, and x rays, all of which arrive simultaneously at the earth because they travel with the free space velocity of light (essentially). Solar cosmic rays are also emitted with relativistic velocities and these may take 15 min to several hours to reach the earth, where they produce polar cap absorption. Slower particles, which have transit times of from 20 to 40 hr, result in ionospheric storms, magnetic storms, and visible displays of the aurora borealis. It should be remembered, of course, that not all the effects shown in figure 6.1 are associated with every flare.

6.2. SUDDEN IONOSPHERIC DISTURBANCES

6.2.1. D-Region Absorption

At times, communications on high frequencies by skywave propagation over the daylight hemisphere of the earth are "blacked out" by abnormally high absorption in the D region. The association between these shortwave fadeouts (SWF) and solar flares was discovered by Dellinger [1]. The condition of high absorption may last from a few minutes to several hours. Onset of this absorption is usually, but not always, very sudden (hence the name "sudden ionospheric disturbance," SID); it is followed by a relatively slow recovery, as shown in figure 6.2. Shortwave fadeouts (SWFs) are sometimes accompanied by transient variations in the earth's magnetic field (fig. 6.2) indicating the existence of electric currents in the D region. Not all shortwave fadeouts are sudden and, at the National Bureau of Standards, SWFs are described as sudden, slow, or gradual, depending on the time variation of the recorded signal. Information on the occurrence of ionospheric effects of solar flares is given in CRPL F Series, B, Solar Geophysical Data, issued monthly by the National Bureau of Standards. The production of ionization in the D region gives rise to associated phenomena such as the sudden absorption of cosmic noise (SCNA) received on frequencies above the F₂ layer

¹ Figures in brackets indicate the literaturé references on p. 287.

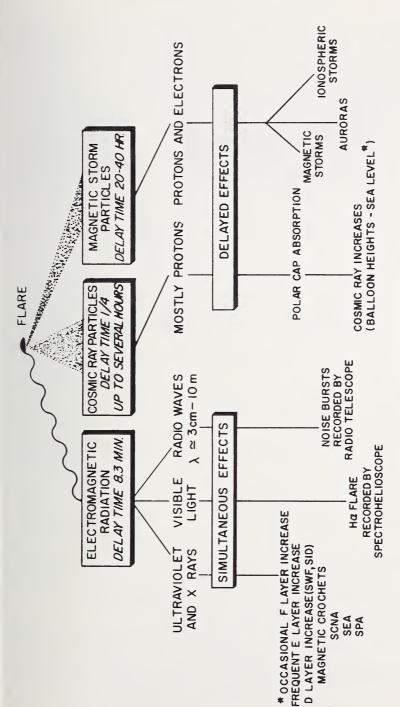


FIGURE 6.1. The terrestrial effects of a solar flare

(After R. W. Knecht, unpublished.)

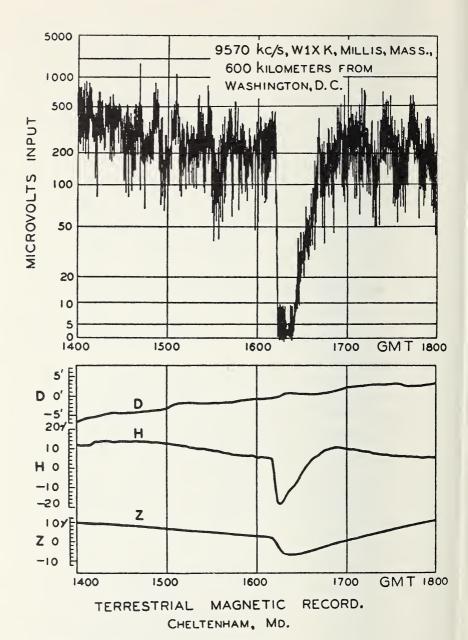


Figure 6.2. Example of a shortwave fadeout and magnetic disturbance on November 26, 1936.

(After J. H. Dellinger, 1937, Sudden disturbances of the ionosphere, J. Res. NBS 19; Proc. IRE 25, 1253; and Terr. Mag. and Atmos. Elec. 42, 49-53).

critical frequency, the sudden phase anomaly on very low frequencies (SPA), and the sudden enhancement of atmospherics on very low frequencies (SEA). From the point of view of interruption of radio communications, shortwave fadeouts are not too serious, but they do constitute a nuisance. The following data on SWFs observed at Washington, D.C., give an idea of this nuisance value. During the sunspot maximum year of 1937, SWFs were observed on 84 days. On 66 of these the fadeout was classified as intense. On 39 days there was more than one SWF and on 33 days the fadeout lasted for more than 1 hr. On the other hand, in the sunspot minimum year of 1944, the corresponding numbers were only 5, 3, 0, and 2. In the sunspot maximum year of 1947 they were again high: 121, 104, 54, and 33.

The height in the atmosphere at which the additional electrons are produced during a solar flare is of importance because it determines the dependence of the absorption on wave frequency. Figure 6.3 shows the time variation of absorption of 10 Mc/s cosmic noise at College, Alaska during a large solar flare on July 11, 1961. From the ratio of the absorption of the ordinary and extraordinary waves it is found that the frequency dependence is given by $(f\pm f_L)^{-2}$, from which we infer (using 2.103) that the absorption is taking place at a level where $(\omega\pm\omega_L)^2\gg^2$.

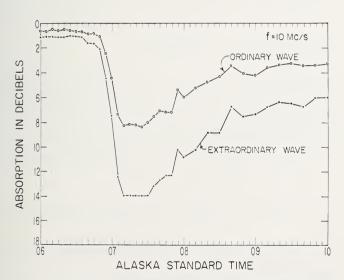


Figure 6.3. Solar flare absorption on 10 Mc/s, College, Alaska, June 11, 1961.

(After R. S. Lawrence, C. G. Little, and H. J. A. Chivers, 1964, A survey of ionospheric effects upon earth-space radio propagation, Proc. IEE 52, No. 1, p. 4.)

On the other hand, there is evidence which indicates that absorption can occur at low levels such that $(\omega \pm \omega_L)$ is comparable with ν . It is of interest to note that during the flare of July 11, 1961, the absorption in the D region increased by a factor of the order of 10.

The vast majority of radio fadeouts is associated with solar flares. Therefore, they exhibit the same 11-yr occurrence cycle as do flares and sunspots. In general, the magnitude of the SID depends on the solar zenith angle.

Shortwave fadeouts have been studied using measurements of the minimum frequencies observed on ionograms [3] (see sec. 3.2.2.4.) to give a synoptic picture of the worldwide distribution. It has been found that f_{\min} varies as $\cos^{0.75} \chi$, where χ is the solar zenith angle.

6.2.2. Sudden Phase Anomalies

The increase of ionization in the *D* region produces an effect on the phase and amplitude of long and very long waves—usually a phase advance due to a lowering of the effective level of reflection. Changes in the effective height of reflection of from 0.9 to 15 km have been reported [4]. There appeared to be a threshold value of this height change of about 6 km, above which SPAs were accompanied by SWFs.

6.2.3. Sudden Frequency Deviations

During a solar flare, it is found that the frequency of a very stable radio signal, observed after reflection from the ionosphere, undergoes certain characteristic changes of a few cycles per second. The technique has already been described in section 2.5.3.

An increase in the electron content of the ionosphere usually brings about a decrease in the phase path of ionospherically reflected signals because of one or both of the following reasons:

- (1) A lowering of the height of reflection, or
- (2) A lowering of the refractive index along the path below the level of reflection.

It is possible to separate these two types of changes under the following extreme conditions:

(a) When the height of the reflecting layer changes without change of layer shape, and/or the refractive index

$$\mu\left(=\sqrt{1-k\frac{N}{f^2}}\right)$$

is approximately equal to

$$\left(1-\tfrac{1}{2}k\,\frac{N}{f^2}\right).$$

(b) When the electron content increases in a layer, below the reflection level, in which the refractive index is approximately unity, i.e., non-deviative.

Under condition (a) the phase path P is independent of wave frequency f. Under condition (b) the refractive index

$$\mu = \sqrt{1 - k(N/f^2)} \approx 1 - \frac{1}{2}k(N/f^2)$$
,

where N is the electron density and k is a constant (see 2.78). Substitution of these conditions into (2.128) shows that the change Δf in frequency is related to the carrier frequency by the formulas:

$$\Delta f \propto f$$
, (a)
$$\Delta f \propto 1/f$$
. (b)

If the effect of the earth's magnetic field is included and the propagation conditions are quasi-longitudinal, (6.1a) remains unchanged but (6.1b) is modified as follows:

$$\Delta f \propto \frac{1}{f \pm f_L},\tag{6.2}$$

where the + and - signs refer to the ordinary and extraordinary waves, respectively.

An example of the effect of a solar flare on the reception of WWV-10 is shown in figure 6.4. The frequency increases to a peak, then drops rapidly, overshoots, and recovers slowly. The total change in phase path

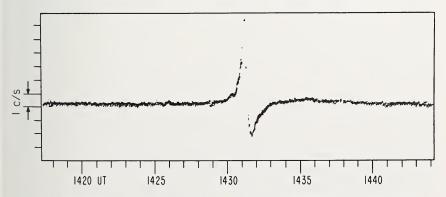


FIGURE 6.4. Effect of solar flare on received frequency of WWV, September 4, 1961.

 ΔP can be determined from the area under the curve, i.e.,

$$\Delta P = -\lambda_0 \int \Delta f \, dt, \tag{6.3}$$

where λ_0 is the free space wavelength. With the use of suitable models to represent the electron density profile, it is possible to convert the phase path changes into changes in total electron content or changes in height of reflection.

It is of interest to note that the following equivalence exists between frequency shifts on oblique and vertical paths [19].

$$\Delta f_{ob} = \Delta f_v, \tag{6.4}$$

where Δf_{ob} is the frequency shift on a wave transmitted over an oblique path and Δf_v is the frequency shift on the equivalent vertical wave (see 4.2).

In the case of changes below the level of reflection, it is possible to estimate the height at which the extra electrons are produced from simultaneous measurements of the changes in absorption ΔA of the signal and in phase path ΔP . It can be shown (using (2.100) and the definition of phase path, $P = \int \mu \ ds$) that for a thin layer, in which the ray path length is s, that

$$A = \kappa s = \frac{\nu}{2c} \left(\frac{1}{\mu} - \mu \right) s$$

and

$$P = \mu s$$
.

Hence

$$\Delta A = -\frac{\nu}{2c} \left(\frac{1}{\mu^2} + 1\right) \Delta \mu s \approx -\frac{\nu}{c} \Delta \mu s$$

and

$$\Delta P = \Delta \mu s$$
.

$$\frac{\Delta A}{\Delta P} = -\frac{\nu}{c} \,. \tag{6.5}$$

Knowing the variation with height of the collision frequency ν , it is possible to estimate an average height of electron production. Application of this theory to experimental data shows that, while no two flares produce identical results, most of the observed frequency changes are due to enhanced ionization in the E region [5].

Flares that produce shortwave fadeouts are not necessarily those that produce the large frequency changes. Indeed some flares, which have produced large absorption by the creation of a relatively small number of electrons at levels where the collision frequency is high, produce little frequency change.

6.2.4. Effects on Very High Frequencies

Very high frequency waves (50 Mc/s) are propagated via the *D* region by scattering from ionospheric irregularities. During shortwave fadeouts it has been found that these signals are enhanced by as much as 9 dB and there is little evidence of any weakening of the signal (on 50 Mc/s) during an HF blackout [6]. However, on 27.7 Mc/s it was found that the signal enhancement lasted for a few minutes only and was followed by marked attenuation [7]. From these observations it would be concluded that the scattering occurred in the absorbing region and that the increased absorption was compensated for by increased scattering on the higher frequency but not on the lower frequency.

6.3. IONOSPHERIC STORMS

6.3.1. Association with Magnetic Storms

The term "ionospheric storm" is used to describe the conditions which may prevail for several days and which are accompanied by magnetic disturbances of the type referred to in section 1.5.3. It is, therefore, of interest to consider briefly the characteristics of magnetic storms.

Magnetic storms are disturbances of the earth's magnetic field lasting from a few hours to several days during which time the various components of the earth's field fluctuates over much wider limits (several percent of the total field in middle latitudes) than they do under normal conditions (a few tenths of one percent). In spite of the irregularity of the field the overall pattern can generally be classified into certain types.

One such type is that which begins with a sudden commencement (SC) which is essentially simultaneous all over the world. During the first few hours (the initial phase) the horizontal component remains above normal; then it drops rapidly to well below normal (the main or negative phase). After this a slow recovery takes place over several days and this is called the post-perturbation phase. Magnetic disturbance is usually most intense in the vicinity of the auroral zones.

Large magnetic storms with either sudden or gradual commencement are accompanied by one or more of certain ionospheric phenomena such as: a depression of the daytime critical frequencies of the F_2 layer, radio blackout, enhanced spread F, and sporadic E. These ionospheric effects may last from 2 to 5 or more days. During sunspot maximum years there is a tendency for the effects to be shorter (2 to 3 days) and more severe while during sunspot minimum they tend to last longer (4 to 5 days) and are rather less intense.

6.3.2. Depression of F₂ Critical Frequencies

The most prominent features of ionospheric storms are the reduction in the F_2 critical frequencies and the increase in D region absorption. The practical consequence of this lowering of the maximum usable frequency and increase in the lowest usable frequency is a narrowing of the usable frequency spectrum. The effects of a magnetic storm on f_0F_2 at a given location depend, in an involved way, upon the local time, season, magnetic latitude, and the storm time (that is, time measured from the onset of the storm).

Figure 6.5 shows the effect, on critical frequencies, of a storm in middle latitudes. The associated magnetic storm had the following time sequence:

```
Start—about 0400 LT, March 26;
Maximum—morning, March 27 (K=8+; see section 1.5.4.);
End—late, March 29.
```

On the f plots for the second and third days, f_0F_2 is well below normal and the maximum electron density at noon is down by a factor of seven. Note also the appearance of the F_1 layer. On the fourth day, the daytime f_0F_2 s return towards normal, but depressed values and spread F (solid vertical lines in f plot) continue during the night hours for several additional days (not shown). In certain latitudes, when the storm starts in the afternoon, the first effect on f_0F_2 is an increase rather than a decrease. Later the usual decrease sets in.

Some results of a statistical study of the morphology (space and time variations) of ionospheric storms, by Matsushita [8], are shown in figure 6.6. The world is divided into eight zones of geomagnetic latitude as follows: zone 1, $60^{\circ}-55^{\circ}$; zone 2, $55^{\circ}-50^{\circ}$; zone 3, $50^{\circ}-45^{\circ}$; zone 4, $45^{\circ}-40^{\circ}$; zone 5, $40^{\circ}-29^{\circ}$; zone 6, $29^{\circ}-20^{\circ}$; zone 7, $20^{\circ}-9^{\circ}$; and zone 8, $+9^{\circ}$ to -9° . The results shown represent the average effects of 51 strong storms and 58 weak storms that occurred in the period 1946 through 1955. It will be seen that the most severe depressions in electron

density (and hence f_0F_2) occur between about 20 and 40 hr storm time in geomagnetic latitudes of 45° and higher. In intermediate latitudes only a mild depression occurs, and in equatorial regions an actual increase is observed. Note also, that an initial *increase* tends to occur during the first 9 hr or so of the storm in all zones except those with the lowest latitudes. Of course, it must be realized that this is the statistical picture and so an individual storm will not necessarily follow this pattern.

In addition to the storm time variations there are marked variations which depend on the local time. Thus the time of maximum depression of $N_{\rm max}$ depends on local time. Some useful factual data are presented in table 6.1 (after Matsushita), showing how the times (local and storm) of maximum depression depend on magnetic latitude.

Table 6.1. Variation with geomagnetic latitude of times of peak depression of $N_{\rm max}$ F_2 during a storm

| (A) | (B) | (C) | (D) |
|---|---|--|--|
| Zone | Decrease (%) | Local Time (Hours) | Storm Time (Hours) |
| 60°-55° 55°-50° 50°-45° 45°-40° 40°-29° | 30–50 30–45 30–45 15–25 15–20 | $\begin{array}{c} 14-22 \\ 22-04 \\ 01-07 \\ 03-13 \\ 03-13 \end{array}$ | $ \begin{array}{c} 17-42 \\ 10-41 \\ 10-42 \\ 19-55 \\ 20-48 \end{array} $ |

The table should be interpreted as follows: In the zone given in column (A) a maximum decrease of about the percentage shown in (B) will occur at about the local time shown in (C) during the period after the onset of a strong magnetic storm with a sudden commencement indicated in (D).

The fact that the statistical picture in figure 6.6 can be a little misleading is shown by the seasonal variation of storm pattern in zone 6. The data shown would suggest that there is relatively little storm time variation in the F_2 layer in these latitudes. The results of a seasonal analysis, however, show that the electron density is depressed during the summer but enhanced in the winter. The overall average is, therefore, not representative of a single storm in either of those seasons.

6.3.3. Absorption

6.3.3.1. Blackout Statistics

During some magnetic storms, the absorption of radio waves in the D region is so intense that no detectable signals are reflected. This is

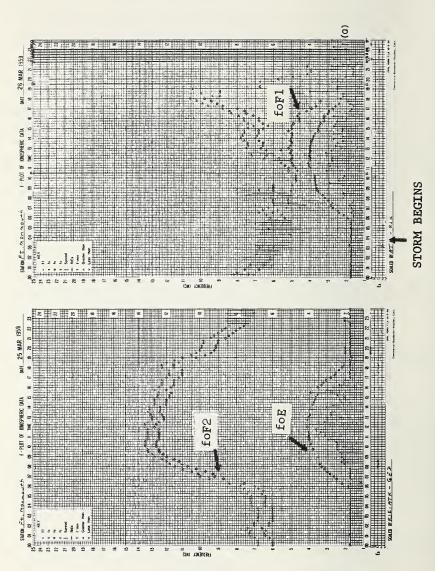


Figure 6.5. Ionospheric storm effects in middle latitudes.

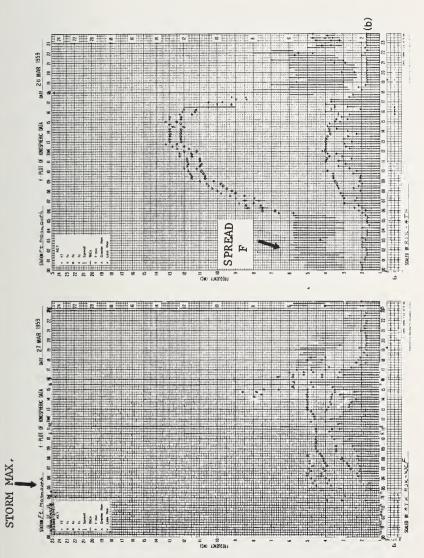


FIGURE 6.5.—Continued. Ionospheric storm effects in middle latitudes.

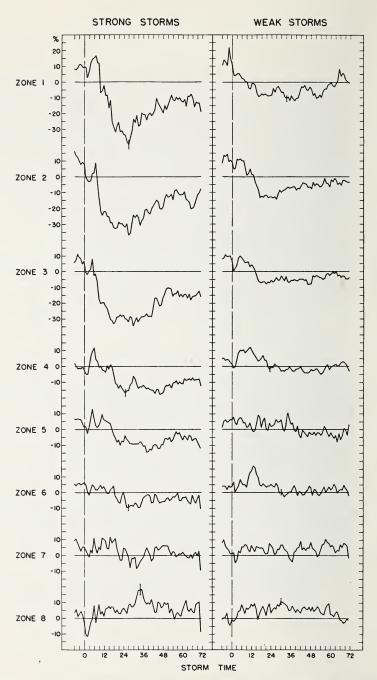


FIGURE 6.6. Storm time variations of maximum electron densities (F₂) in different latitudes. (After S. Matsushita, 1959, A study of the morphology of ionospheric storms, J. Geophys Res. 64, 305.)

particularly true near the auroral zones and the absorption is often referred to as auroral absorption or auroral blackout. These blackouts have been studied statistically by several workers [9, 10, 11] to determine the geographic and time distributions in their occurrence. The procedure has been to count the occurrences of the no-echo condition on conventional ionograms. This condition is denoted by the letter B on the hourly data sheets of ionospheric characteristics. Alternatively, a measure of absorption can be obtained from the minimum frequency f_{\min} observed on ionograms (see sec. 3.2.2.4). The occurrence of high absorption can be determined from the occasions when f_{\min} exceeds a certain frequency.

6.3.3.2. Time of Maximum Occurrence

The most probable time of occurrence of blackout is in the morning and the least probable in the evening. Furthermore, the most probable time is later as the latitude increases; for instance, it varies from about 0700 at Winnipeg to about 1300 at Resolute Bay. The geographical variation of the local time of maximum occurrence of blackout during the International Geophysical Year is shown in figure 6.7 for the northern

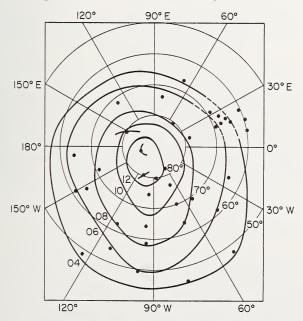


Figure 6.7. Local mean time of maximum frequency of occurrence of blackout, northern hemisphere-IGY.

(After V. Agy, unpublished.)

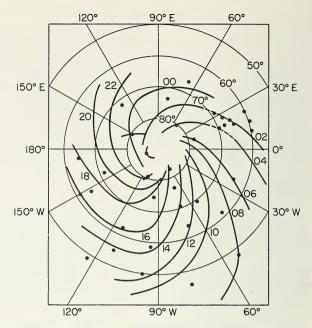


FIGURE 6.8. Universal time of maximum frequency of occurrence of blackout, northern hemisphere—IGY.

(After V. Agy, unpublished.)

hemisphere. Note that the lines of given time are not concentric with geographic latitude but are, roughly, circles centered on the geomagnetic pole. When plotted in universal time, the above circles are transformed into a series of arcs as shown in figure 6.8. These arcs have been called spirals by analogy with the Störmer-Birkeland spirals for the precipitation of ions in a dipole magnetic field, but this analogy may be quite misleading [12, 18].

6.3.3.3. Total Time of Occurrence

The amount of blackout as a fraction of the total time is shown in figure 6.9 for the various seasons during the International Geophysical Year 1957–58. It can be seen that the summer and winter patterns are very similar with two regions of high occurrence (8 percent), one over northern Scandinavia and the other over Alaska. During the equinox there appears to be a westward shift of the Alaska high and an increase of occurrence to around 10 percent. Because of the uncertain nature of the

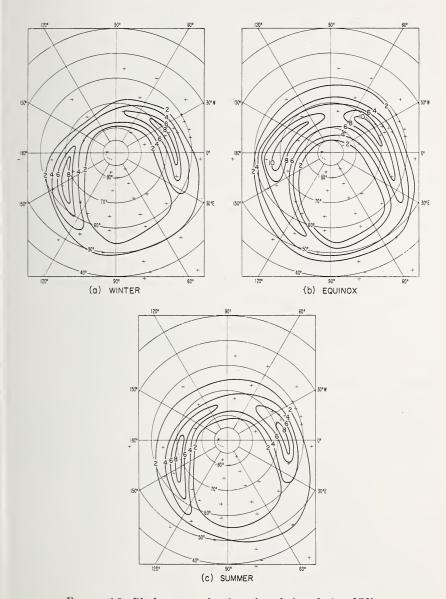


FIGURE 6.9. Blackout as a fraction of total time during IGY.

(After V. Agy, unpublished.)

data on which these maps are based, too much attention should not be paid to small variations. The average diurnal path of the blackout pattern for the equinox months is shown in figure 6.10. Notice that the blackout pattern moves around with the sun (shaded region represents darkness) and that the peak percentages vary with longitude. In all three seasons the maximum contour leads the sun by some 6 hr or so and the motion of the contours is relatively uniform except over Canada ($\approx 90^{\circ}$ west).

6.3.3.4. Latitude Variation

Maps such as those shown in figures 6.9 and 6.10 show that the maximum occurrence of blackout takes place in a ring similar to, but not necessarily identical with, the visual auroral zone. North of this zone there is a polar region in which the incidence of blackout is relatively low. The width of the absorption zone has not yet been established with certainty but appears to lie between about 6° [13] and about 15° [14]. This difference may be brought about by an increase in both the radius of the ring (southward motion) and a broadening with increasing sunspot numbers.

Within the auroral ring the average incidence of blackout is of the order of 5 percent [15], although at a small number of abnormally sensitive stations in the ring the average may rise to 15 percent.

6.3.3.5. Magnetic Correlation

In relatively low latitudes, outside the absorption ring, there is a high correlation with the K_p index. In higher latitudes, however, the magnetic correlation is obscured by the presence of polar cap absorption [14]. There is also a marked 27-day recurrence tendency in the occurrence of auroral absorption similar to that in magnetic activity [14].

6.3.3.6. Sunspot Variation

There appears to be a strong association between the 11-yr sunspot cycle and the long-term cycle of auroral blackout occurrence [14]. The peak phases of the two cycles are displaced by 2 to 3 yr. The peak in blackout occurrence over Canada took place around 1950–51, whereas the sunspot numbers peaked in 1947 and reached a minimum in 1954 [14]. This behavior is similar to that of moderate geomagnetic disturbances, which also fail to show a clear decrease at sunspot minimum.

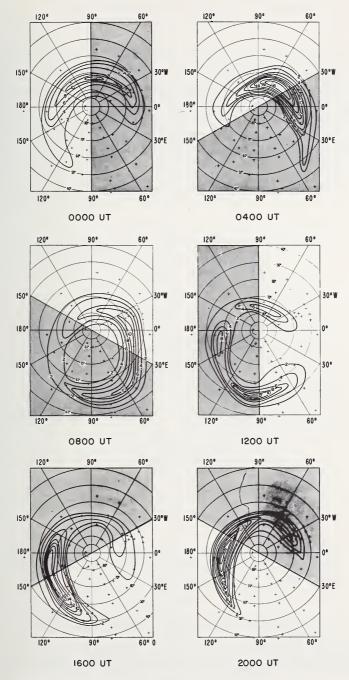


FIGURE 6.10. Diurnal changes in blackout patterns (equinox).

(After V. Agy, unpublished.)

6.3.4. Sporadic E

Certain types of E_s , those associated with magnetic activity, may be called storm E_s [16]. This type of E_s occurs frequently near the auroral ring during storms [17] and particularly during the nighttime. As in the case of blackout, statistical analyses show that the universal times of maximum occurrence of E_s lie on arcs [18] but the curvature of the arcs is in the opposite direction as shown in figure 6.11. This implies that the peak time occurs earlier in higher latitudes.

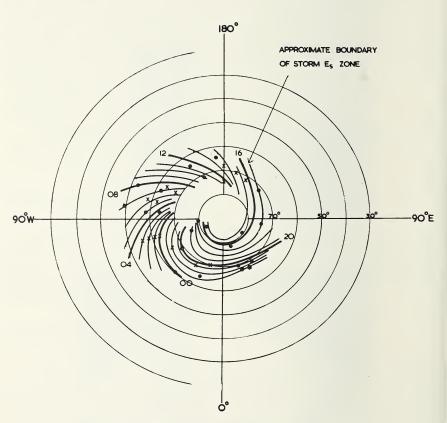


FIGURE 6.11. Time of maximum occurrence of storm Es.

Mean percent time of IGY "auroral zone" blackout occurrence, northern hemisphere. (After L. Thomas, 1960, The temporal distribution of storm-type sporadic E in the northern hemisphere, Some Ionospheric Results—International Geophysical Year (ed. W. J. G. Beynon), Elsevier Publ. Co., 172.)

6.4. POLAR CAP ABSORPTION

6.4.1. Duration

The majority of auroral blackouts is relatively short lived, lasting up to a maximum of 5 or 6 hr. The duration of long-lasting blackouts usually increases with latitude, as illustrated in figure 6.12. This type of disturbance is evidently associated with the polar regions and not with the auroral ring. Furthermore, it is not closely correlated with magnetic disturbance except, possibly, in its later stages. Polar cap absorption is believed to be due primarily to the ionizing effects of high-energy solar protons down to altitudes of the order of 50 km.

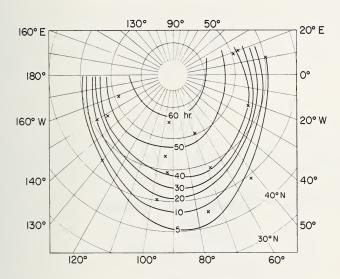


FIGURE 6.12. Average duration of eight long-lasting blackouts, 1949-52.

(After V. Agy, 1954, Geographic and temporal distribution of polar blackouts, J. Geophys. Res. 59, 499.)

Useful techniques for studying polar cap absorption are the riometer (sec. 3.2.2.3), VHF forward scatter [20], and partial reflections [21, 22]. Together with ionogram blackout data, these techniques have resulted in the determination of the geographic, temporal, and sunspot cycle variations of PCAs.

Some major characteristics of PCA events are as follows [23]:

(1) They are almost always preceded by a major solar flare on the visible hemisphere of the sun. The time interval between the appearance

of the flare and start of the PCA is from a fraction of an hour to several hours.

- (2) The duration is usually about 3 days but may be as short as 1 day; the longest may be about 10 days.
- (3) They are not usually accompanied by noticeable increases in either geomagnetic or auroral activity, except in the later stages when an auroral zone storm may set in.

Although there is a paucity of data for the south polar cap it is believed that PCA events occur simultaneously in both hemispheres.

6.4.2. Temporal Variations

Within a few hours after the solar flare, strong absorption occurs over the polar cap in geomagnetic latitudes greater than about 64°. The absorption attains its maximum within a few more hours and, thereafter, begins to decay. During the decay period, the radio wave absorption

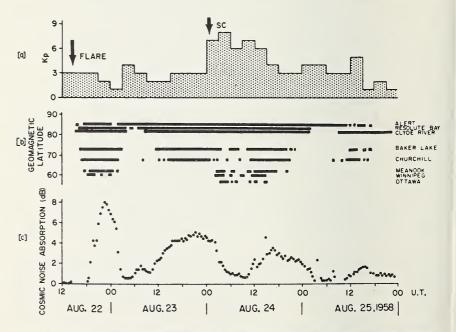


Figure 6.13. Cosmic noise absorption at Churchill and blackout pattern for northern stations, 22-25 August 1959.

(After C. Collins, D. H. Jelly, and A. G. Matthews, 1961, High-frequency radio-wave blackouts at medium and high latitudes during a solar cycle, Can. J. Phys. 39, 35.)

exhibits a pronounced diurnal variation. The daytime value is about four times greater (in decibels) than at night. An example of a PCA event is shown in figure 6.13. The absorption (c) was that measured at Churchill [24]. Ionogram blackout data show clearly the long duration in high latitudes. Notice that the absorption has occurred for about 32 hr before the onset of the magnetic storm.

The long-term variation in the occurrence of PCA events is shown in figure 6.14 together with the annual mean sunspot numbers. Clearly the events are closely associated with the general level of solar activity, as would be expected from their association with major flares.

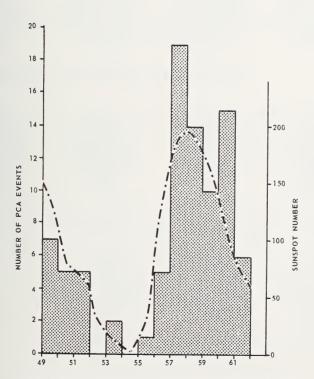


FIGURE 6.14. Distribution of polar cap absorption events 1949-1961.

(After D. H. Jelly, unpublished).

6.4.3. Geographical Extent

A sequence of events in the development of a PCA is shown in figure 6.15. This is based on f_{\min} data [25]. The time of a sudden commencement is indicated by the appearance of the geomagnetic coordinates. Notice that the PCA starts in a small area in relatively low latitudes and spreads until it engulfs the polar cap. The PCA finally breaks up into smaller regions which may be over the polar cap or in the auroral ring. This particular event should not be construed to be typical of all PCA events.



(UT)

FIGURE 6.15. Geographical development of a PCA, Oct. 20-23, 1957.

(After V. Agy, unpublished.)

6.4.4. Frequency Dependence of the Absorption

If the absorption takes place high in the D region, where $\nu\ll\omega$, we should expect the absorption to obey (2.99), whereas if it occurs very low down, where $\nu\gg\omega$, we should expect (2.101) to hold. The frequency dependence can, therefore, be used to determine (at least roughly) the altitude at which the absorption takes place. This approach has been used by Little and Silberstein [26] in an analysis of continuous wave transmissions between Barrow and Kenai, Alaska, on 5, 10, and 15 Mc/s along with riometer measurements on 50 Mc/s made by aiming the riometer antennas along the probable oblique HF paths at both ends. It was concluded that the inverse square law was inoperative on the lower frequencies and, therefore, that the absorption takes place at levels from 50 to 70 km.

6.5. EFFECTS ON RADIO COMMUNICATIONS IN HIGH LATITUDES

6.5.1. Some General Considerations

The effect of shortwave fadeouts on radio communications is so insignificant, especially in high latitudes where the solar zenith angle is large, that it will not be considered further. On the other hand, the effects brought about by storms and polar cap events are often catastrophic.

A lowering of the maximum frequency (due to depression of the critical frequency) and an increase in the lowest frequency (due to absorption) can occur separately or simultaneously. In all cases the effect is a narrowing of the usable frequency spectrum. The former often happens in middle latitudes and the latter has been observed near the auroral ring.

Ionospheric storms are frequently accompanied by spread F constituting a breaking up of the reflecting layer. This in turn brings about rapid fading called "auroral flutter." This flutter is disastrous to voice communication.

The combination of these effects makes HF communications via the auroral regions rather unreliable. Also, the southward extension of the auroral ring during storms disrupts communications between North America and Europe and relaying of the traffic through low-latitude stations is necessary. Thus, although ionospheric disturbance may last only 5 percent of the time, high-frequency communications cannot be used when 100 percent reliability is essential.

6.5.2. WWV Monitoring

Some information on the reliability of HF communications for paths into the Arctic from outside can be obtained from a monitoring of WWV carried out for many years in Canada. These data are published by the Defence Research Telecommunications Establishment, Ottawa, and consist of aural estimates of the strength of WWV, on frequencies of 2.5, 5.0, 10.0, 15.0, and 20.0 Mc/s using a range of 0 to 9. 0 denotes no signal and 9 denotes the strongest signals. This rather subjective approach has shown that one or others of the above frequencies is received over 90 per cent of the time at Resolute Bay, Baker Lake, and Churchill. During 1953–54 the percentage reception times were Churchill, about 90 percent; Baker Lake, 98 percent; Resolute Bay, 95 percent. The corresponding figures for 1957–58 were Churchill, 98 percent; Baker Lake, 98 percent; Resolute Bay, 95 percent. The relatively low value at Churchill for 1953–54 is due to MUF limitation (F₂) at low sunspot numbers.

These results might be interpreted as indicating that, with a free choice of frequencies (2.5 to 20 Mc/s), it would be possible to communicate between arctic and non-arctic stations over 95 percent of the time. However, this figure depends on the type of modulation used and the information rate required.

6.5.3. Some Path-Loss Data

From what has been said above, it will be realized that the most important factor in high-latitude radio propagation is the variability of ionospheric conditions rather than the average state. Thus propagation near the auroral ring is, for long periods, as good as elsewhere and at other times communications are entirely disrupted. To describe the conditions we need, in addition to an average value of some characteristic, a measure of the variability from hour to hour and from day to day.

Very little information of this sort is available; however, an experiment was carried out by the CRPL during the International Geophysical Year, using transmissions on 8 Mc/s over paths from Bismarck, North Dakota, to College, Alaska, and Anchorage, Alaska, and from Maui, Hawaii, to the same receiving locations (fig. 6.16). For the 9-month period April to December 1958, it was found that path loss (relative to that over the Maui-Anchorage path) over the four paths could be compared for the nighttime hours. The results are shown in table 6.2, from which we see the marked increase in path loss for those circuits nearest the auroral

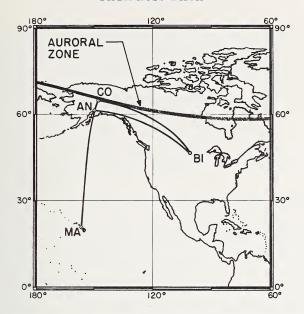


FIGURE 6.16. Transmission circuits near the auroral ring.

CO—College, AN—Anchorage, BI—Bismark, MA—Maui.

(After V. Agy, unpublished.)

TABLE 6.2. Path loss relative to Maui-Anchorage (dB) (2200-2400 150° WMT: April-December, 1958)

| | Receiver | |
|------------------|-----------|---------|
| Transmitter | Anchorage | College |
| Maui Bismarck | 0 12 | 7 22 |

(These values have been corrected for the difference in path and transmitter power).

ring. It must be borne in mind that these data are for (a) specific paths, (2) nighttime, (3) monthly mean conditions averaged over 9 months, and (4) the peak of the sunspot cycle.

The dispersion of the night-to-night data is shown in table 6.3 for the same 9-month period. The values given are interdecile ranges; that is, the range between the lower decile (exceeded 90 percent of the time) and the upper decile (exceeded 10 percent of the time). These values indicate that the paths with higher path losses are those with greater variability. It has been found that, for non-auroral paths, the decile separation is about 13 dB.

Table 6.3. Dispersion of daily values (2200-2400 150° WMT; April-December, 1958) Inter-decile ranges (dB)

| Transmitter | Receiver | |
|------------------|-----------|----------|
| | Anchorage | College |
| Maui Bismarck | 13 26 | 19 30 |

6.5.4. Remedial Measures

The WWV monitoring results suggest that one remedy is a relatively large selection of operating frequencies. Owing to the overcrowding of the spectrum and the methods of allocating frequencies, this method is not particularly practical except in special cases (e.g., WWV).

The use of oblique ionosondes to determine the optimum frequency is another possibility. This may be particularly valuable in certain phases of ionospheric storms because of the enhancement of E_s , which may extend to sufficiently high frequencies at which ionospheric absorption is low enough to yield a usable signal. This method also requires a free choice of frequencies.

Given a free choice of frequencies, it is possible to put a signal of usable strength into the polar regions over 90 percent of the time—if the period of trial is long enough. The quality of the signal, however, is unknown on a percentage-of-time basis. For voice circuits the rapid "flutter" fading is probably the worst of the difficulties to be overcome. Although suggestions have been made for combating its effects [27], no serious attempt has yet been made to carry them out.

One remedy which has been used, to some extent, is the relaying of messages around the disturbed area. This is feasible where the blackouts are most frequent along the auroral ring and are usually (though not always) limited in time to a few hours, and in extent to a few hundreds of kilometers. Furthermore, owing to their local time dependence, it is possible to forecast their occurrence to some extent, and hence take remedial action. Such action is, however, of only limited value in polar cap absorption events which cover very large areas and the occurrence of which cannot be predicted. Even in PCAs there have been reports of radio contact in high latitudes. These signals may have been propagated by paths which avoid the absorbing region either because of tilts (sec. 4.6.6) or side scatter (sec. 4.6.5). An alternative possibility is that the ionization

is created very low down in the D region; under these conditions the absorption would not increase on the lower frequencies (see (2.101)) as much as it would if the absorption occurred at higher altitudes.

Other alternatives are the use of very low frequencies, very high frequencies (forward scatter, meteor scatter, etc.), and tropospheric scatter.

6.6. RADIO PROPAGATION FORECASTING

Forecasting of the probable occurrence of an ionospheric storm can be very useful from several points of view. For example, a communications operator is warned to transmit his essential messages before his circuit is blacked out; alternatively he may start up various relay links,

or change his operating frequency.

The two radio forecasting centers of the Central Radio Propagation Laboratory regularly issue three types of forecasts of radio propagation conditions. These forecasts apply to skywave propagation (usually within the frequency range 2 to 30 Mc/s) over certain particularly important radio paths. The North Atlantic Radio Warning Service is concerned primarily with transmission over paths such as New York–London or Washington–Paris; their forecasts will apply to a lesser extent on nearby paths like Boston–North Africa, Maine–Greenland, etc. The North Pacific Radio Warning Service forecasts are designed for paths like Anchorage–Seattle, San Francisco–Fairbanks, or Tokyo–Anchorage; they can be given special interpretation, however, for others, such as short intra-Alaska circuits, but again with less reliability.

Average quality is forecast for a specified 6-, 12-, or 24-hr period. All times are Universal Time (UT or GCT). The CRPL radio quality scale

is used in all instances:

1—Useless 6—Fair-to-good 2—Very poor 7—Good 3—Poor 8—Very good 4—Poor-to-fair 9—Excellent. 5—Fair

The average quality in the 2 hr preceding the issue time is expressed in the following letter code:

W—disturbed (1 to 4) U—unsettled (5) N—normal (6 to 9). The forecasts must be interpreted in the light of the user's own experience. A forecast of "3" means that the conditions experienced should be relatively poor, but the operator must interpret this in terms of the expected performance of his circuit. If the forecast is correct, no more than 5 or 10 percent of all days should be so poor. There may be, however, a systematic difference between the word-descriptions used by the operator and by the forecaster, and the operator must take this into account in interpreting the forecast. For instance, he may be used to calling conditions "very poor" when the forecaster calls them "poor," or the operator of another, perhaps easier, circuit may never see conditions as worse than "fair." The forecasts are expressed on a scale which corresponds to the average experience reported on a typical circuit.

The estimate of present conditions (the letter) is made available to aid the user in interpreting the forecast (the number). For example, if an "N-5" is issued, and the operator is already at the time of the forecast experiencing what he would call unsettled (quality 5) conditions, then he would expect conditions to become even worse. The statement N-5 indicates that the forecaster looks for a deterioration of at least one grade during the forecast period. The value of this scheme rests on the fact that the operator is concerned with expected changes in conditions and so is given information to tie in with his current experience. If the "5" had been issued without the "N," the user would not have been prepared for a drop in quality since he was already experiencing what he called quality "5" conditions, although the concensus available to the forecaster rated conditions "normal."

A third forecast, the 24-hr forecast, is also available daily by telephone and teletype from the two forecasting centers. Separate quality estimates are issued for nighttime and daytime of the ensuing 24-hr period. The range of frequencies on which the predicted quality should be realized is also included.

Additional information concerning the radio forecasting services may be obtained from:

For the North Atlantic area:

North Atlantic Radio Warning Service (or NARWS)
National Bureau of Standards, Box 178, Fort Belvoir, Va.
(Telephone—Washington, D.C., 780-1436 or 780-1444)

For the North Pacific and Alaskan area:

North Pacific Radio Warning Service (or NPRWS) National Bureau of Standards, Box 1119, Anchorage, Alaska (Telephone—753-2211 or 753-7210) Past CRPL forecasts together with the actual conditions which developed are included in the CRPL F series, B, Solar Geophysical Data.

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CHAPTER 7

Ionospheric Propagation Predictions

7.1. AIM OF THE CHAPTER

The aim of this chapter is to give the reader a brief idea of the way in which ionospheric data are applied to the problems of high-frequency communications via the ionosphere. The problems concerned with the prediction of optimum working frequencies (see sec. 4.7.3) and system loss are more adequately dealt with in another publication [1]¹ of the Central Radio Propagation Laboratory, and the reader of this chapter is urged to consult that work. Data on the world wide distribution of noise levels, which are required for the determination of required transmitter power, are given in CCIR Report 322 [2]. These two documents will be extensively referenced in this chapter.

An outline will be given of the procedures used at CRPL in preparing predictions, and the application of the data to practical problems will be illustrated by some simple numerical examples.

7.2. PURPOSES OF PREDICTIONS

Because the ionosphere varies from hour to hour and from day to day, etc., it is necessary to have a knowledge of this variability in order to select the optimum frequency, required transmitter power, antenna configuration, and so on. Broadly speaking there are two types of predictions required.

(1) Relatively short-term frequency predictions are required by the circuit operator in order that he may be able to anticipate MUF failure and thus increase the circuit reliability.

(2) The long-term predictions are required for the planning of terminal installations. This involves both the circuit planner and the

¹ Figures in brackets indicate the literature references on p. 341.

frequency allocator. The sort of questions they are faced with are: What will be the range of usable frequencies over the next sunspot cycle? What is the minimum power necessary to fulfill the requirements of the circuit? What elevation angles must be used in antenna design?

It might be noted here that yet another type of prediction, if it may be called a prediction, is the short-term information obtainable from oblique ionosondes (sec. 4.4.) or backscatter observations. This type is of importance primarily to traffic control centers and those concerned with circuit operation.

For the first type of prediction, the most accurate method is to predict median values of the required parameters month by month. Such monthly predictions are issued usually about 3 months in advance and include observed ionospheric data up to 1 year before the prediction is made. The solar cycle information required is usually based on even more recent data. Predictions of type (2) are needed over a complete sunspot cycle and normally include data over the solar cycle prior to that in which the prediction is made. The behavior of the E and F_1 layers of the ionosphere is so regular that permanent nomograms can be used for determining the required characteristics. On the other hand, the F_2 layer is very irregular, and since it is the most important from the point of view of high-frequency communications, maps have been prepared giving the variation of f_0F_2 and the M factor (sec. 4.3.2), etc., as a function of time of day, season, and sunspot number.

The purpose of the present chapter is to show how a prediction system can be used to give information about a specific circuit. The essential phenomena concerning the ionosphere and the underlying theory have already been discussed and will be considered only briefly below.

7.3. PREDICTABLE CHARACTERISTICS²

7.3.1. Sunspot Number

The long-term variation of ionospheric parameters is tied closely to the sunspot cycle, and although no completely satisfactory measure of solar activity is available, the 12-month running average sunspot number is most widely used (see sec. 3.3.5.4). Normally, the most practical way for circuit operations and planners to determine the sunspot number is to use the predictions of others [3]. When predictions of future cycles are required, an average minimum of 10 and an average maximum of 130

² Most of the figures in this section are from a lecture by G. W. Haydon.

are recommended as a rule of thumb. New indices, based upon other parameters (e.g., ionospheric and solar noise), are being investigated [4, 5].

7.3.2. Maximum Frequencies

The predictions of f_0F_2 are based on the diurnal, seasonal, and geographical variations and/or sunspot number dependence established from previous data (see sec. 3.3.5.4). No attempt is made, in these long-term predictions, to estimate the day-to-day fluctuations in critical frequency since these are rather localized in both space and time. Furthermore, no account is taken of ionospheric disturbances, such as those discussed in chapter 6, as these constitute a relatively small percentage of the total time.

The *basic* ionospheric data used in predictions are the E, F_1 , and F_2 layer ordinary-wave critical frequencies and the M(3000) F_2 (sec. 4.3.2)—that is, the M factor for a distance of 3000 km.

The behavior of the E and F_1 layers is such that the critical frequencies can be predicted, fairly accurately, in terms of solar zenith angle χ and sunspot number \bar{R} by means of (3.31) and (3.32) respectively. Furthermore, the higher critical frequency and the lower M factor for the F_1 layer are such that the product gives roughly the same maximum frequency as do the corresponding values for the E layer. The E layer is usually the controlling layer for distances up to about 2000 km and the F_1 layer for distances between 2000 km and 3000 km. Thus, from a knowledge of χ and \bar{R} , nomograms can be constructed to give f_0E . The use of these nomograms will be discussed below.

The behavior of the F_2 layer is more complicated than that of the E and F_1 layers and cannot be represented analytically. In the preparation of F_2 predictions, the first step is to obtain the line of best fit of the monthly median values of f_0F_2 to the 12-month running average sunspot number. This is done for each hour (or each alternate hour) of the day and for all stations. The slopes and intercepts of these lines are then used to construct worldwide maps from which, with a knowledge of \bar{R} , it is possible to calculate f_0F_2 . Sometimes, the value of f_0F_2 at some specific \bar{R} (=50, for example) is given instead of the intercept or together with it to give the slope. The predictions of the $M(3000)\,F_2$ are prepared in a similar manner. In those prediction methods (which are published monthly) the sunspot, seasonal, and diurnal variations are automatically taken into account [3]. Given the F_2 zero distance maximum frequency, MUF, (ZERO) $F_2(=f_xF_2)$ and the 4000 km maximum frequency, it is

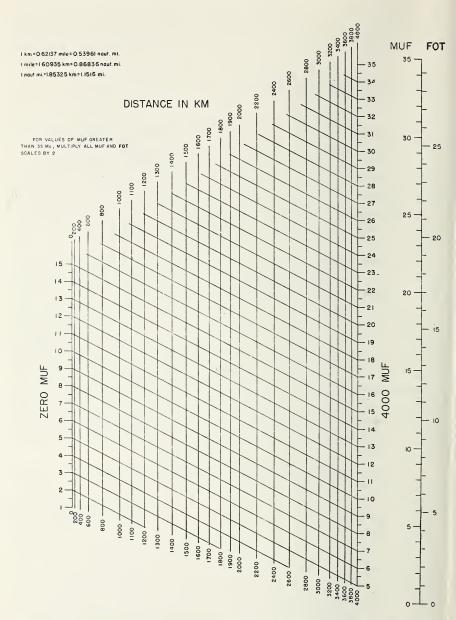


Figure 7.1. Nomogram for transforming $F_2(ZERO)MUF$ and $F_2(4000)MUF$ to equivalent maximum usable frequencies for intermediate transmission distances.

Also conversion scale for obtaining optimum working frequency (FOT). The nomogram can be used to find the skip distance for a given frequency from the MUF(ZERO) F_2 and MUF(4000) F_2 .

possible to interpolate for intermediate distances by means of figure 7.1. Note that the $M(4000) F_2$ is obtained by multiplying $M(3000) F_2$ by 1.1.

7.3.3. Radiation Angle

This depends on the height of reflection (assumed specular) of the waves. In the case of the E layer, it is sufficiently accurate to take the angles of elevation given in figure 4.31. This figure can also be used to give rough values in the case of F_2 layer propagation but, in general, it is more accurate, if the height of reflection is known, to determine the elevation angle from figure 7.2. The monthly median heights of the F_2 layer are given on a worldwide basis in reference [1].

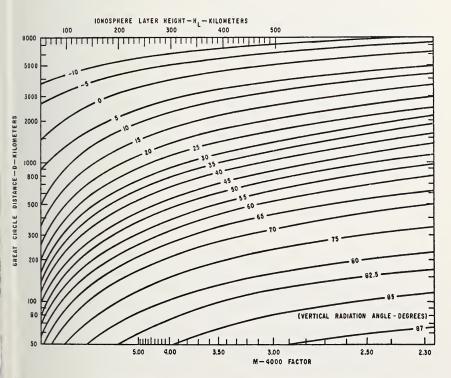


Figure 7.2. Radiation angle as a function of great circle distance and ionospheric layer height.

7.3.4. System Loss

7.3.4.1. The Elements of System Loss

The concepts of system loss and path loss have already been discussed in sections 5.2 and 5.3, respectively. In this section we shall consider the various losses that occur between the transmitting and the receiving terminals.

We shall need to consider the following path losses:

- (1) Ground loss which occurs on reflection in multi-hop propagation, L_g ;
- (2) Distance loss due to spatial spreading of the wave, L_{sp} ;
- (3) Ionospheric absorption, L_a ;
- (4) Fading and polarization factors;
- (5) Antenna gain, G.

7.3.4.2. Ground Loss

This depends on the conductivity of the ground and on the angle of elevation of the incident radiation. The losses for a good conducting surface (e.g., sea water) are less than for a poorly conducting surface such as bare rock or desert. For two types of surface the value of L_q (in decibels) can be obtained, with a knowledge of the wave frequency and the radiation angle Δ , from figures 7.3a and 7.3b.

7.3.4.3. Distance Loss

In general, it is too complicated to take into account the detailed effects of focusing, etc., so that the effective distance s_e (see (5.8)) is essentially the geometrical distance of the path which depends upon the ground range and height of reflection. For long distance transmission, involving single or multiple hops, the effective distance is, essentially, linearly related to the ground range. This is incorporated into the nomogram of figure 7.4 in which the distance attenuation has been combined with the frequency characteristics of an isotropic radiator for which the plane wave capture area in free space is given by $c^2/4\pi f^2$, where c is the free space velocity of height.

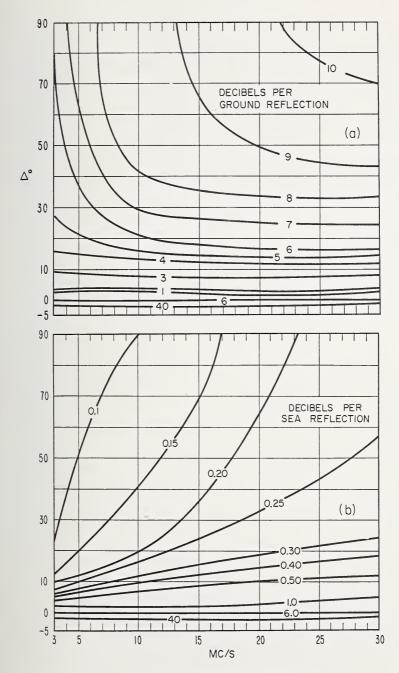


FIGURE 7.3. Power loss at reflection.

(a) Poor earth, ϵ =4, σ =10⁻² mho/m. (b) Sea water, ϵ =80, σ =5 mho/m.

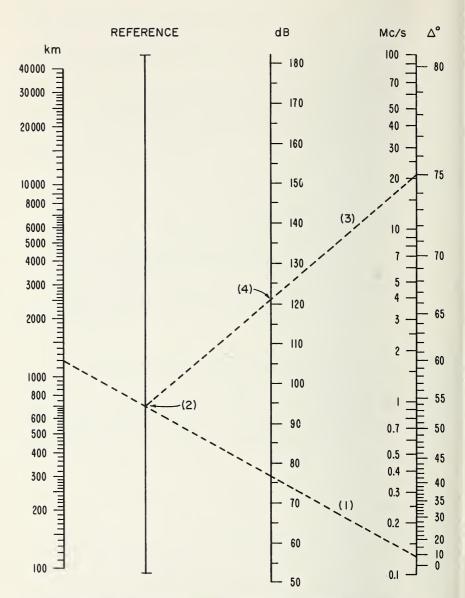


FIGURE 7.4. Nomogram for the determination of transmission loss due to distance attenuation with an isotropic radiator.

Example: (1) For a great circle distance of 1200 km and $\Delta=8^{\circ}$, draw a straight line which gives reference point (2). With reference point (2) and the wave frequency (in Mc/s) draw line (3). The intersection of line (3) with the dB axis gives the spatial loss (4).

7.3.4.4. Ionospheric Absorption

The ionospheric absorption, L_a , depends on several parameters, namely: sunspot number, solar zenith angle, season, operating frequency,

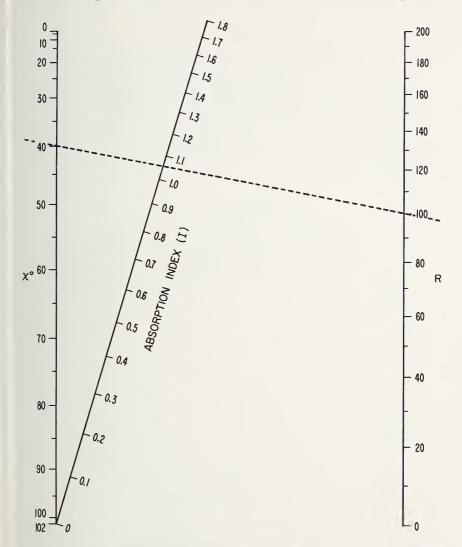


Figure 7.5. Nomogram for the determination of absorption index I from the solar zenith angle (χ) and the mean sunspot number R.

Example: With $\chi=40^{\circ}$ and R=100, draw a straight line. The intersection of this line with the absorption index lines gives I=1.06.

gyrofrequency, and radiation angle. The dependence on solar zenith angle χ and sunspot number R can be expressed, to a sufficient degree of accuracy, in terms of an absorption index I by the formula (see sec. 3.3.6.2 and sec. 3.3.6.3)

$$I = (1 + 0.0037R) (\cos 0.881\chi)^{1.3}. \tag{7.1}$$

This equation is incorporated into the nomogram shown in figure 7.5, whence I can be obtained for given values of χ and R.

The seasonal dependence on $\cos \chi$ has to be corrected for the winter anomaly (sec. 5.2.5.5). The corrected I (I_c , say) is obtained by multiplying the value obtained from figure 7.5 by the factors in table 5.1.

The next step is to incorporate the frequency dependence (sec. 3.3.6.2) and the path length in the medium. These are incorporated in figure 7.6 in which the corrected absorption index, I_c , should be used where

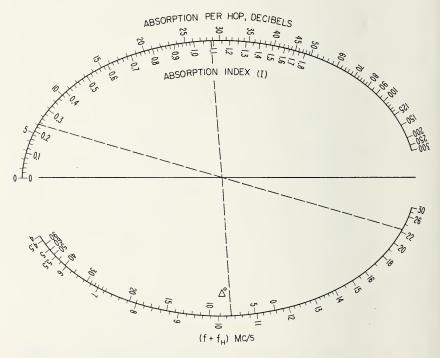


Figure 7.6. Nomogram for obtaining the ionospheric absorption per hop from the absorption index I, the effective wave frequency $f+f_H$, and the angle of elevation Δ .

Example: (1) Enter with the absorption index I (1=1.09) and the elevation angle Δ (=8°). (2) Mark the reference point of intersection with the center line. (3) With reference point and effective frequency $f+f_H$ (=22.4) draw a straight line as far as the curve marked absorption per hop (=6 dB).

appropriate. The gyrofrequency, f_H , can be obtained for any geographical location from figure 7.7. Note that the use of f_H instead of f_L introduces some error into the calculated absorption of the ordinary wave, but this is relatively small except for strictly east-west propagation when it is probably better to drop the magnetic term altogether. The nomogram

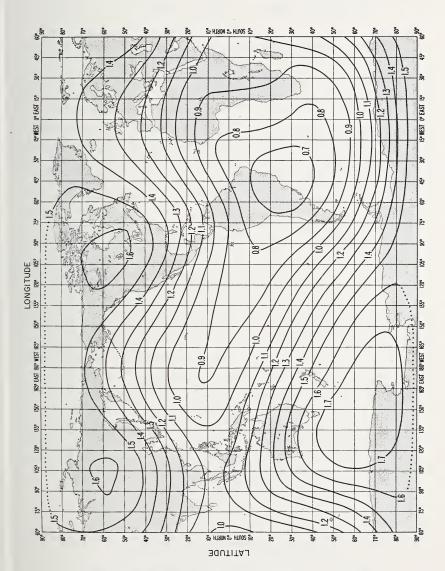


FIGURE 7.7. World map of gyrofrequency for a height of 100 km.

should be used as follows: With the corrected absorption index and radiation angle draw a line interesecting the center line. The intersection gives a reference point. With the reference point and the effective frequency $(f+f_H)$ extrapolation gives the absorption per hop (in decibels).

7.3.4.5. Allowance for Fading, Polarization, Etc.

The above considerations of transmission loss are all based on median values; that is, they refer to nonfluctuating signals. Owing to short-term variations in electron content along the ray path, the signal will, in general, fade so that for a certain fraction of the time the signal level will drop well below the median value. In order to ensure that the signal exceeds a minimum level for a certain percentage of the total time, an allowance must be added to the path loss. By this means, the matching polarization terms L_{tp} and L_{rp} (see (5.5)) are automatically taken into account. Tables giving the necessary allowances for various types of service are given by the CCIR [6].

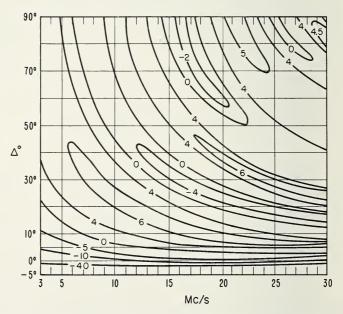


FIGURE 7.8. Space-wave radiation of a half-wave horizontal antenna 20 m above poor earth, ϵ =4, σ =10⁻³ mho/m.

Numbers on curves are decibels above an isotropic radiator in free space.

7.3.4.6. Antenna Gain

In order to determine the system loss, it is essential to know the gains of the transmitting and receiving antennas at the appropriate radiation angles. Of course, this information can only be obtained from the geometry of the antennas. An example of the type of information required, for the case of a half-wave horizontal antenna, is shown in figure 7.8.

7.4. FREQUENCY PREDICTION SYSTEMS

7.4.1. Monthly Predictions³

A variety of ionospheric predictions is issued monthly by laboratories in a number of different countries, usually three months or so in advance. Many of them are for localized areas, but several attempt worldwide predictions [3, 7]. While all prediction services use essentially the same ionospheric data and established physical relationships, there is considerable variation in the form of presentation and in the approximations used in applying the various predictions to propagation problems. The CRPL prediction system, based on a method of numerical mapping of ionospheric characteristics developed by Gallet and Jones [8, 9, 10], using electronic computers, will be described briefly.

The term "numerical map" is used to denote a function, $\Gamma(\lambda, \theta, t)$, of the three variables: latitude (λ) , longitude (θ) , and time (t). The function $\Gamma(\lambda, \theta, t)$ is obtained by fitting certain polynomial series of functions of the three variables to the basic ionospheric data. The general form of $\Gamma(\lambda, \theta, t)$ is the Fourier time series

$$\Gamma(\lambda, \theta, t) \pm a_0(\lambda, \theta) + \sum_{i=1}^{H} \left[a_j(\lambda, \theta) \cos jt + b_j(\lambda, \theta) \sin jt \right],$$
 (7.2)

where H denotes the number of harmonics retained to represent the diurnal variation. The Fourier coefficients, $a_j(\lambda, \theta)$ and $b_j(\lambda, \theta)$, which vary with the geographic coordinates, are represented by series of the form

$$\sum_{k=0}^{k} D_{sk} G_k(\lambda, \theta) \tag{7.3}$$

where the $G_k(\lambda, \theta)$ are given in table 7.1. The index s denotes which Fourier

² This section was written by Mr. S. M. Ostrow.

| Mair | n latítudinal | Mixed latitudinal and longitudinal variation | | | |
|-------------|------------------------|--|---|--|---|
| variation | | First order in longitude | | Second order in longitude | |
| k | $G_k(\lambda, \theta)$ | k | $G_k(\lambda, \theta)$ | k | $G_k(\lambda, \theta)$ |
| 0 1 2 | 1 sin λ sin²λ | $k_0+1 \\ k_0+2 \\ k_0+3 \\ k_0+4$ | $ \begin{array}{c} \cos\lambda \cos\theta \\ \cos\lambda \sin\theta \\ \sin\lambda \cos\lambda \cos\theta \\ \sin\lambda \cos\lambda \sin\theta \end{array} $ | $k_1 + 1 \\ k_1 + 2 \\ k_1 + 3 \\ k_1 + 4$ | $\cos^2 \lambda \cos 2\theta$ $\cos^2 \lambda \sin 2\theta$ $\sin \lambda \cos^2 \lambda \cos 2\theta$ $\sin \lambda \cos^2 \lambda \sin 2\theta$ |
| k_0 | sin ^q ₀λ | | $\sin^{q_1}\lambda \cos\lambda \cos\theta$ $\sin^{q_1}\lambda \cos\lambda \sin\theta$ | K-1 K | $\sin^{q_2}\lambda \cos^2 \lambda \cos 2\theta$ $\sin^{q_2}\lambda \cos^2 \lambda \sin 2\theta$ |

Table 7.1. Geographic functions $G_k(\lambda, \theta)$

coefficient is represented, in the order given by

$$s = 2j$$
, for $a_j(\lambda, \theta)$, $j = 0, 1, \dots, H$, (a)
 $s = 2j - 1$, for $b_j(\lambda, \theta)$, $j = 1, 2, \dots, H$. (b)

A numerical map, $\Gamma(\lambda, \theta, t)$, is completely defined by a relatively small table of coefficients, D_{sk} .

An important advantage of the numerical mapping method is that, as new data become available, the coefficients can be easily revised by the use of an electronic computer. Also, as additional physical relationships are established, they can be incorporated readily into the mapping program. The value of the parameter mapped can be derived for any location, and graphical maps may be prepared by computations using the table of coefficients.

The numerical map is particularly useful when large numbers of propagation path computations are required. The use of a computer permits rapid and economical inclusion of all required propagation variables in routine computation. Tables of predicted coefficients may be obtained in the form of tested sets of punched cards from the Prediction Services Section, CRPL. Users who do not have access to a computer, or whose requirements are not large enough to justify their own computer facility, may arrange to have ionospheric propagation calculations performed at a reasonable cost by the Frequency Utilization Section, CRPL.

For those who do not have access to a computer, or require a manual solution to an ionospheric propagation problem for some other reason, the CRPL also issues a monthly publication, Ionospheric Predictions [3]. This bulletin contains the basic tables of predicted coefficients of f_0F_2

and $M(3000) F_2$ three months in advance, in addition to world maps of predicted MUF(ZERO) F_2 and MUF(4000) F_2 for every even hour of Universal Time. The predicted maps are calculated from the tables of predicted coefficients using the approximations:

$$MUF(ZERO) F_2 = f_0 F_2 + f_H / 2 = f_x F_2, \tag{7.5}$$

$$MUF(4000) F_2 = f_0 F_2 \times M(3000) F_2 \times 1.1.$$
 (7.6)

Instructions for the use of these maps may be found in the National Bureau of Standards Handbook 90 [11]. Tables 7.2 and 7.3 give examples of tables of predicted coefficients D_{sk} defining the function $\Gamma(\lambda, \theta, t)$ for monthly median f_0F_2 and $M(3000)\,F_2$ for June 1963. Figures 7.9a and 7.9b show examples of world maps of MUF(ZERO) F_2 and MUF(4000) F_2 for the hour 1800 Universal Time, predicted for June 1963. These maps were derived from the predicted coefficients of tables 7.2 and 7.3.

7.4.2. Permanent Predictions

In contrast to the monthly prediction systems, permanent predictions systems describe the variation of the ionosphere over a complete solar cycle. They are particularly useful for long-term frequency planning and communications equipment specification. Such systems have been issued by the CRPL, the United States [12]; the Radio Research Station, England [13]; The Defence Research Telecommunications Laboratory, Canada [14]; and the Radio Research Laboratories of Japan [15]. These are usually issued in the form of a set of maps for solar cycle minimum and maximum conditions, but may also be in the form of a set of maps for a specific level of solar activity accompanied by a set of maps showing the world variation of the dependence on solar activity. Permanent predictions in the form of numerical maps for solar cycle minimum and maximum are available from CRPL and are part of the current CRPL prediction system.

By applying a suitable index of solar activity to a permanent prediction system, ionospheric characteristics may be obtained for any level of solar activity. They may be used as monthly predictions by using a predicted monthly index. The Zürich sunspot number has been the most commonly used index of solar activity. An index based on past ionospheric data, such as $I(F_2)$ of the Radio Research Station, is also sometimes used.

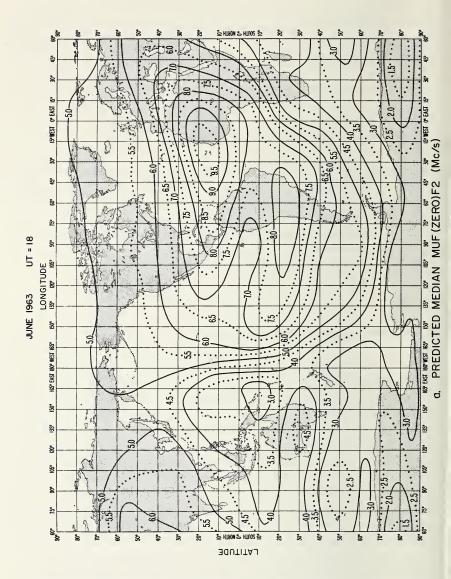


Figure 7.9a. Predicted median F_2 layer parameters for 0800 UT for June 1963, $MUF(ZERO)F_2$.

(From CRPL Ionospheric Predictions.)

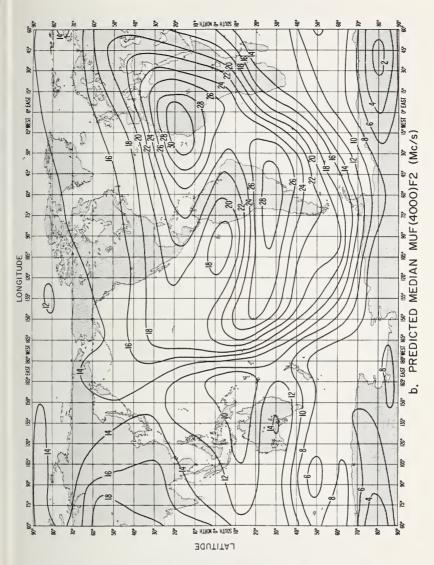


Figure 7.9b. Predicted median F_2 layer parameters for 1800 UT for June 1963, $MUF(4000)F_2$.

(From CRPL Ionospheric Predictions.)

TABLE 7.2 TIME VARIATION

| 4 | | 26E-02 66E-01 92E 00 49E-01 03E 01 03E 01 05E 01 73E 01 74E 00 06E 01 | 926-02 906-02 906-02 196-01 |
|----------|---------|--|--|
| | 80 | -4.0957426E-02 5.227966E-01 1.11629E-00 1.131629E-00 1.131629E-00 1.131629E-00 1.339679E-00 2.339679E-00 2.20759E-00 2.20759E-00 2.6074676-00 9.6074676-00 | 1,7616.39.76.6.02 1,262.20.20.6.02 1,262.20.6.02 |
| | 7 | 2.8943823E-01 -0.0138651E-02 -0.0138651E-02 -0.021710E 00 -0.453110E 00 -0.453110E 00 -0.453110E 00 -0.453110E 00 -0.4531833E 01 -0.4531833E 01 -0.4688746E 01 -0.4688746E 01 -0.4688746E 01 | 5.8020305-02 7.700036-02 5.3872916-01 5.3872916-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.874696-01 6.87469-01 6.8746 |
| | | 2 .8943523F - 6 .0138051E - 6 .023716E - 7 .0523716E - 7 .0523716F - 7 .0523 | 5 . 90 2 0 90 3 6 - 2 . 90 2 0 90 3 6 - 2 . 90 2 90 90 6 - 5 . 90 2 90 90 8 - 5 . 90 2 90 8 - 5 . 90 8 90 2 8 - 6 . 90 8 90 2 8 - 7 . 90 8 90 2 |
| | 9 | 4.8877851F-01 1.0004823-01 1.3006418-00 1.3006418-00 1.3006418-00 1.3004418-00 1.3004418-00 1.3004048-01 1.3004048-01 1.3004048-01 1.3004048-01 1.3004048-01 1.3004048-01 1.3004048-01 1.3004048-01 1.3004048-01 1.3004048-01 | 1.600.2623E-0.2 3.6166.294E-0.2 3.6166.294E-0.2 3.6166.294E-0.2 3.616.294E-0.2 3. |
| ю | | 7-4-17-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7 | |
| | ın | 4.115565E-01 3.403999-02 1.611630E-00 1.611630E-00 1.611630E-00 1.302600E-01 2.866350T-01 2.8 | 1.317846.2E-02 5.107696.E-02 7.25052701E-012 5.0052701E-012 5.0052701E-012 6.0050201E-012 6.0050201E-012 6.0050201E-02 |
| | | | |
| | 4 | 1,234,580,5E-01 1,404,234,8E-00 5,403,817,5E-00 3,995,654,E-01 1,638,656,E-01 1,638,656,E-01 1,638,656,E-01 1,638,656,E-01 1,638,656,E-01 1,638,656,E-01 1,638,656,E-01 1,638,656,E-01 2,469,716,2E-00 2,469,716,2E-00 2,340,826,E-00 3,340,827,E-00 9,340,827,7E-01 | 1.277388 b E - C - C - C - C - C - C - C - C - C - |
| 2 | | | 1 1111 1111 1111 |
| | ю | 3,1579392E-01 3,176294BE-01 1,6424BE-01 1,6424BE-00 1,157790E-01 2,5685290E-01 2,5685290E-01 2,5069BE-02 2,2063BE-02 2,2063BE-02 2,2063BE-02 2,2063BE-02 2,56480E-02 1,566790E-02 | 5.0505434E-03 11.6070899E-01 2.9311790E-00 11.41764T-E-00 2.931140E-00 11.431764T-E-00 2.93140E-00 2.93140E-00 2.93140E-00 2.93140E-00 2.9393939E-01 2.9393939E-03 2.939396E-03 2.939396E-03 2.939396E-03 2.939396E-03 2.939396E-03 2.939396E-03 2.939396E-03 2.939396E-03 2.93958312E-00 2.9358312E-00 2.9358313E-00 2.9358313E-00 2.9358313E-00 2.9358313E-00 |
| - | | | |
| | 2 | 1,845,843,55 2,1949,43,50 2,1949,43,50 2,1949,49,50 2,1949,49,50 1,457,548,60 1, | 1,9775085 COL |
| - | | | |
| | - | 1.4603118E 00 3.302588E-01 4.6401598E 01 6.6401598E 01 1.2116415E 02 2.6651694E 02 2.6651694E 02 2.6651694E 02 2.6651694E 02 3.6651694E 02 3.6651694E 02 1.1539116E 02 1.1539116E 02 1.46978002E 02 | 3,7130833E 02 1,873888E 02 1,1509397E 02 1,15093 |
| | | 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | 1.00 |
| | | 6.0616632E 0 6.888481E 0 1.701294E 0 1.701295E 0 1.7074297E 0 1.704297E 0 1.704297E 0 1.704297E 0 2.357931E 0 2.357931E 0 8.2213793E 0 6.6363263E 0 | 1.43259176 1.43259176 1.43259176 1.43259176 1.43259176 1.43259176 1.43259176 1.43259176 1.43259176 1.4325918 1.43225 |
| | | 6.0618632E 6.8888481E 1.73134684E 1.7012039 4.0080876E 1.6746462E 2.440462E 2.440462E 2.4507621E 2.4507621E 2.4507621E 2.4507622E 2.450762E 2.450762E 2.450762E 2.450762E | -3.11113.46- -3.2559176- -4.15618.2559176- -5.15618.2559176- -5.15618.2559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7558.3559176- -6.7568.3559176- |
| Harmonic | % /× | 0 1 2 8 4 8 7 9 7 1 1 1 1 2 8 8 7 9 8 7 9 8 7 8 8 8 7 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 | 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 |
| £ | | H | П |

GEOGRAPHICAL VARIATION

TABLE 7.2. CONTINUED

| | -1.1388443E-01 | -1.8216440E-01 | 4 - 889454BE-01 | -5.4257892E-01 | 2.1043183E 00 | 5 * 4360603E-01 | -1.7723341E 00 | 2.2463466E 00 | -6.0461426E 00 | -2.5987278E-01 | 1.3832242E 00 | -2.0336876E 00 | 4.5043299E 00 | |
|-----|----------------|----------------|-----------------|----------------|----------------|-----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| | -2.2310859E-02 | -7.3152581E-04 | -6.7762142E-02 | -1.914144E-03 | 1.5382243E-01 | ~2.1096271E-02 | 8.0105853E-02 | 1.1798088E-02 | -1.6829177E-01 | | | | | |
| | -1.8593028E-02 | 3.5013250E-02 | 1.1353041E-02 | 7.2831482E-02 | 2.2094268E-01 | 1.7885350E-01 | 1.3367833E-01 | -1.4545954E-01 | -8.5617251E-01 | -1.5392106E-01 | -2.1109224E-01 | 6.2926208E-02 | 7.9760529E-01 | |
| 1 | -1.6233762E-02 | 3.0602094E-04 | 9.0444803E-03 | 1.6831259E-02 | 1.4394707E-01 | -1.8689688E-02 | -7.6970087E-03 | 2.9966173E-03 | -2.0120531E-01 | | | | | |
| | 10-3116///211 | 5.3268600E-01 | ~2.0632316E 00 | -1.1436232E-01 | -1.5175129E 00 | -1.9275214E 00 | 7.3258049E 00 | 6.6426865E-01 | 2.1299899E 00 | 1.7774499E 00 | -6.5445791E 00 | -9.5221753E-01 | | |
| | 1.8254183E-02 | 3.1498853E-01 | 2.5105565E-01 | -9.2413288E-01 | -7.3792610E-01 | -1.3718429E 00 | -8.6683769E-01 | 1.9260939E 00 | 1.0363975E 00 | 2.2254380E 00 | 5.0302925E-01 | -4.0478348E-01 | -8.3808459E-01 | -1.4950064E 00 |
| | 1.1528//3E-01 | -1.4733867E-01 | 2.0313565E 00 | 8.6734731E-01 | -4.2161978E-01 | 1.3474982E 00 | -8.8650360E 00 | -6.7690841E-01 | -2.6571760E-01 | -1.2792030E 00 | 8.0317355E 00 | | | |
| | 1.9965690E-01 | -4.0945373E-01 | 3.0933786E-01 | 2.0250975E-01 | -8.4940921E-01 | 2.2253875E 00 | -6.1580197E-01 | -9.8925537E-01 | -1.4805479E 00 | -4.9787298E 00 | 5.7236017E-01 | 8.5847125E-01 | 9.8485116E-01 | 3.0332794E 00 |
| | -2.224355UE-01 | -4.1157782E-01 | -6.0129504E-01 | -5.4718356E-01 | 2.4431573E 00 | 3.7672088E 00 | 2.0633151E 00 | 1.0412184E 00 | -5.4059122E 00 | -9.2573766E 00 | -1.7357938E 00 | -3.8134213E-01 | 3.3317464E 00 | 6.2966958E 00 |
| 0.0 | 39 | 04 | 41 | 42 | 43 | 77 | 45 | 94 | 14 | 48 | 64 | 20 | 51 | 52 |
| f | - | | Ī | | Ī | | E | | | _ | | | Ī | |

| | 91 | -5.9442100E-03 6.6448063E-02 -2.1168590E-03 -6.9653336E-02 |
|----------|---------|--|
| 60 | 15 | 7.9136678E-02 -5.9442100E-03 2.93762E-02 6.64448053E-02 -3.947695E-01 -2.1168590E-03 3.4033103E-01 -6.965338E-02 3.4033103E-01 |
| 7 | 14 | **8662231E-02 1:4059348E-01 -1.163976xE-01 2:1836845E-02 -2.3778916E-02 -7.9171870E-02 -7.91780E-02 -7.91780E-02 -7.91780E-01 -7.90840E-01 -7.90840E-01 -7.90840E-01 -7.90840E-01 -7.90840E-01 -7.90840E-02 -7.90840E-02 -7.90840E-02 -7.90840E-02 -7.90840E-01 -7.90840E-02 -7.90840E |
| | | -2,3775916E-02 7,904,1764E-02 7,1871463E-02 -9,2053959E-02 -5,1274070E-02 |
| | 12 | 2.1836845E-02 -1.0365909E-01 4.8571369E-02 1.0664306E-01 -7.9006805E-02 |
| 9 | Ξ | -1.0450172E-01 -1.0450172E-01 5.1600007E-01 1.1369507E-01 -4.1776517E-01 |
| | 10 | 9.%66231E-02 1.4059348E-01 1.4.405943E-01 -2.10060813E-02 3.0291571E-01 -3.4494815E-01 1.5709466E-01 3.0373425E-02 2.2238367E-01 2.4354806E-01 |
| | 6 | 9.9662231E-02 -1.4969493E-01 -3.0921571E-01 1.5709866E-01 2.2238367E-01 |
| onic | s/ × | 4 9 2 1 0 |
| Harmonic | | н |
| | NO | TAIRAV |

GEOGRAPHICAL

Notation: For each entry the number given by the first eight digits and sign is multiplied by the power of ten defined by the last two digits and sign. I - Main latitudinal variation. Mixed latitudinal and longitudinal variation: II - First order in longitude, III - Second arder in longitude.

PREDICTED COEFFICIENTS DSK DEFINING THE FUNCTION $\Gamma(\lambda,\theta,t)$ FOR MONTHLY MEDIAN f_o F2 (MC/S) JUNE 1963

TABLE 7.3 TIME VARIATION

| 23 | - | 2.6272681E-03 1.2.6240838E-01 1.2.6240838E-01 1.2.6240838E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62688E-01 1.2.62189E-01 1.2.62189E-01 1.2.62189E-01 1.2.62189E-01 1.2.6463789E-01 1.2.6463789E-01 | | | | |
|----------|---------|---|--|--|--|--|
| | 5 | 6.2078843E-03 6.2078843E-02 -2.307403DE-01 -2.307403DE-01 3.4670172E-01 -1.40173E-01 -1.40172E-03 -1.4052100E-01 6.7625800E-03 -2.505028E-03 -2.505028E-03 -2.505028E-03 -2.505028E-03 -2.70649E-01 -2.70649E-01 -2.70649E-01 -3.707899E-01 -3.707899E-01 -4.45268E-01 -5.4157878E-01 -5.4157878E-01 -5.4157878E-01 -5.4157878E-01 -5.4157878E-01 -5.4157878E-01 -5.4157878E-01 -5.4157878E-01 -5.4157878E-01 -5.4157878E-01 | | | | |
| | 4 | 2.5740258E-01 1.436732E-02 1.436405E-02 1.2364405E-00 1.055473E-00 1.055479E-00 1.055479E-00 9.6300536E-01 6.8461235E-01 6.8461235E-01 1.276926E-01 1.276926E-01 1.276926E-01 1.27663E-01 | | | | |
| 2 | ю | -2.1199636E-02 1.1232397E-01 -6.163394E-02 -1.048953E-01 2.0027040E-02 -2.2495297E-02 -4.225093E-01 -4.225093E-01 -4.225093E-01 -4.225093E-02 -4.225093E-02 -4.225093E-02 -1.048990E-02 -2.349736E-03 -4.369890E-01 -3.51978830E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 -3.51978809E-01 | | | | |
| | 2 | 2.46622776-01 1.246596E-01 1.2465747E 00 -2.64971996E 00 -2.64971996E 00 1.6652026E 00 1.6652026E 00 -2.59971996E-01 -2.97159136-02 -2.97159136-02 -3.0716996E-01 -3.0716996E-01 -3.0716996E-01 -3.0716996E-01 -3.0716996E-01 -3.0716996E-01 -3.0716996E-01 -3.0716996E-01 -3.0716996E-01 -3.0716968E 00 -3.0716968E 00 - | | | | |
| | - | -8.8046694E-02 -7.6290212E-02 3.665342EE-01 -2.0459337E-01 -2.1771823E-02 1.0088166E-01 3.4345697E-02 2.1791890E-02 2.1797083E-02 -1.7957083E-02 -1.7957083E-02 -1.7957080E-02 -1.7957080E-01 -2.077680E-02 -1.7957080E-01 -2.077680E-01 -2.077680E-01 -2.077680E-02 -1.7957080E-01 -2.077680E-01 -2.077680E-01 -2.077680E-02 -1.79570E-01 -2.077680E-02 -1.5586E-02 -1.6676528 00 -2.6725012E 00 -2.6725012 | | | | |
| 0 | 0 | 2.9846047E 00 1.851271E 00 8.4137349E-01 1.852310E-01 5.6360138E 00 3.829232E-01 2.4321780E-02 2.4321780E-02 2.4321780E-02 2.4321780E-02 2.4321780E-02 2.4321780E-01 1.25448176-02 4.425431E-02 4.425431E-02 4.425431E-02 1.2768956E-01 1.2468926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.2469926E-01 1.24699496E-01 1.246996E-01 1.2 | | | | |
| Harmonic | s/ × | 0 1 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | | | | |
| Harn | | н | | | | |

TABLE 7.3, CONTINUED

| 60 | 50 | 03 | 04 | 03 | 03 | 0.3 | _ | - | _ |
|-------------------------------|----------------|------------------------------|----------------|----------------|------------------------------|----------------|----------------|----------------|----|
| -7.92473895- | 1.8606725E-04 | -4.2794055E- | 4.3180137E-04 | 1.6117318E-03 | 2.46937735-03 | 7.2261267E-03 | | | |
| -5.5957838E-03 -7.9247389E-03 | -2.4613063E-03 | 3.9470262E-02 -4.2794055E-03 | | 1.8910241E-02 | 1.8073043E-03 | -1.0169957E-01 | -6.7063709E-04 | -1.3745593E-02 | |
| | 1.5027262E-02 | | 2.6412399E-02 | | | | | | |
| -6.5126359E-03 | -6.5084171E-03 | -9.6650246E-03 | 2.0909759E-02 | -5.7752228E-02 | -5.0660560E-03 | -1.5078302E-02 | | | |
| -7.3129424E-03 2.8285532E-02 | 4.7417305E-03 | 6.6375435E-04 | -6.8907294E-02 | 2.9154513E-03 | 9.5583291E-02 -1.0230071E-02 | | | | |
| -7.3129424E-03 | -1.8759120E-03 | -1.1350380E-01 | 2.4667502E-02 | -3.7223690E-04 | 9.5583291E-02 | 2.6012231E-01 | | | |
| . 1.4449766E-02 | -6.0268623E-03 | -1.4362969E-03 | 2.0993976E-03 | -1.3104181E-01 | | | | | |
| 27 | 28 | 59 | 30 | 31 | 32 | 33 | 34 | 35 | 36 |
| | | | | E | 1 | | | | |

| _ | | - | |
|--|----------|----------|--|
| | 9 | 12 | 2.8147691c-03 6.5125544E-03 2.8678856E-03 -1.7787042E-02 6.3869251E-03 -5.9672219E-03 1.2369828E-03 1.8982024c-04 |
| The second secon | | = | -2.8147691E-03 -2.867885E-03 6.3869251E-03 1.2369628E-03 |
| | 2 | 10 | 8.4443347E-03 1.1299466E-02 -3.5465446E-02 -i.2499808E-02 -3.6797341E-03 -1.7900707E-02 3.5480584E-02 1.4455502E-02 |
| | | 6 | 8.4443347E-03 -3.5465446E-02 -3.6797341E-03 3.5480584E-02 |
| | | 8 | 7.0531886E-03 2.2202710E-02 -1.8260167E-02 -1.5475290E-02 |
| | 4 | 7 | 1.9780783E-02 1.845239E-02 -3.2098590E-02 -1.725620IE-02 |
| | Harmonic | ω/ \× | 0106 |
| | Harr | | <u> </u> |

GEOGRAPHICAL
VARIATION

Notation: For each entry the number given by the first eight digits and sign is multiplied by the power of ten defined by the last two digits and sign. 1 - Main Tatitudinal variation. Mixed latitudinal and Tongitudinal variation: II - First order in longitude, III - Second order in Tongitude.

PREDICTED COEFFICIENTS D_{SK} DEFINING THE FUNCTION $\Gamma(\lambda,\theta,t)$ FOR MONTHLY MEDIAN M(3000)F2 JUNE 1963

7.5. RADIO NOISE PREDICTIONS

7.5.1. Importance of Noise

In every communications system (radio or otherwise) noise is the limiting factor which determines whether or not the signal is usable for the transmission of information. In principle, if all noise could be eliminated from a system then only an infinitesimal transmitted power would be required and the amplification in the receiver could be unlimited. In the presence of noise, there is a limit to the amount of useful amplification because both signal and noise are amplified to the same extent. Thus, in choosing a receiving site, it is very important to have a knowledge of the ambient noise with which the desired signal must compete so that sufficient power may be transmitted in order to override the noise.

Radio noise arises from a number of noise sources such as resistors, radio tubes, etc. (thermal noise), galactic noise (thermal) from outer space, atmospheric noise from lightning discharges (thermal and/or impulsive in nature), and from electrical machinery (impulsive or spikey) [16].

Noise internal to the receiving system is usually the dominant noise in systems operating on frequencies above about 300 Mc/s. In the high-frequency band (3 to 30 Mc/s), atmospheric and galactic noise usually determines the noise level at sites well removed from civilization. It is with these types of noise that we shall be concerned in this chapter.

Measurements of atmospheric noise levels have been made for many years by the Radio Noise Section of the Central Radio Propagation Laboratory and the reader is referred to their publications [17, 18, 19] for details on the method of noise measurement and the applications to the design of communications systems. These details need not concern us here; it will suffice to know that experience has shown that the noise power is generally the most significant single parameter in relating the interference effect of the noise to system performance.

The noise power is measured in terms of quantity, F_a , which is defined as the external noise power available from a lossless antenna, expressed in decibels above kT_0 , where k is Boltzmann's constant and T_0 = 288.39 °K is a reference temperature, which is the noise generated in a unit bandwidth by a thermal source at a temperature T_0 . On the assumption that noise power is proportional to the bandwidth b (in cycles per second) we have that the total power (P_n in decibels above one watt) available at the terminals of a lossless antenna is given by

$$P_n = F_a + B - 204 \text{ dB/W}$$
 (7.7)

where $B = 10 \log b$ and $10 \log k T_0 = -204$. Notice that this is based on the assumption that the noise is incident on the antenna uniformly in all directions.

7.5.2. Presentation of Noise Data

7.5.2.1. Long-Term Characteristics

The noise power at any point on the earth's surface depends on the following:

- (1) Geographic location;
- (2) Time of day;
- (3) Season of year;
- (4) Operating radio frequency;
- (5) Bandwidth of the receiving system.

Hourly noise data have been collected at a number of locations on a routine basis over several years. Any long-term variation appears, at present, to be small. The diurnal and seasonal variations of the noise parameters are represented by dividing the year into the following four seasons:

| | Seasons | | | | |
|--|--------------------------------------|--------------------------------------|--|--|--|
| Months | Northern hemisphere | Southern hemisphere | | | |
| December, January, February March, April, May June, July, August September, October, November | Winter Spring Summer Autumn | Summer Autumn Winter Spring | | | |

The noise levels are presented as median values F_{am} of F_a for each of the following 4-hr periods of local time at the receiver: 00–04, 04–08, 08–12, 12–16, 16–20, and 20–24. The statistical distribution of the individual values F_a about the median F_{am} is given by the upper decile ratio D_u (= $F_{au} - F_{am}$) where F_{au} is the value of F_a exceeded 10 percent of the time. When plotted on a normal probability graph (level in decibels), the amplitude distribution of the deviations, D, above the median can be repre-

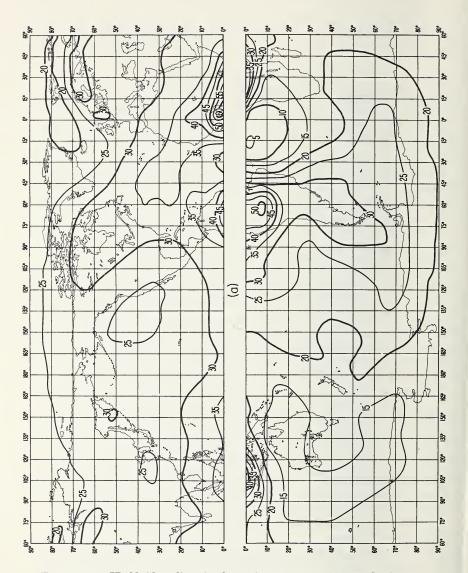
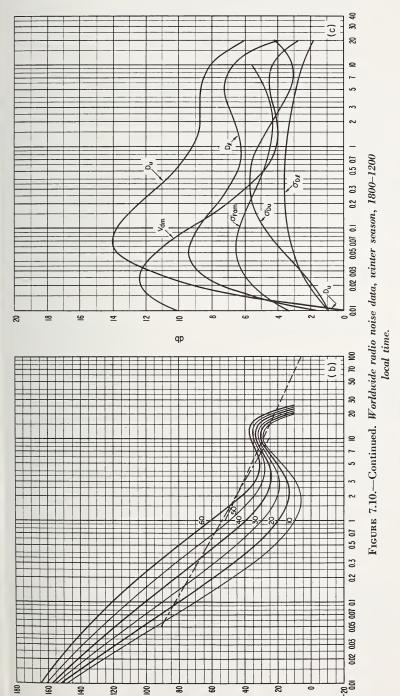


Figure 7.10. Worldwide radio noise data, winter season, 0800-1200 local time.

(a) Expected values of F_{am} , in decibels above kT_0B , on 1 Mc/s.



(b) Variation of radio noise with frequency. (c) Data on noise variability; $\sigma_{F_{am}}$ =standard deviation of F_{am} ; σ_D =standard deviation of values of D_u ; D_u =ratio of upper decile to median of F_{am} .

sented with reasonable accuracy by a straight line through the median and upper decile value. A corresponding line through the median and lower decile value D_l can be used to represent the deviations below the median. The lower decile is of little practical importance and will not be considered here.

The values of F_{am} presented in the maps are deduced from values taken at several geographical locations and on a number of frequencies. From the frequency dependence of F_{am} a reference value on an effective frequency of 1 Mc/s is obtained and this is plotted on the sample noise map in figure 7.10a. Of course, the data presented are smoothed values and the measurements on a specific frequency at a particular location will, in general, differ from the value deduced from the curves. A measure of the error introduced by the smoothing procedure is, therefore, given by the standard deviation of these differences $\sigma_{F_{am}}$. In a similar way, the standard deviations of D_u , σ_{Du} , are measures of the difference to be expected between the values of D_u obtained from the curves and the actual measured values. The variations with frequency of the above noise parameters are given in figures 7.10b and 7.10c. A complete set of these maps can be found in the CCIR Report 322.

7.5.2.2. Short-Term Characteristics

The parameters discussed above represent the fluctuations in the long-term character of the noise, that is, from one time block to the next and from season to season. To evaluate the effect of the noise on a communications system, we need also some knowledge of the short-term character of the noise. This subject is dealt with fully in the publications of W. Q. Crichlow and his coworkers [17, 18, 19] and the interested reader should consult those references. For many purposes, and particularly those involving subjective factors, the simplest procedure is to take the short-term effects into account by using the CCIR tables of signal/noise ratio [6].

7.5.2.3. Application of Noise Data

To understand how the information presented in figure 7.10 is applied to an actual problem, let us consider the following example.

Détermine the noise level at Washington, D.C., on a frequency of 13 Mc/s in a 6 kc/s channel at 1400 UT in December 1963.

From an atlas or some other source we determine the geographic coordinates of Washington, D.C.—39°North, 77°West and, hence, the local time is approximately 1400-0500=0900 hours. From the noise grade map of figure 7.10a we find that F_{am} on 1 Mc/s is about 32 dB. In order to determine the value of F_{am} on 13 Mc/s we locate the 32 dB point on the 1 Mc/s line in figure 7.10b and move up in frequency (keeping just above the 30 dB line). On 13 Mc/s, we have $F_{am} \approx 32$ dB. To take into account the uncertainty in the value of F_{am} due to the spread of the data we add a correction $\sigma_{F_{am}}$ obtained from figure 7.10c. On 13 Mc/s we find that $\sigma_{F_{am}} \approx 6$ dB. Hence the noise power on 13 Mc/s in an effective bandwidth of 1 c/s is 32+6=38 dB above the reference value of kT_0 .

On the assumption that noise power is proportional to bandwidth we find that the noise power in a 6 kc/s channel is $38+10 \log 6000=38+37.8=75.8$ dB above kT_0 . Substitution in (7.7) gives $P_n=-128.2$ dB above 1 W.

7.6. CALCULATION PROCEDURES FOR DISTANCES LESS THAN 4000 km

7.6.1. Introduction

The average height of the F_2 layer (320 km) corresponds to a maximum one-hop distance of about 4000 km. Hence, this distance gives a convenient dividing line between long distance and intermediate distance transmission. In this section we shall discuss, by example, the procedure to be followed for transmission distances of less than 4000 km.

7.6.2. Problem 1

- Part 1. Determine the optimum working frequency around noon in June 1963 for a transmitter in Boulder, Colo., and a receiver in Washington, D.C.
- Part 2. Find the transmitter power required to ensure the following performance of an A3 telephony double sideband system with a bandwidth of 6 kc/s. The required grade of service is marginally commercial for 90 percent of the hour and the antennas are half-wave horizontal dipoles at heights of 20 meters.

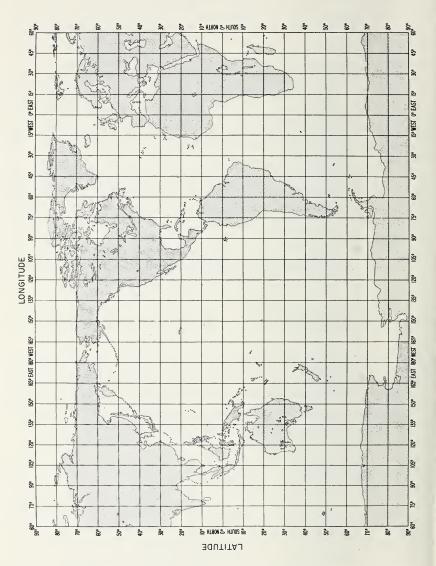


Figure 7.11. World map used for determining latitude and longitude of end points, midpoint, control points, and great circle path.

Path Length, Location of Midpoint, and Solar Angle

First we find the geographic coordinates of the end points, from a map (figure 7.11) or elsewhere:

Boulder 40°N 105°W Washington 38.9°N 77°W

To find the path length and midpoint we lay a sheet of transparent paper over the world map (fig. 7.11) and proceed as follows:

- Step 1: Draw on it the equator and the 0° and 180° meridians.
- Step 2: Locate and mark the geographic coordinates of the transmitter and receiver.
- Step 3: Transfer the transparency to the great circle chart (fig. 7.12) and, with the equators coincident, slide the transparency along the equator until the terminals lie on the same great circle (solid lines) or a proportionate distance between adjacent great circles.
- Step 4: Estimate the great circle distance from the broken lines—this gives about 2400 km.
- Step 5: Estimate the midpoint location from the broken lines—approximately 40.4°N 91°W—and mark on the transparency.
- Step 6: Transfer the transparency to figure 7.13 and read the dipole latitude at the path midpoint—about 51°.
- Step 7: Determine the appropriate universal time at the path midpoint. 1200 (90° WMT) corresponds to 1800 UT.
- Step 8: Determine the sun's zenith angle χ as follows. Place the transparency over the chart in figure 7.14. Keeping the equators coincident make the zero meridian coincide with the universal time (1800) obtained in step 7. Then read off, by interpolation if necessary, the value of χ at the midpoint of the path—about 18°. A complete set of maps of χ is given in reference 1.

7.6.3. Determination of Optimum Frequency

Step 9: From figure 7.9a and b, respectively, we obtain

 $MUF(ZERO) F_2 = 6.0 Mc/s$

 $MUF(4000) F_2 = 17.0 Mc/s.$

Step 10: From the data obtained in step 9, we find, from figure 7.1, by

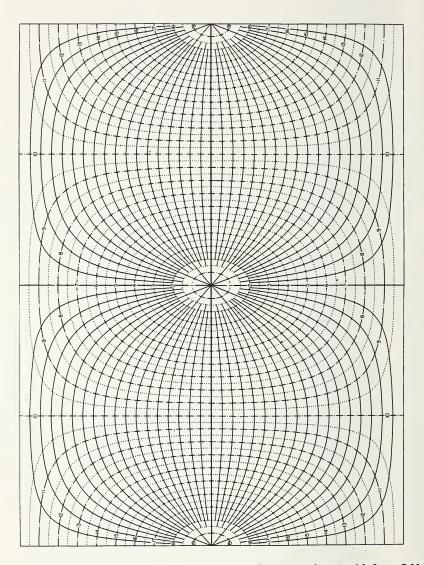


FIGURE 7.12. Great circle chart centered on the geographic equator for use with figure 7.11.

The solid lines represent great circles. The numbered dot-dash lines indicate distance in thousands of kilometers.

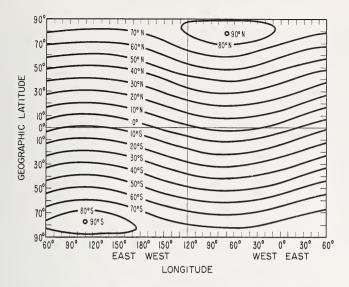


FIGURE 7.13. World map of magnetic dipole latitude.

interpolation, that the MUF and FOT for 2400 km are respectively 13.8 Mc/s and 11.7 Mc/s. The FOT is 0.85 MUF (see sec. 4.7.3.).

It is now necessary to determine the effect of the ${\cal E}$ layer. Here there are three possibilities.

- (1) The normal \vec{E} layer will determine the MUF.
- (2) The sporadic E layer will determine the MUF.
- (3) That E layer cutoff will occur (sec. 4.7.2.).
- Step 11: Determine the radiation angle for one-hop E propagation for a distance of 2400 km. From figure 4.31 we find that this is less than zero and so this possibility is eliminated.
- Step 12: The angle of elevation $\Delta(F_2)$ for one-hop F_2 propagation is found by first determining the height of the F layer from figure 7.15 as follows: Place the transparency over the appropriate chart and, keeping the equators coincident and with zero degree meridian coincident with the universal time (1800), read off the F_2 -layer height at the midpoint of the path. We find the height to be about 400 km. From figure 7.2 we obtain $\Delta(F_2) = 13^\circ$. A complete set of maps for obtaining the F_2 -layer height is given in reference [1].
- Step 13: To see whether the MUF for the two-hop E mode dominates we proceed as follows for a distance of 1200 km (half the path

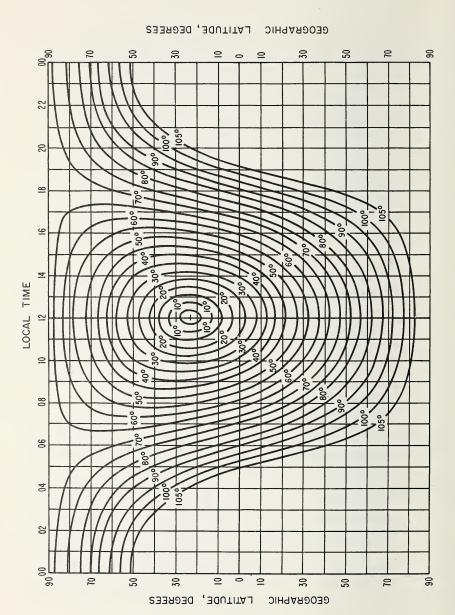


FIGURE 7.14. Solar zenith angle for June.

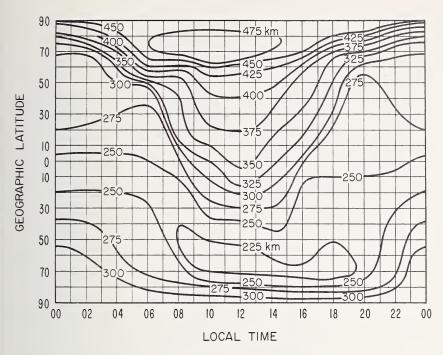


FIGURE 7.15. World map of F2 layer heights for June.

length). Knowing the zenith angle (18°) and the average sunspot number (25) we find the MUF(2000) E from figure 7.16.

$$MUF(2000) E = 17.6 Mc/s$$

Using figure 7.17 we find

$$MUF(1200) E = 14.5 Mc/s$$

which is also equal to the combined $E-F_1$ optimum working frequency because the day-to-day variation in this quantity is negligible. The reason for combining the E and F_1 layers is that the greater value of f_0F_1 (as compared with f_0E) is almost exactly balanced by the greater obliquity of the E layer path giving the same f_v sec ϕ_0 (see sec. 4.2) as for the F_1 path.

We see now that the MUF for E layer propagation exceeds that for F_2 layer propagation.

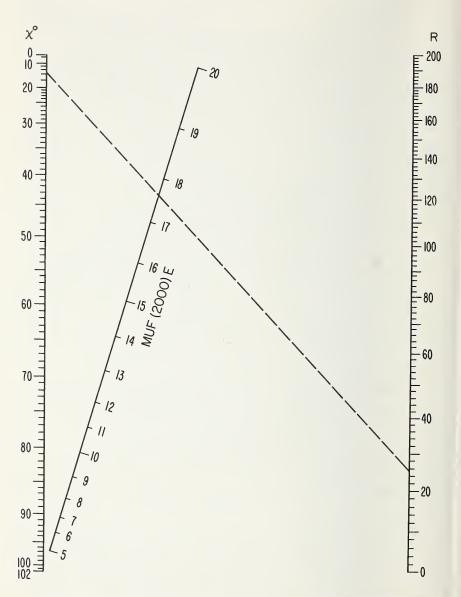


Figure 7.16. Nomogram for obtaining MUF(2000)E from the 12-month moving average sunspot number R and solar zenith angle χ .

Example: With $\chi=15^{\circ}$ and $R=25^{\circ}$, the MUF(2000)E is 17.6 Mc/s.

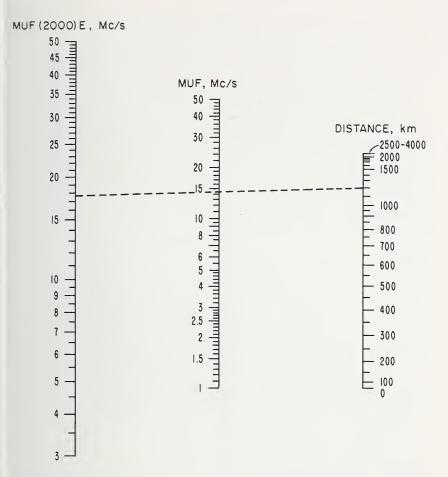


Figure 7.17. Nomogram for transforming MUF(2000)E to equivalent maximum frequencies and optimum working frequencies due to combined effect of the E layer and the F_1 layer for other distances.

Also from the MUF(2000)E it is possible to find the skip distance corresponding to a given frequency. Example: With MUF(2000)E of 17.6 Mc/s, the MUF(1200)E is 14.2 Mc/s.

Step 14: To see whether the sporadic E layer controls the maximum frequency we use figure 7.18. This gives the median fE_s contours for the month of June. A set of 12 such maps (one for each month of the year) is given in reference [1]. Note that the solar cycle variation of E_s has not been definitely established and so, for the time being, these charts may be considered as permanent. Furthermore, it will be seen that dipole latitudes

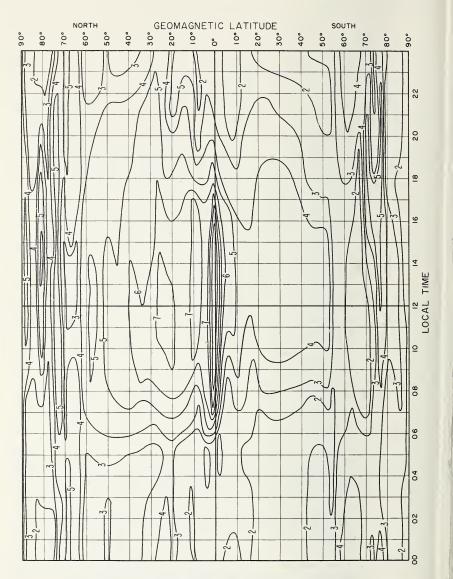


FIGURE 7.18. Worldwide distribution of fEs for June.

are used to simplify the longitudinal presentation of the data. From the dipole latitude, obtained in Step 6 (=51°N), we find the median fE_s to be 5 Mc/s. The corresponding median value of $MUF(2000)E_s$ is given by multiplying fE_s by 5, i.e.,

$$MUF(2000) E_s = 25 Mc/s.$$

Because of the variability of the fE_s an allowance must be made as a safety margin to insure communications 90 percent of the days. As a working rule, it is suggested that the optimum working frequency for 2000 km be obtained by subtracting 4 Mc/s from the MUF(2000) E_s . This gives OWF(2000) $E_s \approx$ 21 Mc/s. With the aid of figure 7.17 we obtain OWF(1200) $E_s \approx$ 17 Mc/s. Clearly, propagation via the E_s layer will determine the optimum working frequency.

Step 15: To determine the E (or E_s) layer cutoff frequency we proceed as follows: Step 12 gives $\Delta(F_2) = 13^\circ$ and, by using figure 4.31, we find that the corresponding E distance is approximately 800 km. Knowing the MUF(2000) E_s (=25 Mc/s), from figure 7.17 we find that the MUF(800) $E_s \approx 15.3$ Mc/s. Thus the OWF (17 Mc/s) will penetrate the E layer (for $\Delta = 13^\circ$). However, since this frequency is well above the MUF(2400) F_2 it will not normally be reflected from the higher (F_2) layer.

We now conclude that the dominant path for propagation is the two-hop E_s path and that the optimum working frequency is 17 Mc/s.

Path loss

Step 16: The absorption loss is determined as follows. The index I is obtained (for $\chi = 18^{\circ}$, R = 25) from figure 7.5. This gives I = 1.04.

From figure 7.7 we find that the appropriate value of f_{H} is 1.5 Mc/s. Therefore, $f+f_{H}=17+1.5=18.5$ Mc/s. The radiation angle for two-hop E_{s} (from fig. 4.31) is $\Delta(2 E_{s})=8^{\circ}$. Using figure 7.6 we obtain

absorption per hop=8.5 dB

total absorption = 17 dB.

Step 17: Distance loss. With an isotropic radiator, this is obtained from figure 7.4:

distance loss per hop=120 dB

total distance loss = 120+6=126 dB.

Step 18: Ground reflection loss. From figure 7.3b we obtain, for $\Delta=8^{\circ}$ a ground reflection loss = 3 dB.

Total path loss $L_{\text{path}} = 17 + 126 + 3 = 146 \text{ dB}$.

System Loss

Step 19: Antenna gain. From figure 7.8, with $\Delta=8^{\circ}$, the gain per antenna is 6 dB. Therefore, the antenna loss $L_a=-12$ dB. For information on other types of antennas the reader may consult reference $\lceil 20 \rceil$ and follow up the references cited therein.

Step 20: Total system loss L_s is given by

$$L_s = L_{\text{path}} + L_a$$

= 146-12=134 dB.

Step 21: Required carrier/noise ratio. From the CCIR tables [6] we find that the required value of peak RF signal/noise ratio under steady (nonfading) conditions for the specified performance is 27 dB. On the assumption of 100 percent depth of modulation this requires a median carrier/noise ratio of 21 dB. To allow for the random (Rayleigh) fading of the signal we must add 8 dB, i.e., the ratio of the value P exceeded 90 percent of the time to the median P_m . This is obtained from the formula

$$T = \exp\{-0.693P/P_m\} \tag{7.8}$$

where T is the fraction of time that the instantaneous value exceeds P.

For the upper decile value, $10 \log P/P_m \approx 8 \text{ dB}$.

The required carrier/noise is, therefore, 21+8=29 dB. Step 22: Noise power. Following the procedure outlined in sec. 7.5.2.3, we obtain from figure 7.19a

$$F_{am}$$
 on 1 Mc/s=70 dB.

Together with figure 7.19b this gives

$$F_{am}$$
 on 17 Mc/s \approx 33 dB.

This value of F_{am} , being a median, gives the noise level exceeded 50 percent of the days. In order to find the level exceeded 10 percent we require the upper decile value F_{au} . This is obtained from $D_u(=F_{au}-F_{am})$ which is given, as a function of frequency, in figure 7.19c. On 17 Mc/s, $D_u \simeq 8$ dB, therefore $F_{au} = F_{am} +$ $D_u = 33 + 8 = 41$ dB. Because of the spread in the data, from which F_{am} and D_u are derived, there are inherent inaccuracies in the median values. These inaccuracies can be partially taken into account by the standard deviations $\sigma_{F_{am}}$ and σ_{D_u} respectively which are given in figure 7.19c. From this figure we obtain $\sigma_{F_{am}} \approx 4$ dB; $\sigma_{D_u} \approx 3$ dB. The total uncertainty σ_T is deduced on the basis that the errors are uncorrelated, i.e., $\sigma_T^2 = \sigma_{Fma}^2 +$ σ_{Du}^2 , hence $\sigma_T = 5$ dB. The effective upper decile is, therefore, $F_{\rm eff} = F_{au} + \sigma_{\tau} = 46$ dB. When circuit operation is required for some percentage of the time other than 90 percent, F_{au} and F_{am} can be plotted on probability paper and the appropriate value of F_a obtained by linear interpolation (or extrapolation). A more complete account of this procedure is to be found in CCIR Report 322 [2]. Furthermore, further corrections need to be made to obtain the true total uncertainty σ_T but these are negligible and will not be considered here. The interested reader should consult CCIR Report 322 for a more detailed treatment.

The effective noise level for a 6 kc/s channel is given by substitution in (7.7).

$$P_n = F_{\text{eff}} + B - 204 = 46 + 37.8 - 204$$

= -120.2 dB above 1 W.

Step 23: Required carrier power Pr at receiver. From step 21 we have

Required carrier/noise =
$$P_r - P_n = 29 \text{ dB}$$

$$P_r = 29 + P_n = 29 - 120.2 = -91.2$$
 dB above 1 W.

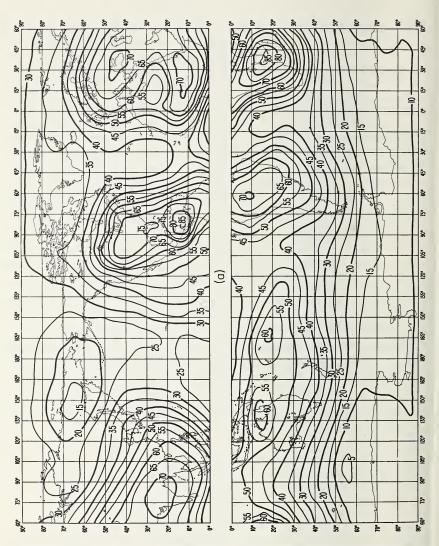
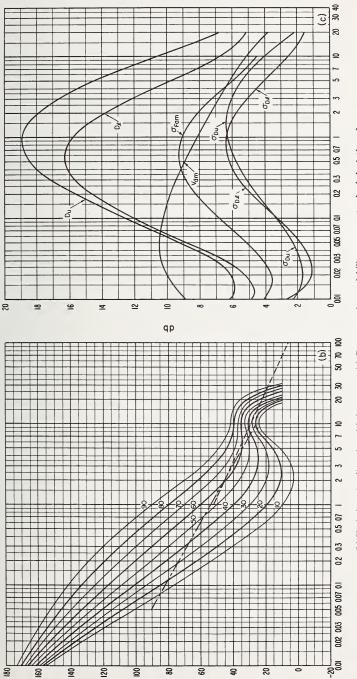


FIGURE 7.19. Worldwide radio noise data, summer season, 1200-1600 local time.

(a) Expected values of F_{am} , in decibels above kT_0b , on 1 Mc/s.



(b) Variation of radio noise with frequency. (c) Data on noise variability; $\sigma_{F_{\alpha m}}$ =standard deviation of $F_{\alpha m}$; σ_{D_u} =standard deviation of values of D_u ; D_u =ratio of upper decile to median of $F_{\alpha m}$.

Step 24: Required transmitter power P_t .

$$P_t = P_r + L_s$$
.

From step 19, $L_s = 134 \text{ dB}$; and step 23, $P_r = -91.2 \text{ dB}$.

 $P_t = 42.8 \text{ dB above } 1 \text{ W}$

 $\approx 19,000 \text{ W} = 19 \text{ kW}.$

7.7. CALCULATION PROCEDURES FOR DISTANCES GREATER THAN 4000 km

7.7.1. Control Points

As the distance of propagation is increased beyond the one-hop F_2 limit (around 4000 km) it has been found (empirically) that the propagation is not suddenly cut off. Some physical reasons for this, discussed in section 4.6, are ionospheric and ground scatter, the high-angle ray, and ionospheric tilts. Empirically, it has been found that propagation did not appear to fail until the ionosphere failed to support the propagation at two "control points" on the great circle path at 2000 km from each end. This was apparently true, within limits, over wide ranges of path lengths, geographical locations, and time.

In the practical solution of determining the MUF for F_2 -layer propagation, the control points 2000 km from each end are chosen. The MUF for the path is the lower of the two MUFs, for a distance of 4000 km, for each control point as the midpoint of the 4000-km path.

When it is desired to apply the procedure to the E, E_s , and F_1 layers, an additional pair of control points 1000 km from each end may be used. However, there is less justification for this course than is the case with F_2 propagation.

7.7.2. Statement of Problem 2

Determine the transmitter power requirements of the following circuit:

| Transmitter location | London | 51.5°N | 0°W |
|----------------------|------------|--------|------|
| Receiver location | Washington | 38.9°N | 77°W |

Month—December 1963 Time—1400 UT

Sunspot number 17 (CRPL Predictions)

Frequency 13 Mc/s

Antennas—half-wave horizontal antennas 20 meters high, A3 telephony—good commercial quality, 90 percent of time

Bandwidth 6 kc/s

7.7.3. Control Points and Midpoint

Mark a sheet of transparent paper, as in problem 1, and determine the coordinates of the midpoint and the two control points (2000 km from either end). Following the procedures outlined in problem 1 we obtain the following information:

| Geographic Geomagnetic |
|------------------------|
| °N 30°W 62°N 30°W |
| °N 57°W 60°N 57°W |
| °N 42°W |
| 4 Mc/s |
| 00 km |
| 1 |

7.7.4. Frequency Calculations

We follow the course outlined in problem 1, bearing in mind that the use of the control point method implies that the maximum frequency is that appropriate to a distance of 4000 km, i.e., zero angle of radiation. We obtain the following data.

| Step | Parameter | Source | A | Midpoint | В |
|------------|---|----------------------------------|------|----------|------|
| (1) | Local time | | 1200 | 1112 | 1012 |
| (1) (2) | Solar angle χ | Step (1) and figure 7.21 | 78° | 75° | 77° |
| (3) | $	ext{MUF}(ext{ZERO})F_2 \ 	ext{(Mc/s)}$ | CRPL Predictions (fig. 7.20a) | 6.5 | _ | 6.2 |
| (4) | $MUF(4000)F_2$ | CRPL Predictions | 22.5 | | 21.5 |
| (5) (6) | (Mc/s) F_2 layer height (km) | (fig. 7.20b) Figure 7.22 | 225 | 220 | 220 |
| (6) | Average F_2 height (km) | Average of step (5) | | 222 | |
| (7) | Absorption index I | Figure 7.5 | 0.28 | 0.333 | 0.30 |
| (8) | Average I | Average of step (7) | | 0.30 | |
| (9) | Corrected I | Step (8) and table | | 0.46 | |
| (10) | OWF(Mc/s) | 0.85×21.5 | | 18.3 | |

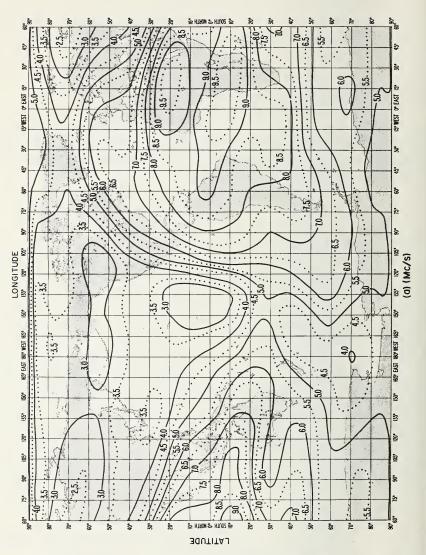


Figure 7.20a. Predicted median F_2 layer parameters for December 1963, UT=1400, $MUF(ZERO)F_2$

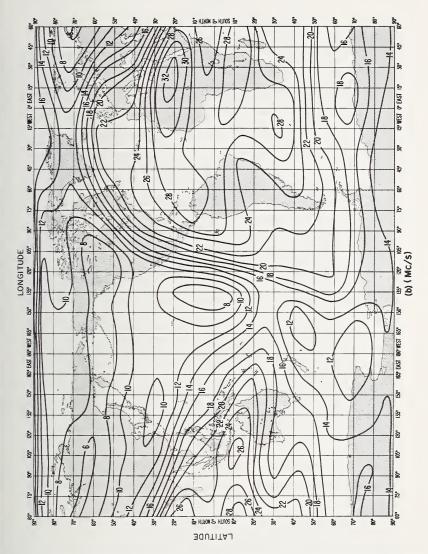


Figure 7.20b. Predicted median F_2 layer parameters for December 1963, UT=1400, $MUF(4000)F_2$.

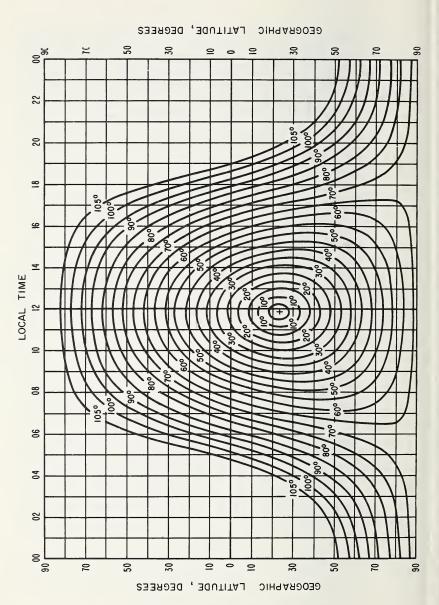


FIGURE 7.21. Solar zenith angle for December.

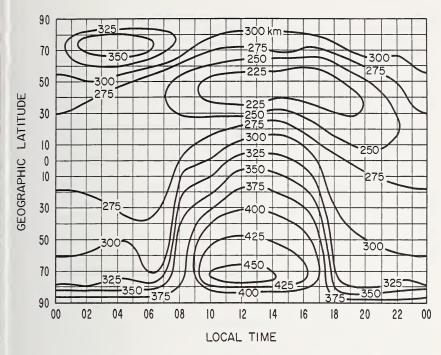


FIGURE 7.22. World map of F2 layer heights for December.

Hence (since 18.3>13), propagation on 13 Mc/s will be possible for more than 90 percent of the time.

7.7.5. Path Structure

The next step is to determine the dominant propagation paths (see sec. 4.7.1). For this we must depend on the stable paths so that although the Pedersen path (sec. 4.4.3.2), or scatter (sec. 4.6.4), may sometimes predominate, these paths cannot be relied upon for stable propagation. First we find the ground ranges corresponding to a single leg of the multihop path, e.g., 2F, 3F, 3E, etc. We then find the maximum elevation angle for reflection from the E layer and the minimum F layer Δ that can penetrate the E layer. In this way forbidden paths can easily be

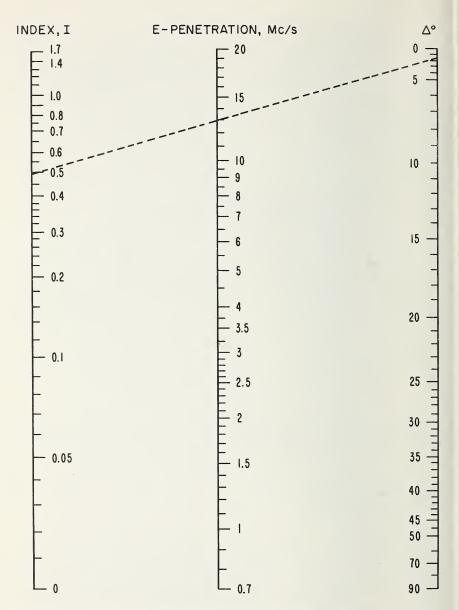


Figure 7.23. Nomogram for the determination of the E layer penetration frequency for any elevation angle Δ .

eliminated as follows:

| | | | | | Paths | | |
|------|----------------------------------|---|------|------------|-------|------|------------|
| Step | Parameter | Source | 3E | 4 <i>E</i> | 2F | 3F | 4 <i>F</i> |
| (11) | Distance per hop | Total distance number of hops | 1967 | 1475 | 2950 | 1967 | 1475 |
| (12) | Radiation angle Δ° | Steps (6) and (11) and figs. 7.2 (F) and 4.31 (E) | 1.5° | 4° | 2° | 8° | 13° |
| (13) | Maximum Δ (E layer) | Minimum of step (7) A or B and figure figure 7.23 | <0° | | | | |
| (14) | Minimum Δ (F layer) | Maximum of step (7) A or B and figure 7.23 | | | <0° | <0° | <0° |
| (15) | Minimum F distance (km) | Minimum A or B of step (3) and step (4) and figure 7.1 (for $f = 13$ Mc/s) | | | 1600 | 1600 | 1600 |

A consideration of these paths shows:

- (a) 3E and 4E are impossible because Δ exceeds the maximum $\Delta(E)$,
- (b) 2F and 3F are possible,
- (c) 4F is impossible because the hop distance (1475 km) is less than the minimum (1600 km).

7.7.6. System Loss

7.7.6.1. Path Loss

| | | | Paths | |
|--------------|--|---|-------|-----|
| Step | Parameter | Source | 2F | 3F |
| (16) (17) | Effective frequency Loss per hop (dB) | $f+f_H=13+1.4=14.4$ Steps (9), (12), (16) and figure 7.6 | 8 | 6 |
| (18) | Total absorption loss | Step (17) times number of hops | 16 | 18 |
| (19) | Ground loss per reflec- tion (dB) | Step (12) and figure 7.3a | 1 | 0.5 |
| (20) | Total ground loss (dB) | Step (19) times number of re- flections | 1 | 1.0 |
| (21) | Distance loss | Frequency, distance, Δ, and figure 7.4 | 130 | 130 |
| (22) | Path loss L_{path} | Step (18) + step (20) + step (21) | 147 | 149 |

7.7.6.2. Antenna Loss

We shall assume that the appropriate antennas are perfectly matched to the transmitter and receiver. From figure 7.8 we obtain the following antenna gains relative to an isotropic radiator.

| | | | Paths | | |
|----------------------|---|--|----------------|--------------|--|
| Step | Parameter | Source | 2F | 3F | |
| (23) (24) (25) | Transmitter antenna gain Receiver antenna gain Total antenna loss $L_{	exttt{antenna}}$ | Figure 7.8 and step (12) Figure 7.8 and step (12) | -5 -5 10 | 4 4 -8 | |

7.7.6.3. Total System Loss

$$L_s = L_{
m path} + L_{
m antenna}$$
 $L_s(2F) = 147 + 10 = 157$ $L_s(3F) = 149 - 8 = 141$

Since the loss on the 2F path is very much larger than that on the 3F path, the latter is the dominant path and it alone needs to be considered further.

7.7.7. Noise Power

From section 7.5.2.3 we see that, on 13 Mc/s, $F_{am} = 32 \text{ dB}$ and $\sigma_{F_{am}} = 6 \text{ dB}$. To find the effective upper decile value we proceed as follows:

| Step | Parameter | Source | 3F Value |
|--------------------------------------|---|--|--|
| (26) (27) (28) (29) (30) | D_u σ_{Du} Upper decile F_{au} Total uncertainty Effective noise level above kT_0b | Figure 7.19c Figure 7.19c $F_{au} = F_{am} + D_u = 32 + 9$ $\sigma_T = \{\sigma_{Fam}^2 + \sigma_{Du}^2\}^{\frac{1}{2}}$ $F_{au} + \sigma_T$ | 9 dB 3 dB 41 dB 6.7 dB 47.7 dB |
| (31) (32) | Correction for 6 kc/s bandwidth Correction for kT_0 | Add 10 log 6000 = +37.8 (see (7.7) -204 | 85.5 dB -118.5 dB/W |

7.7.8. Required Carrier Power at the Receiver

| Step | Parameter | Source | 3F Value |
|------|--|-----------------------|----------|
| (33) | Peak RF signal/ | Reference [6] | 35 dB |
| (34) | Carrier/noise (based on 100% modulation) | Step (33) — 6 dB | 29 dB |
| (35) | Allowance for Ray- leigh fading | Equation (7.8) | 8 dB |
| (36) | Required carrier/ | Step (34) + step (35) | 37 dB |
| (37) | Required carrier power P_r | Step (32) + step (36) | -81.5 dB |

7.7.9. Required Transmitter Power P.

$$P_t = P_r + L_s$$

= -81.5+141=59.5 dB/W
= 890 kW.

This rather high value of required power will normally be reduced by the use of more highly directive antennas.

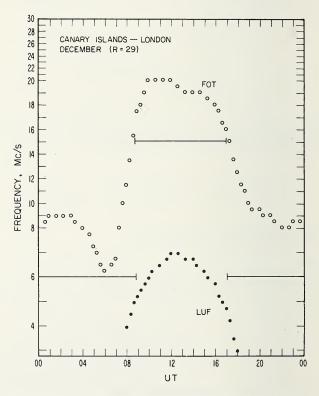
7.8. CHOICE OF OPERATING FREQUENCY

7.8.1. Optimum Working Frequency

The optimum working frequency (0.85 MUF) can be calculated for each hour of the day by the methods described above. In principle, it would be desirable to change the frequency slowly throughout the day in order to make use of the optimum conditions. However, in practice, this is both inconvenient and, in most cases, impossible because of international methods of allocating frequencies. In general, a user is allocated only two or three frequencies for use on a given circuit. A knowledge of the diurnal variation of the FOT will, however, aid the circuit operator in anticipating circuit failure due to penetration of the ionosphere by the signal.

7.8.2. The Lowest Usable Frequency

For a given transmitter output power, as the operating frequency is decreased, the available power at the receiver normally decreases due to increased ionospheric absorption, etc. Furthermore, the noise power increases so that the signal-to-noise ratio deteriorates and the circuit reliability decreases. The minimum frequency below which the reliability is unacceptable, is called the lowest useful high frequency (LUF). The LUF depends upon transmitter power, the factors that determine the path loss (frequency, season, geographical location, etc.), and the noise level (mainly frequency and receiver location). One of the main factors is ionospheric absorption and hence, since this normally varies with solar zenith angle, the LUF peaks around noon. Consequently, in



Example: With I=0.49 and $\Delta=1.5^{\circ}$ the E penetration frequency is 13 Mc/s.

FIGURE 7.24. Sample diurnal variation of the optimum working frequency (FOT) and the lowest usable high frequency (LUF) to illustrate the selection of operating frequencies.

selecting a frequency, it is necessary to ascertain whether the LUF exceeds this frequency.

7.8.3. Operating Frequency

The diurnal variations of the FOT and the LUF for a circuit between the Canary Islands and London in a December when the average sunspot number is 29 are shown in figure 7.24. It will be seen that, during the night, it is necessary to use a frequency of around 6 Mc/s in order to ensure that the operating frequency does not exceed the FOT by an appreciable amount for too long a time. The use of this frequency band during the day is impossible because it lies below the LUF. During the daytime it would be better to use a frequency around 15 Mc/s.

Of course, it should be realized that occasionally the MUF may drop to an exceptionally low value, as during a magnetic disturbance, or that increased D region absorption will raise the LUF. Under these circumstances even the FOT may be unusable.

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CHAPTER 8

Scatter Propagation on Very High Frequencies

8.1. SCATTERING FROM IONOSPHERIC IRREGULARITIES

The very high frequency (VHF) band is usually defined as the frequency range from 30 Mc/s to 300 Mc/s. Such a definition is of course purely arbitrary. From the point of view of magneto-ionic theory, the numerical values of Y(2.69) are very small and, in general, are negligible, except possibly for Faraday rotation effects (see sec. 4.9.5). Furthermore, the maximum electron densities in the ionosphere are rarely sufficient to reflect waves on frequencies much above 30 Mc/s except for relatively short periods (e.g., in the equatorial regions near the peak of the sunspot cycle). Ionospheric transmission on VHF is, therefore, mainly the result of scattering of waves by irregularities in the electron density distribution in the ionosphere rather than by gradual refraction. If sufficiently high transmitter powers are used the net scattering of energy from the individual electrons (quasi-incoherent scatter) can be detected.

The chief sources of irregularities in the ionosphere are:

- (1) Irregularities due to turbulent mixing in the D region.
- (2) Ionized trails due to the passage of meteors through the atmosphere.
 - (3) Spread F irregularities (cause unknown).
 - (4) Sporadic E.
 - (5) Individual electrons.

In this chapter we shall select a few of these topics for discussion.

8.2. CHARACTERISTICS OF PROPAGATION ON VERY HIGH FREQUENCIES

Ionospheric effects on frequencies above 100 Mc/s are small (but see sec. 4.9) and not particularly important from the point of view of

radio communications. We shall, therefore, concentrate our attention on the frequency band from 30 Mc/s to 100 Mc/s.

Ionospheric propagation in the 30 Mc/s to 100 Mc/s range is characterized by the following features:

- (a) Regular but weak scattering from the D region which is useful for continuous single-frequency communication in the 30 Mc/s to 60 Mc/s range over path lengths of the order of 1000 to 2000 km.
- (b) Intermittent reflections from ionized meteor tracks which are useful for burst communications in the 40 Mc/s to 80 Mc/s range over path lengths up to 2000 km.
- (c) Sporadic and intense reflections on frequencies which may be useful up to about 50 Mc/s to long distances (greater than 4000 km) via irregularities in the F region at times of high sunspot number.
- (d) Reflections from patches of sporadic E are sometimes important (especially as a source of interference) up to distances of 2000 km or so and on frequencies as high as 80 Mc/s.

The chief disadvantages of VHF propagation, from the point of view of radio communications, are:

- (1) Low signal strengths, because of the relative inefficiency of the scattering mechanism.
 - (2) Rapid fading.
 - (3) Limited ground range (2000 km).
 - (4) Mutual interference between channels normally independent.

8.3. D-REGION SCATTERING¹

8.3.1. Scattering From Irregularities in the D Region

Irregularities are produced by the action of turbulence, wind shears, etc., on the electron distribution in the height range between about 70 km and about 90 km. These irregularities in electron density result in corresponding fluctuations in refractive index. Since turbulence merely brings about a redistribution of the electrons, these types of irregularities will exhibit marked solar control as does the overall electron content of the D region. There is also evidence for stratification in the D region [1], which means that the refractive index changes abruptly with height.

¹ This section is based on a lecture by R. C. Kirby.

² Figures in brackets indicate the literature references on p. 390.

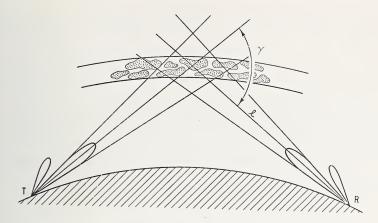


FIGURE 8.1. Geometry of forward scatter from the D region.

The effect of these rapid changes, both in time and space, on very-high-frequency waves is to scatter the energy out of the direction of the incident beam [2]. Since most of the energy is scattered in directions making small angles with that of the incident beam, the phenomenon is called "forward scatter."

The geometry of forward scatter is sketched in figure 8.1 in which a volume V of the ionosphere is illuminated by a transmitter. If p_t is the power radiated in the direction of V, then the available power p_a from a receiving antenna R is given by

$$p_a = p_t r_0^2 l^{-2} b A_r \csc(\gamma/2) S(K),$$
 (8.1)

where

 r_0 is the electron radius $(2.8 \times 10^{-15} \text{ m})$, l is the distance from V to R, b is the thickness of the scattering volume, A_r is the effective area of the receiving antenna, γ is the angle through which scattering takes place, S(K) is the spectrum of turbulent irregularities,

and

$$K = \frac{4\pi}{\lambda} \sin \frac{1}{2}\gamma, \tag{8.2}$$

where λ is the wavelength. Equation (8.1) applies when single scattering is the dominant mechanism (i.e., the amplitude of a twice-scattered wave is negligible) and for isotropic irregularities.

The scattering process acts like a narrow band filter on the spectrum, emphasizing those irregularities of size K^{-1} , where K is given by (8.2). Notice that the isotropy assumption prevents the application of this theory to magnetic field-alined irregularities. Furthermore, we have neglected the effect of the polarization of the incident wave. The latter requires the inclusion, in (8.1), or a $\sin^2 \chi$ term where χ is the angle between the incident electric vector and the scattering direction. Equations (8.1) and (8.2) emphasize the joint frequency-distance dependence of received power which is characteristic of scatter propagation, and shows that the spectrum of irregularities is the basic description of the turbulent electron density variations which is required in electromagnetic theory. In the case of turbulent mixing it can be shown $\lceil 2 \rceil$ that

$$S(K) = K^{-n}(dN/dh)^2,$$
 (8.3)

where dN/dh is the electron density gradient.

From (8.1), (8.2), and (8.3) we find that the relationship of system loss to the frequency f and geometry of the propagation path is given by

$$p_t/p_a \propto l^2 f^{n_s} \left(\sin \frac{1}{2} \gamma\right)^{n_s-1}, \tag{8.4}$$

where $n_s(n_s=n+2)$ is the frequency exponent for an antenna the gain of which is constant with respect to frequency. The use of n_s allows for the frequency dependence of A_τ because the gain of the antenna increases as the square of the frequency.

8.3.2. Height of Scattering

Experimental evidence suggests that the scattering of VHF waves is produced primarily from two layers. During the daytime the predominant heights are around 70 km; this scattering layer is subject to solar control and, therefore, is thought to be due to turbulence. During nighttime the scattering appears to come from the 85 to 90 km region, the ionization in which is thought to be produced by the influx of meteors. Some observations seem to be best explained on the basis of simultaneous scattering from both layers.

8.3.3. Signal Strengths in Middle and High Latitudes

8.3.3.1. Long-Term Variations

From hourly median values of signal strengths it has been found that, in the frequency range from 25 to 108 Mc/s, over distances of from 1000 to 2000 km, the system loss ranges from about 140 dB to about 210 dB. The loss depends on several factors such as wave frequency, type of antenna, geography, and time.

Median values of system loss [3] indicate that on a frequency of about 50 Mc/s the diurnal variations of signal strength are as follows:

Middle latitudes: A maximum near noon and a minimum near 2000 hr local time with the diurnal curve broader in summer than in winter, as would be expected from the solar illumination.

High latitudes: The diurnal maximum is broader and tends to be centered earlier in the day as compared with middle latitudes. The system loss for a given hour varies considerably from day to day. This variation is greater in high latitudes than in middle latitudes.

In middle and high latitudes the seasonal variation is characterized by a strong maximum in summer for all hours of the day. No definite long-term (solar cycle) variation has been established.

The above results were obtained over paths of about 1200 km length and with narrow-beam (6°) rhombic antennas aimed along the great circle.

8.3.3.2. Frequency Dependence

According to (8.4) the system loss should vary with frequency to the power n_s . Observations with narrow-beam (6°) antennas show that the values of n_s vary with time but that 90 percent of the observations give values in the range 7 to 9.5 with an overall median of 8. Daytime values are generally greater than nighttime by 1 or 2. Furthermore, summer values tend to be lower than those in other seasons, though winter daytime values are also lower than equinoctial daytime values. With wide beam (56°) antennas the values of n_s are about $\frac{1}{2}$ to 1 less than with the narrow beam (6°) antennas.

The diurnal and seasonal variations of n_s , and the beamwidth dependence, have been interpreted as evidence of the combined effects of turbulence and meteoric ionization. The lower values of n_s are associated

with dominant meteoric contributions to the received signal, and the higher values with turbulence.

A limited amount of data indicates that average values for frequency dependence for arctic paths are about the same as in middle latitudes, though less data are available. The measurement of frequency dependence in high latitudes is often complicated by the prevalence of high absorption on the lower frequencies.

The dependence of the intensity of the signal on scattering angle in the plane of the great circle has also been measured directly. Measurements have been carried out in summer daytime, over short paths (500 to 800 km) using pulse transmissions to separate ionospheric and tropospheric returns. Values of n from 4 to 8 (corresponding to values from 6 to 10 for n_s) have been obtained. These are not inconsistent with the values from frequency dependence measurements, but as very few observations have been made, the statistical significance of the frequency dependence measurements is much greater.

8.3.3.3. Short-Term Variations

8.3.3.3.1. Amplitude Distribution and Fading Rate

Observed amplitude distributions show that, during most of the day, the envelope is, essentially, distributed in a Rayleigh manner. The distributions are peaked somewhat at the high-signal end during the late night and early morning hours. Fading rates normally lie between 0.2 c/s and 3 c/s, the rate increasing with frequency. Most observations show that this rate depends on carrier frequency raised to a power between 0.75 and 1.25. One would expect a linear dependence (exponent = 1.0) if the drift speed of the scattering region were dominant compared to the changing structure of irregularities. This departure from linear dependence at times favors the idea of a turbulent D region as against meteor-produced ionization.

Fading rates are higher for broad-beam systems, and for off-great-circle paths, than for great-circle transmission with narrow beams.

8.3.3.3.2. Space Correlation

Correlation of signals received on antennas spaced in the great circle is much greater than for antennas spaced perpendicular to the path. Measurements on 50 Mc/s, with narrow-beam transmitting antennas, show that the correlation coefficient falls to 0.5 at 3.5 wavelengths normal to the path, while along the path the corresponding distance is about 40

wavelengths. In the analyses of these data, recognizable meteoric signals were excluded.

8.3.3.3. Frequency Correlation

The extent of correlation of fading across a frequency band affects the modulation bandwidth which may be usefully employed and, hence, the design of frequency diversity techniques. Using narrow-beam (6°) antennas on 50 Mc/s, the correlation coefficient has been found to fall to about 0.5 for frequency separations of 6 kc/s during the early morning hours; and near noon the corresponding (6 kc/s) correlation coefficient is 0.65, falling to 0.5 for about 7 kc/s separation. This correlation is poorer for broad-band systems and for off-great-circle paths.

8.3.3.4. Geographical Variations

Observations have shown that, except for paths near the equator, the transmission loss for paths in the arctic, the United States, and Europe differ by less than ± 5 dB from the overall median value. Within these limits, the signal strengths on the arctic paths are, statistically, higher than those in middle latitudes.

Near the magnetic equator the signal intensities are, on the whole, much higher than in the United States. The background scatter signal is about the same, but this is obscured for a large portion of the time by strong enhancements (up to 50 dB) which appear to be reflected from field-alined ionization in the E region [4]. Rapid fading is often characteristic of these enhancements.

It may be of interest to note here that there is little correlation between VHF transmission loss in temperate latitudes and f_0E , or HF attenuation. There appears to be little variation of signal intensity with sunsport number but there is a statistical correlation (positive) with the magnetic K index [5].

8.3.4. Abnormal Behavior

8.3.4.1. Sudden Ionospheric Disturbances

These have been discussed already in section 6.2.4, but a few more comments are appropriate as it appears that the behavior of the received VHF signal varies with frequency. The increased ionization created by

the flare radiation appears to produce two effects: intensity enhancement (more efficient scattering) and increased D region absorption. On the lower frequencies, where the absorption effects are greatest, the net result is a decrease in signal. On the higher frequencies the overall effect is an increase in signal. On intermediate frequencies little effect is seen in many instances, from which it may be concluded that the two processes just cancel. The effect on the received signals on five frequencies are shown in figure 8.2 for signals transmitted over a 1295 km path (United States) employing narrow beam antennas. A definite frequency dependence is evident. On the other hand, with parallel broad-beam systems, increased attenuation was observed on all frequencies up to 75 Mc/s (the highest frequency used).

8.3.4.2. Correlation With Auroral Phenomena

We have seen already (sec. 6.3.3) that HF propagation in the auroral zone is characterized by periods of high absorption. These periods are

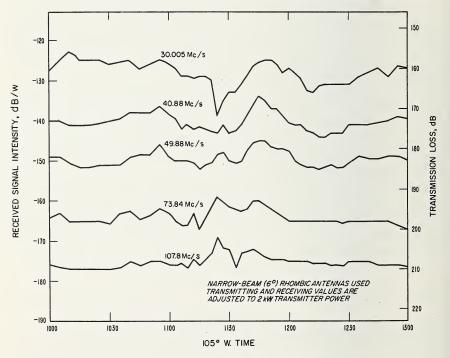


Figure 8.2. Signal behavior on five frequencies during a sudden ionospheric disturbance, March 29, 1958.

(After J. Blair, R. M. Davis, and R. C. Kirby, 1961; J. Res. NBS 65D (Radio Prop.), 417.)

not, in general, periods of high absorption of VHF waves. On the contrary, high signal intensities, on 50 Mc/s, are usually observed during periods of enhanced HF absorption and strong geomagnetic activity. It has been found also that marked increases in signal level often coincide with isolated intervals of HF blackout [6].

8.3.4.3. Sputter

An additional effect associated with aurorae is the occurrence of rapid fading called "sputter," which is due to a multipath signal. There have been occasions when "sputter" speeds of up to 200–300 c/s have been observed, i.e., about 100 times the normal fading rate. The effect is minimized with narrow-beam antennas. It may be observed, to some degree or other, 100 hr and more per year [3].

8.3.4.4. Polar Cap Absorption Effects

Forward scatter signals are affected during PCA events (see sec. 6.4) in high latitudes. If the onset of the proton flux (which gives rise to the PCA) occurs at night, the VHF signals are enhanced (fairly abruptly) followed by strong absorption during the ensuing daylight. The fact that the scattered signals are absorbed during the PCA while enhanced during auroral blackouts indicates that the height at which scattering occurs lies below the region of auroral absorption (90 km) but above the height at which polar cap absorption occurs (60 km).

Polar cap absorption events are generally confined to paths with midpoints at geomagnetic latitudes greater that about 60°. The onset of this absorption (in the lower latitudes) usually follows the onset of a magnetic storm and often at the time of a strong (Forbush) decrease in the intensity of cosmic rays which is, in general, many hours after the commencement of the PCA itself in higher latitudes.

8.4. METEOR SCATTER³

8.4.1. Ionization by Meteors

Mention has been made above to the fact that in VHF forward scatter strong bursts of signal are frequently superimposed on the background

¹ This section is based on a paper by G. R. Sugar (1964), Radio Propagation by Reflection from Meteor Trails, Proc. IEEE 52, No. 2, 116-135.

signal reflected from turbulent irregularities. These bursts are due to reflections from ionized "trails" produced by meteors mostly in the height range 80 to 120 km. Billions of these trails are produced daily; they diffuse rapidly and usually disappear within a few seconds. During their brief existence, however, these ionized columns will reflect VHF waves particularly in the frequency range 20 to 110 Mc/s. The lower frequency limit is set by the need to be above the regular maximum usable frequency and the upper limit is set by technical limitations, since reflections on the higher frequencies are relatively weak.

The ionized trail is the result of conversion of the kinetic energy of the meteor into potential energy of ionization as the meteor is slowed down by collisions with the neutral molecules. The ionization is distributed in the form of a long, thin paraboloid of revolution with the particle at the head of it. The electron density per unit length of the trail is proportional to the mass of the particle.

The height distribution of trails varies with particle characteristics. The higher velocity particles (of a given mass) produce trails at the higher (120 km) heights, with the mean trail height increasing by about 10 km as the velocity increases from less than 15 km/s to greater than 60 km/s [7]. For a given velocity, particles of higher mass produce maximum trail ionization at lower heights. Over the mass range 10^{-7} to 10^3 g the height variation is around 44 km. There is also a height variation with the zenith angle (χ) of the trail, larger angles corresponding to greater heights. A variation of about 13 km corresponds to the range of χ from 0 to 90°.

The lengths of the trails depend primarily on the mass and zenith angle. Typical lengths range up to 50 km, the most probable value being 15 km, although this depends on the definition of "length."

The initial radii of the trails are in the range 0 to 1.2 m (with a mean value of 0.65 m) based on visual studies, while radio observations give a range from 0.55 m to 4.35 m. The 0.55-m-radius is for a height of 81 km.

Let us consider now the dissipation of the ionization. Once the trail is formed it expands by diffusion at a relatively low rate, thus producing a radial distribution of material that is approximately Gaussian. After a time t the radius r is related to initial radius r_0 by the expression:

$$r^2 = r_0^2 + 4 Dt, (8.5)$$

where D is the diffusion coefficient of the electrons and varies from one m^2/\sec at '85 km to 140 m^2/\sec at 115 km. Hence, after 1 sec, a trail will have a radius in the range 2 to 20 m.

The practical lifetime of a trail depends, of course, on the means of detection. Most trails, detected by radio methods, are those resulting from small particles and last for a fraction of a second only. Larger meteors produce more densely ionized trails, and trails with durations of the order of 1 min are observed several times per day. Trails with durations of the order of an hour or more are extremely rare.

The dissipation of trails is complicated further by the action of winds in the 80 to 120 km region. At the time of formation, trails are quite straight but they are deformed rapidly by winds of the order of 25 m/sec and vertical wind shears with maxima of the order of 100 m/sec per km. A wind shear of this magnitude can rotate part of a trail through an angle of 5° in 1 sec.

8.4.2. Meteor Data

Before considering the reflection of radio waves from meteor trails, it will be useful to discuss some of the physical properties of meteors. Nearly all our knowledge in this field comes from visual and radio observations. The term "meteor" will be restricted to those particles entering the earth's atmosphere that are completely burned up by frictional heating.

Particles in the mass range of 10^{-7} to 10^3 g and dimensions in the range 40 μ to 8 cm are primarily responsible for radio reflections. Before being swept up by the earth's atmosphere these meteors move in elliptical orbits around the sun and they are thought to be of cometary origin.

Meteors can be divided into two classes:

Shower meteors are collections of particles all moving with the same velocity in fairly well-defined orbits around the sun. These meteors, while the most spectacular, account for only a small fraction of the total incidence of meteors.

Sporadic meteors comprise nearly all those of interest to radio work. These meteors seem to move in random orbits so that, in contrast to the shower meteors which appear to come from a specific "radiant" point in the sky, sporadic meteors have radiants that appear to be randomly distributed over the sky. It is of interest to note that a meteor shower is often named after the stellar constellation in which the radiant point lies, e.g., Leonid for Leo.

The radiants and times of occurrence of sporadic meteors are random and of course cannot be cataloged in this manner. Their radiant points are not, however, uniformly distributed in the sky but are for the most part concentrated toward the ecliptic plane (the plane of the earth's orbit) and move in the same direction around the sun as the earth moves [8]. The orbits are not uniformly distributed along the earth's orbit but are concentrated so as to produce a maximum incidence of meteors at the earth in July and a minimum in February. This variation in the space density of meteors is shown in figure 8.3, which has been adapted from the data of Hawkins [8].

The rate of incidence of sporadic meteors at the earth is further modified by two factors. The first of these, resulting in a regular diurnal variation in meteor rate, is illustrated in figure 8.4. On the morning side of

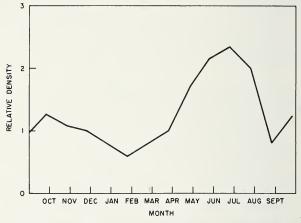


FIGURE 8.3. Variation of space density of meteors along the earth's orbit.

(After G. S. Hawkins, 1956, Monthly Notices Roy. Astron. Soc. 116, 103.)

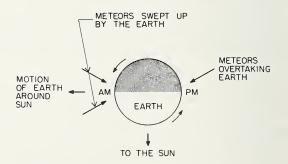


FIGURE 8.4. Diurnal variation of meteor rates.

In the evening only meteors overtaking the earth are observed. In the morning meteors with orbital directions opposite to that of the earth and the slower ones with the same orbital direction are observed. (After G. R. Sugar, 1964, Radio propagation by reflection from meteor trails, Proc. IEEE 52, No. 2, 116.)

the earth, meteors are swept up by the forward motion of the earth in its motion around the sun. On the evening side the only meteors reaching the earth are those which overtake it. This results in a maximum occurrence rate around 6 a.m. and a minimum rate around 6 p.m. The ratio of maximum to minimum depends on the latitude of the observer. A further minor seasonal variation is introduced because of the tilt of the earth's axis relative to the ecliptic plane. This variation, also dependent on the latitude of the observer, can change the expected hourly rates by factors as large as 1.4.

The mass distribution of sporadic meteors is such that there are approximately equal total masses of each size of particle. There are, for example, 10 times as many particles of mass 10^{-4} g as there are particles of mass 10^{-3} g. This approximate relation between particle mass and number is given in table 8.1. The mass distribution of shower meteors is somewhat similar to that for the sporadic meteors with the important

Table 8.1. Order-of-magnitude estimates of the properties of sporadic meteors

| | Mass (grams) | Visual magnitude | Radius | Number of this mass or greater swept up by the earth each day | Electron line density (electrons per meter of trail length) |
|---|--|--|---|---|--|
| Particles pass through the at- mosphere and fall to the ground | 104 | -12.5 | 8 cm | 10 | |
| Particles totally disintegrated in the upper atmosphere Approximate limit of radar measure- ments→ | 10 ³ 10 ² 10 1 10 ⁻¹ 10 ⁻² 10 ⁻³ 10 ⁻⁴ 10 ⁻⁵ 10 ⁻⁶ 10 ⁻⁷ 10 ⁻⁸ | $\begin{array}{c} -10.0 \\ -7.5 \\ -5.0 \\ -2.5 \\ 0.0 \\ 2.5 \\ 5.0 \\ 7.5 \\ 10.0 \\ 12.5 \\ 15.0 \\ 17.5 \end{array}$ | 4 cm 2 cm 0.8 cm 0.4 cm 0.2 cm 0.08 cm 0.02 cm 80 μ 40 μ 20 μ 8 μ | 10^{2} 10^{3} 10^{4} 10^{5} 10^{6} 10^{7} 10^{8} 10^{9} 10^{10} 10^{11} 10^{12} ? | 10 ¹⁸ 10 ¹⁷ 10 ¹⁶ 10 ¹⁵ 10 ¹⁴ 10 ¹³ 10 ¹² 10 ¹¹ 10 ¹⁰ ? |
| Micrometeorites (Particles float down unchanged by atmospheric collisions) | $ \begin{array}{c} 10^{-9} \\ 10^{-10} \\ 10^{-11} \\ 10^{-12} \end{array} $ | 20.0 22.5 25.0 27.5 | 4 μ 2 μ 0.8 μ 0.4 μ | Total for this group estimated as high as 10 ²⁰ | Practically none |
| Particles removed from the solar system by radia- tion pressure | 10-13 | 30 | 0.2 μ | | |

difference that there are more large particles relative to the number of smaller ones than for the sporadic meteors [9].

The velocities of meteors approaching the earth are in the range 11.3 to 72 km/s. The lower limit is the escape velocity for a particle leaving the earth and is, therefore, the lowest velocity that a particle falling toward the earth can have. The upper limit is the sum of two components, a 30 km/s component associated with the velocity of the earth in its orbit around the sun, and a 42 km/s component associated with the meteor itself. This latter velocity is the escape velocity for a particle leaving the solar system. Nearly all observations indicate that meteor velocities fall in the above range, which suggests that meteors are members of the solar system.

8.4.3. Reflection From a Meteor Trail

8.4.3.1. Important Parameters

The distribution of energy reflected by a meteor trail is a function of many variables. The ionization density distribution across and along the trail, the orientation of the trail, the radio wavelength, the polarization of the incident wave relative to the trail, motion of the trail either as part of the process of formation or due to ionospheric winds, and the straightness of the trail are all significant. In discussing the reflection properties it is convenient to divide the trails into two classes—underdense trails and overdense trails—and to examine the properties of each class independently. Underdense trails are those wherein the electron density is low enough so that the incident wave passes through the trail and the trail can be considered as an array of independent scatterers. Overdense trails are those wherein the electron density is high enough to prevent complete penetration of the incident wave and to cause reflection of waves in the same sense that the ordinary ionospheric reflections occur. A rough sorting of trails into these two categories can be done on the basis of trail lifetime or duration. On long wavelengths (relative to the VHF band) the underdense trails have durations of less than about 1 sec while the overdense trails have longer durations. The analysis can be further divided in terms of the radio wavelength. On long wavelengths the effective duration of a trail is large compared to the time it takes the trail to form, and the trail may be considered to have a cylindrical shape. On short wavelengths, however, the duration is much shorter and the column must be considered to be of the paraboloidal form previously indicated.

The solutions to be considered here are at best useful approximations to the physical problems. They will apply quite well to some of the trails observed and rather poorly to others. A complete analysis of the reflections from even a relatively simple trail would be far too complex to be of any practical use or interest. In the following treatment the terms long wavelength, etc., are used in a relative manner to indicate the lower frequency end of the VHF band, etc.

8.4.3.2. Long Wavelength Reflections From Low-Density Trails

On the assumption that the trail is an infinitely long right circular cylinder of electrons whose diameter is very small compared to the wavelength, assume also that the trail electron density is low enough that the incident wave passes through the trail without major modification. Consider the case of radarlike reflections with transmitter and receiver at the same location. Figure 8.5a illustrates the reflection geometry and the trail model. Let R be the length of the perpendicular from the radar set to the trail. The signal received can be computed by summing the energy backscattered by each electron in the trail while taking proper account of the phase relations of these contributions. When this is done it is found that the principal contribution of energy from a trail is from its first Fresnel zone, a region of length $\sqrt{2\lambda R}$, centered at the point on the trail where the line from the radar is normal to the trail. For example, on 50 Mc/s a trail 200 km away will have a first Fresnel zone 1.6 km in length. As the trail expands by diffusion, the phase difference of the contributions from the electrons on opposite sides of the trail increases so that the received power decreases. The signal amplitude will have fallen to $1/\epsilon$ of its initial value ($\epsilon = 2.718$) at the time the radius of the trail is $\lambda/2\pi$. On 50 Mc/s this radius is 1 m.

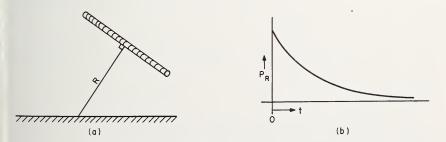


FIGURE 8.5. Low-density long-wavelength reflections.

(a) Reflection geometry. (b) Variation of received signal with time. (After V. R. Eshleman, 1960, Meteor scatter, The Radio Noise Spectrum, ch. 4, Harvard Univ. Press.)

The transmission equation can be written in terms of the scattering cross section σ in the following way:

$$\frac{p_r}{p_t} = \frac{g_t g_r \lambda^2}{16\pi^2 R^4} \, \sigma,\tag{8.6}$$

where p_t and p_r are, respectively, the transmitted and received power,

 g_t and g_r are, respectively, the power gains of the transmitting and receiving antennas relative to an isotropic radiator in free space,

 λ is the wavelength in meters,

R is the distance from transmitter to the trail in meters, and σ is the scattering cross section of the trail in square meters.⁴

If it is assumed that the trail is initially in the form of a line of electrons (an initial trail radius of zero), the scattering cross section may be written as

$$\sigma = (\sqrt{R\lambda/2}r_eq)^2 \exp\left(-\frac{32\pi^2 D}{\lambda^2}t\right), \tag{8.7}$$

where $r_e = \mu_0 e^2 / 4\pi m = 2.8178 \times 10^{-15}$ m, the classical radius of the electron, where μ_0 is the permeability of free space and e and m are the charge and mass of the electron,

q is the electron line density of the trail in electrons per meter, D is the diffusion coefficient in square meters per second, and t is time measured from the formation of the trail, in seconds.

The first of the two factors in (8.7) represents the scattering cross section of the initial line distribution of electrons, and the second factor represents the attenuation with time as the trail expands and destructive interference begins. The first factor may be interpreted as follows: The effective cross section of the trail is the same as would be obtained for in-phase addition of scattered fields associated with each electron within one-half of the first Fresnel zone. Since the power scattered by an electron is proportional to r_e^2 then the field is proportional to r_e . The number of electrons in half of the first Fresnel zone is $q\sqrt{R\lambda/2}$ and the field is, therefore, proportional to $r_e\sqrt{R\lambda/2}$. The total effective cross section is just the square of this product.

The second factor in (8.7) results from the integration across the trail. The distribution of electrons across the trail has a Gaussian shape

⁴ The scattering cross section is the ratio of the power scattered per unit solid angle to the power incident per unit area.

[9] with an effective radius of $\sqrt{4Dt}$. Using this with (8.6) and (8.7), it can be shown that the signal amplitude will fall to $1/\epsilon$ when the effective radius is $\lambda/2\pi$.

If the initial radius is nonzero, the peak amplitude is reduced from that given by (8.6). The form of the time variation of received power is sketched in figure 8.5b.

In the above relation, since it was assumed that trails were of infinite length, every trail had a first Fresnel zone and therefore gave a reflection. In practice, however, since trails are of finite length, this zone may not lie on the trail but rather on an extension of it. In such a case the signal returned from the trail would be a relatively weak one, and in practice these returns are of little importance. Thus a radar can "see" only a fraction of all the trails incident on the ionosphere within its range because most trails do not have the proper orientation for the line of sight to be perpendicular to the trail. The requirement for proper orientation can be restated as requiring that the trail be tangent to a sphere centered at the radar.

When the transmitter and receiver are separated, as in the case of point-to-point propagation, the reflection requirement is that the incident ray and reflected ray make equal angles with the trail axis. Geometrically this is equivalent to a requirement that the trail be tangent to an ellipsoid with foci at the transmitter and receiver. For this case two important changes take place because of the oblique geometry. First, the length of the first Fresnel zone increases and, therefore, more electrons contribute to the received signal. Second, the maximum possible propagation path difference over the cross section of the trail decreases with increasing obliquity. This decrease is equivalent to an increase in wavelength and results in both a larger initial signal and a slower rate of signal decay as the trail expands.

In this case it can be shown [10, 11] that the peak received power varies as $\lambda^3 q^2$ and the signal duration as λ^2 .

8.4.3.3. Long Wavelength Reflections From High-Density Trails

With high electron densities the assumption that the incident wave passes through the trail essentially unmodified is no longer valid. For this case it is assumed that the wave penetrates the trail until reaching a surface of sufficiently high electron density to be reflected. The model used is that of an expanding cylindrical reflector of radius r_c , figure 8.6a. After a time the electron density everywhere within the trail falls below

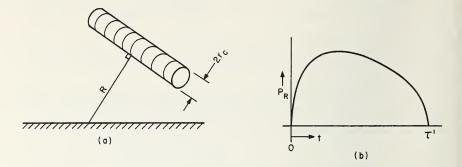


FIGURE 8.6. High-density long-wavelength reflections.

(a) Reflection geometry. (b) Variation of received signal with time. (After V. R. Eshleman, 1960, Meteor scatter, The Radio Noise Spectrum, ch. 4, Harvard Univ. Press.)

the critical value and the underdense model is once more applicable. However, by this time the radius is quite large and the signal contribution is rather small.

In the case of backscatter, the transmission equation is based on reflection from a cylinder and is given by

$$\frac{p_r}{p_t} = \frac{g_t g_r \lambda^2}{64\pi^2 R^3} \left[4 Dt \ln \left(\frac{r_e q \lambda^2}{4\pi^2 Dt} \right) \right]^{\frac{1}{2}}$$
(8.8)

and this applies until approximately the time when the second factor becomes zero. This occurs at a time

$$\tau' = \frac{r_e q \lambda^2}{4\pi^2 D}; \tag{8.9}$$

after this time the relation for underdense trails is applicable [12]. The form of the time dependence of received power predicted by (10.8) is illustrated in figure 8.6b.

For the overdense case the maximum received power varies as $q^{\frac{1}{2}}$ in contrast to the q^2 variation for the underdense case. The λ^3 dependence is the same as for the latter case.

The dividing line between low- and high-density trails is commonly taken to be for q in the range 1 to 2.4×10^{14} electrons per meter. If the transition value is taken at 0.75×10^{14} electrons per meter, then the peak signals predicted by (8.8) will be equal; this is sometimes done for convenience [12].

The extension of (8.8) to the forward scatter case has been done in a relatively simple manner [12]. The derivation, as in the backscatter case, is based on a reflecting cylinder and the refractive effects of the electrons beyond the critical radius of the trail have been ignored. These refractive effects reduce the validity of the transmission equation [13], but their significance is uncertain.

The dividing line between low- and high-density trails is again at $q=0.75\times 10^{14}$ electrons per meter. The effect of the initial radius of the trail can be computed as in the backscatter case.

8.4.3.4. Short Wavelength Reflections From Low-Density Trails

In the previous two sections it has been assumed that the time of formation of a meteor trail is quite small compared to the total time that radio waves are scattered by the trail. The formation of the trail was in effect considered to be a transient state preceding the desired "steady state" trail and this transient was neglected. However, as the wavelength is decreased and the duration of this steady state decreases, the duration of the transient state tends to remain constant. For sufficiently short wavelengths only the transient state remains. In this section and the following one this transient state will be considered [14], first for underdense trails, then for overdense trails.

Consider first the problem of estimating the shortest wavelength for which the long wavelength results are applicable. The time of formation of a trail is essentially the time required for the incoming particle to traverse one-half the first Fresnel zone as defined for the long wavelength case. A rough estimate of the transition wavelength between long- and shortwave cases may be obtained by equating the time of formation for a trail to the duration of a longwave echo and solving for the wavelength. For example, consider backscatter reflections from an underdense trail. The time to traverse half the first Fresnel zone is $(R\lambda/2)^{\frac{1}{2}}/v$, where v is the meteor velocity, and the nominal echo duration (to the $1/\epsilon$ amplitude) is $\lambda^2/16\pi^2 D$. Equating these and solving for λ_T , the transition wavelength, we obtain

$$\lambda_T = (128\pi^4 D^2 R/v^2)^{\frac{1}{3}}. (8.10)$$

Using as typical values R=500 km, v=40 km/s, and D=3 m²/sec, a transition wavelength of 3.3 m is obtained.

Since in practice there can be a wide variation in the values of the parameters in (8.10) it is necessary to evaluate λ_T for each specific case.

If the practical extremes of all of the variables for both the backscatter and forward scatter cases are investigated, it is found that the transitional wavelength can be anywhere in the range 0.1 to 100 m. For a random sample of meteors the transitional wavelength is likely to be near 2.9 m for backscatter and in the range 0.5 to 1.6 m for forward scatter.

The short wavelength case is treated by considering the effects of differential diffusion as the trail is being formed. Each part of the trail begins to diffuse as soon as it is formed, and thus the effective radius of the trail is smaller close to the meteor than farther back along the trail where diffusion has been going on for a longer time. The effective radius for any part of the trail is taken as $r = \sqrt{4 Dt}$, the same value previously used for the whole trail. Now it can be shown that, except near the end of its path, the velocity of the meteor can be considered to be constant. Therefore position along the trail is proportional to t and the relation $r = \sqrt{4 Dt}$ indicates that the trail will have the form of a paraboloid of revolution.

The geometry is shown in figure 8.7a and the time variation in received power is given in figure 8.7b. The time t=0 is the instant of closest approach of the meteor.

In this case the peak power varies as q^2 as was true in the long wavelength underdense trail case. With decreasing wavelength the power falls as λ^6 is compared with λ^3 for the long wavelength underdense case. This rapid variation with wavelength is consistent with the fact that very few observations of meteor reflections have been made on frequencies above the VHF range.

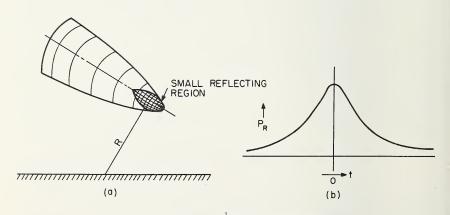


Figure 8.7. Low-density short-wavelength reflections.

(a) Reflection geometry. (b) Variation of received signal with time. (After V. R. Eshleman, 1960, Meteor scatter, The Radio Noise Spectrum, ch. 4, Harvard Univ. Press.)

8.4.3.5. Short Wavelength Reflections From High-Density Trails

This case is of less practical interest than those discussed above and, consequently, will not be treated here. A brief discussion of this case is given in the paper by Sugar [11], which should be consulted by the interested reader.

8.4.4. Other Aspects of Reflections From Meteor Ionization

In the previous four sections, reflections from meteor trails have been considered from a relatively idealized viewpoint and many of the practical aspects have been ignored. In this section some of these will be discussed from a qualitative viewpoint. The discussion is directed toward the long wavelength cases, since relatively few observations on short wavelengths have been made and analyzed.

8.4.4.1. Long Wavelength Reflections During Trail Formation

The transient state associated with trail formation is of some interest since it accounts for some of the observed characteristics of trail reflections. As a trail is being formed, but before the meteor reaches the first Fresnel

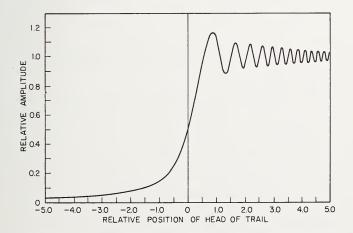


Figure 8.8. Amplitude variation of received signal as trail length increases.

The limits of the first Fresnel zone are at +1 and -1. (After M. Lowenthal, 1956, MIT Lincoln Laboratory Tech. Rept. 132.)

zone, a weak reflection is obtained from the incomplete trail. This comes primarily from the part of the trail corresponding to the shortest transmission path at the instant; and, when, as is usually the case, this is the head of the trail, the reflected signal is shifted in frequency because of the motion of the effective reflecting point. As the meteor approaches the first Fresnel zone for the trail this frequency shift approaches zero, and thus the received frequency decreases with time. The observed frequency will of course depend on trail orientation, meteor velocity, and observing wavelength. A maximum shift of the order of 5 kc/s is possible on 50 Mc/s over a 1000 km path.

As the meteor crosses the first Fresnel zone, the specular reflection occurs, accompanied by a large signal enhancement. Then as the particle continues on, the additional ionization from the lengthening trail creates a minor fluctuation of the signal as shown in figure 8.8. Most trails do not have the proper orientation to produce a specular reflection and in these cases only the weak Doppler-shifted component is observed.

8.4.4.2. Trail Drift and Distortion

The effects of ionospheric winds are appreciable for trails which last for the order of a second or more. A Doppler shift of the received frequency will be associated with the average wind velocity at the trail. For a velocity of 25 m/s this "body Doppler" can be as large as 18 c/s for backscatter observations on 50 Mc/s and will be somewhat less for forward scatter observations.

The trail distortion resulting from wind shears can lead to the formation of several local first Fresnel zones for the trail since a distorted trail can have several points where the transmission path length has a local minimum. These local minima, or "glints" as they have been called, are strong scatters and the received signal is a composite of their contributions. Since they are moving at different velocities, the signals from each have different Doppler shifts and the resultant composite signal fades in an irregular manner. On 50 Mc/s the fading rates observed for forward scatter are of the order of 1 to 10 c/s. In addition to producing the fading observed for long-enduring trails, the wind shears can rotate a trail sufficiently to produce reflections when the initial orientation was not suitable. Thus these trails lose their aspect sensitivity as time goes on, and if their life is of the order of 10 sec they will scatter in all directions.

8.4.4.3. Diversity Effects

As pointed out in section 8.4.3, underdense trails act as small coherent sources and, therefore, CW signals scattered by them exhibit good space and frequency correlation. Correspondingly, very little pulse broadening is observed when pulse signals are used. The limited available data suggest that for a forward scatter path about 1000 km in length, operating near 50 Mc/s, the correlation coefficient observed for single inderdense trails will fall to 0.5 for antenna spacings of the order of 150 km along the path, for antenna spacings of the order of 30 km across the path, and for frequency separations greater than 5 Mc/s. Three-microsecond pulses show no appreciable broadening under these conditions.

Overdense trails, in contrast to the underdense trails, tend to act like relatively large sources and, therefore, exhibit much poorer space and frequency correlation properties. Again, as in the underdense case, specific data on these properties are not available. Available results [13] suggest that the correlation observed for single overdense trails will fall to 0.5 for antenna spacings of the order of 50 λ . Measurements using short pulses over a 1000-km path indicate that the received composite signal can have a total time spread as large as 10 μ sec [15].

8.4.5. Short-Term Statistical Characteristics

8.4.5.1. General Remarks

From the viewpoint of radio propagation it is the collective properties of trail reflections rather than the individual reflections that are of primary interest. These statistical characteristics can be divided into two classes. First there are the short-term properties, the ones which would be observed during a single hour or less. These can be thought of as being associated with a small but statistically significant sample of trails. Second are the long-term statistical characteristics of the reflections. These include the diurnal and seasonal variations, geographical factors, variations with systems parameters, etc. In the following sections the effects of the initial radii of the trails are ignored—the initial radii are assumed to be zero. This approach appears to be satisfactory since the simplified theory accounts satisfactorily for nearly all of the radio propagation properties of meteor trails. Difficulties arise primarily when one tries to deduce properties of the meteors themselves from the radio observations. For example, when the initial radii are assumed not to be zero,

different height distributions and mass distributions are obtained than for the zero radius case. These differences will not be important here since the older theory is consistent with the observations and thus the initial radius problem can be avoided.

8.4.5.2. Peak Amplitude Distribution

The peak amplitude of the reflection from an underdense trail is proportional to the electron line density q and, hence, proportional to the mass of the meteor [9]. For underdense trails the number N of signals observed with peak amplitudes greater than A is given by

$$N \propto A^{-1}. \tag{8.11}$$

For overdense trails A is proportional to $q^{\frac{1}{4}}$ and so

$$N \propto A^{-4}. \tag{8.12}$$

In general, it is better to write the relationship in the form

$$N = CA^{-a} \tag{8.13}$$

where C is a constant of proportionality and where a depends on the details of the observing system and in practice will be a function of the detection threshold A. If a very low threshold is used, then nearly all of the trails detected will be underdense and the exponent observed will be quite near a=1. If a very high threshold is used, nearly all of the trails detected will be overdense and the exponent will be near a=4. Between these two conditions there will be a transition region where contributions from both overdense and underdense trails will be important, and in this region the exponent a will lie between 1 and 4. The extent of the transition region depends on path geometry, antenna directivity, etc. Observations of shower meteors made using backscatter with highly directive antennas and, therefore, concerned with trails localized in position and orientation, indicated that the transition was complete in a 2 to 1 amplitude range [9]. In contrast, forward scatter observations of sporadic meteors, which therefore include a wide variation of positions and orientations, indicated that the transition extended over a 10 to 1 amplitude range [16]. Figure 8.9 gives the relation between threshold and rate computed for one experimental path [16]. The system parameters were $p_t = 100 W$, $\lambda = 7.5 m$, $g_t = g_r = 40$; a transmitter-receiver

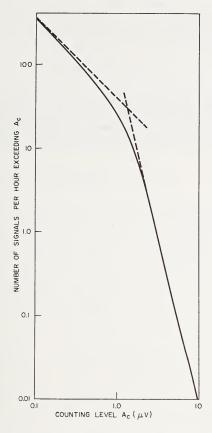


FIGURE 8.9. Theoretical rate-amplitude relation computed for the following parameters: $P_t = 100 \text{ W}$, $\lambda = 7.5 \text{ m}$, $g_t = g_r = 40$.

(After C. O. Hines, 1958, Can. J. Phys. 36, 549.)

separation of 1000 km was assumed and a mean trail height of 100 km was used. The upper and lower dashed lines in the figure have slopes of -1 and -4 respectively, corresponding to the theoretical distributions for underdense and overdense trails.

8.4.5.3. Duty Cycle Versus Threshold

Duty cycle is defined as the fraction of time that a received signal exceeds a prescribed threshold. To a first approximation it is the fraction of time that the reception of messages will occur in a meteor-burst communication system and it is an important parameter in systems work.

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The relationship between duty cycle T and the threshold A_1 for propagation by underdense trails is given by

$$T = (\tau/a) C A_1^{-a}. (8.14)$$

Here τ is the time taken for the amplitude to fall to $(1/2.78\cdots)$ of its initial value and a and C are defined by (8.13). Note that since this can be written as $T = (\tau/a)N$, the factor τ/a is just the average duration of a burst. For underdense bursts a = 1 and since duty cycle P is proportional to T, then

$$P(A > A_1) \propto A_1^{-a} = A_1^{-1}.$$
 (8.15)

In practice, the presence of overdense trails increases the observed value

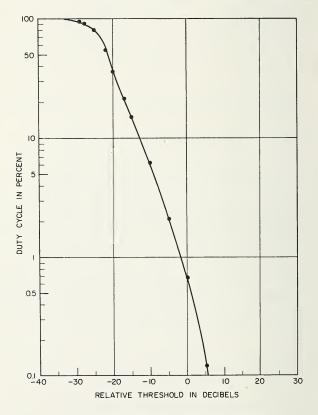


FIGURE 8.10. Duty cycle versus threshold.

(After G. R. Sugar, 1964, Radio propagation by reflection from meteor trails, Proc. IEEE 52, No. 2, 116.)

of a. Values commonly observed are in the range 1.1 to 3.5, with the large values apparently associated with a predominance of overdense trails. An example of the measured variation of duty cycle with threshold is shown in figure 8.10. Note that the slope of the curve increases at higher thresholds. The points at duty cycles higher than 10 percent include contamination from receiver noise and ionospheric scatter transmission as well as signals from overlapping meteor trails. They should not, therefore, be expected to fit the distribution law derived here.

8.4.5.4. Apparent Location of Trails

The geometrical conditions required for strong reflections from a trail, combined with the radiant distribution for sporadic meteors, are such as to favor trails occurring in some parts of the sky and to discriminate against those in other parts of the sky. The result is that the meteors contributing to propagation over a particular path occur in a relatively small region of the sky, the so-called "hot spot." For the longer trans-

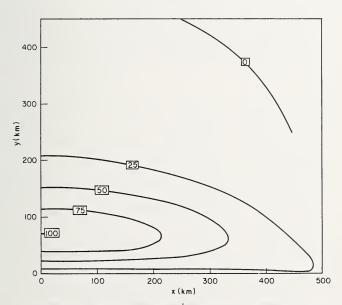


FIGURE 8.11. Relative signal contributions from various parts of the meteor region computed for a 1000 km path.

The origin of coordinates represents the path midpoint, x and y are respectively displacements along and normal to great circle path. Results in the other quadrants are symmetrical to these. (After C. O. Hines, 1956, Can. J. Phys. 34, 1013.)

mission paths this region is near but not at the path midpoint. The midpoint itself is a region where very few trails are observed [17]. Figure 8.11, adapted from Hines and Pugh [18], shows the relative cumulative signal durations for contributions from various parts of the meteor region. The data were computed for a 1000 km transmitter-receiver separation, a meteor trail height of 100 km, and an isotropic distribution of incident meteors. In practice the actual distributions will differ from these because the incident meteor flux is in fact nonisotropic. Further data on this point will be presented in the next section.

8.4.6. Long-Term Statistical Characteristics

8.4.6.1. Diurnal Variations

The characteristics to be discussed in this section include variations observable on an hour-by-hour or month-by-month basis and also variations associated with the characteristics of the observing system and its location. Nearly all data pertaining to these variations are relatively poor because of the large, seemingly random, hour-to-hour fluctuations in meteor activity that are observed. This random component of meteor activity is roughly comparable to a random variation in transmitter power output over a 10-dB range. It introduces a substantial uncertainty into many observations.

The diurnal variation in meteor rate results in substantial diurnal variations in many of the characteristics of meteor propagation. Three basic factors are significant: the meteor arrival rate varies, meteor velocities vary, and the effective radiants vary throughout the day.

The meteor arrival rate will have a roughly sinusoidal variation throughout the day with a maximum around 6 a.m. and a minimum around 6 p.m. The ratio of maximum to minimum averages around 4.

The average meteor velocity also has a roughly sinusoidal diurnal variation, with its maximum around 6 a.m. and minimum around 6 p.m. The diurnal variation in velocity cannot exceed 60 km/s (twice the orbital velocity of the earth) and, in practice, averages much less than this. A variation of 10 to 15 km/s above and below a daily mean velocity of 35 to 45 km/s is typical. The velocity variation is not in itself of much significance in radio work but its consequences are. The velocity variation leads to a diurnal variation in trail height; and this, in turn, because of the variation of diffusion coefficient with height, leads to a diurnal variation in the duration of meteor bursts. Observations of the diurnal variation in the duration of meteor bursts.

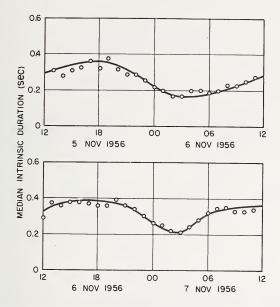


Figure 8.12. Diurnal variation of the $1/\epsilon$ duration of underdense meteor bursts.

(After T. J. Keary and J. H. Wirth, 1960, Statistical characteristics of forward scattered radio echoes from meteor trails, Electromagnetic Wave Propagation,
Academic Press, p. 277.)

ation of the $1/\epsilon$ duration of underdense bursts are illustrated in figure 8.12, which indicates that the duration varies over a 2-to-1 range through the day [19].

The diurnal variation of meteor radiants can be considered here only in a qualitative manner because of the general complexity of the problem and the present uncertainties regarding the actual radiant distributions. Because of the orbital motion of the earth, most meteors appear to have radiants concentrated in the hemisphere ahead of the earth (the morning hemisphere); and very few radiants appear to be behind the earth. As the earth rotates, the position of the predominant radiants changes relative to the transmission path, and the location of the "hot spot" moves around. As a result of this motion, average values of the geometric factors in the transmission equations will vary, and a diurnal change in received power will occur. This change is difficult to observe since received power will also change due to diurnal variations in meteor rate. An indication of the effects of diurnal variation of radiants can be seen in figure 8.13 (after Hines [20]), which depicts the predicted diurnal variation in meteor rates for each side of a north-south and an east-west transmission

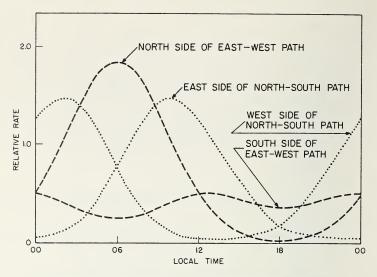


FIGURE 8.13. Predicted diurnal variations in meteor rates.

(After C. O. Hines, 1956, Diurnal variations in forward scattered meteor signals, J. Atmospheric Terrest. Phys. 9, 229.)

path. The differences in the shapes of the various curves indicate the effects of radiant changes relative to path orientation. The sum of all four curves would be an approximate indication of the diurnal variation in the arrival rate of meteors.

Given adequate measures of the above three basic diurnal factors, it should be possible to predict the diurnal characteristics of any transmission path; and it has been possible to do this with a reasonable degree of success in the case of meteor rates. The prediction of duty cycles is more complicated because of the diurnal variation of velocities, and it appears that this prediction has yet to be made.

The combination of the above three basic variations together with the random components of arrival rates results in rather irregular daily variations of meteor rates. Figure 8.14 illustrates the rates observed on 49.8 Mc/s over a 1245-km path on two days, a week apart [21]. While the data for each day show the general characteristics described above, the detailed variations on the two days are quite different.

8.4.6.2. Monthly Variations

Month-to-month variations in meteor-propagation characteristics are primarily associated with similar variations in meteor characteristics.

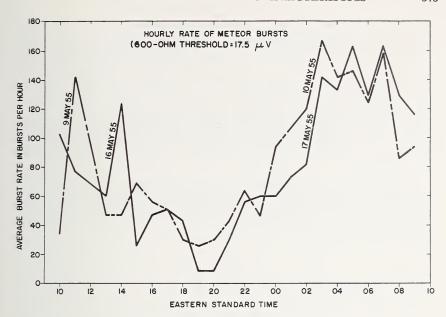


Figure 8.14. Observed diurnal variation of meteor burst rates, Cedar Rapids-Sterling on 49.8 Mc/s.

(After G. F. Montgomery and G. R. Sugar, 1957, The utility of meteor bursts for intermittent radio communication, Proc. IRE 45, 1684.)

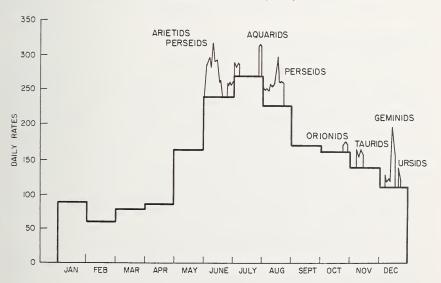


FIGURE 8.15. Seasonal variation of meteor rates.

(After G. S. Hawkins, 1956, Astron. J. 61, 388.)

There is little evidence that any of the normal month-to-month variations in ionospheric characteristics are reflected in meteor propagation characteristics, with the possible exception of D region absorption. The seasonal variation of meteor rates is illustrated in figure 8.15 (after Hawkins [8]). The echo rates shown are for meteor trails with an electron line density of 2.75×10^{14} electrons per meter or greater. The contributions of shower meteors are shown above the histogram for the sporadic meteors. The relative contributions of shower meteors will decrease as the system sensitivity is raised, since the two types have a different mass distribution.

As yet there is no satisfactory answer to the question of year-to-year variations in meteor activity. Such variations have been observed but most workers who have observed them have attributed them to changes in equipment sensitivity.

8.4.6.3. Geographical Variation

As yet this has not been clearly defined. The geographical variations, if present, are masked by the random variations.

8.4.6.4. Abnormal Absorption

Since most meteor trails are produced at heights above the absorbing region, the meteor signals are absorbed in much the same way as HF signals. On frequencies much greater than 30 Mc/s, the normal D region absorption is negligible. During periods of high absorption in high latitudes, the absorption can increase enormously and affect meteor propagation on frequencies as high as 100 Mc/s and more. During a major disturbance the duty cycle on a meteor-burst communications circuit between Goose Bay, Labrador, and Ottawa, Canada dropped by a factor over 10³, implying a signal attenuation of over 30 dB [22]. Disturbances of this magnitude are relatively uncommon and are not important in terms of the average characteristics of meteor-burst propagation. They are an indication, however, that this mode of propagation, like most others, can be disrupted and is, therefore, not the basis of a completely reliable communication system.

8.4.7. Use of Meteor Reflections for Intermittent Radio Communications

8.4.7.1. General Characteristics

Before leaving meteor propagation let us consider an application to communication systems. Meteor-burst communication systems are basically weak signal systems because the signal loss associated with the meteor-trail reflection is relatively high. For example, a typical system [15] operating on 50 Mc/s over a 1300 km path with a transmitter power of 2 kW was commonly set to transmit messages whenever the signal at the receiver exceeded 2×10^{-14} W (2 μV open-circuit voltage for a 50- Ω source). This corresponds to a system loss of 170 dB—under similar circumstances ionospheric scatter propagation would exhibit a system loss of the order of 180 dB. Of this total about 90 dB represents the attenuation associated with the length of the transmission path and 80 dB the scattering loss. Such a system was shown to be capable of a daily average teletypewriter transmission rate of 40 words per minute at a character error rate of 0.35 percent.

As is implied in the title of this section, meteor communication systems operate in an intermittent mode. They transmit messages only during the brief intervals when meteor propagation is present. Control of message transmission is achieved by providing for two-way transmission over the propagation path and transmitting only a control signal when a meteor trail is not present. When a meteor burst occurs, its presence is indicated by reception of the control signal, and message transmission can begin. These principles are incorporated in the JANET system [23]. In the interval between suitable meteor signals a system accepts messages and stores them for subsequent transmission. The system is, in essence, one that adapts its operation to the conditions of the transmission medium; it transmits only under favorable conditions. The aim is, of course, to obtain better overall transmission by avoiding the times when transmission is poor. Whether or not the intermittent mode of operation results in an overall improvement over continuous operation depends on the details of the equipment and on the characteristics of the propagation medium.

8.4.7.2. Channel Capacity

For an intermittent system operated at a fixed transmitter output and with band-limited Gaussian noise interference, the relation between channel capacity M and system bandwidth B is given by [21]

$$M = kB^{(1-\frac{1}{2}a)},\tag{8.16}$$

where k is a constant of proportionality.

From (8.16) we see that if a lies in the range $0 \le a < 2$ then, for a given transmitter output power, the channel capacity will increase as the signaling bandwidth is increased. Early measurements indicated that 1.2 was a typical value for a, thus suggesting that meteor-burst communication might be feasible. It is likely that this result, more than any other, has provided the impetus for the development of meteor-burst communication systems.

8.4.8. Concluding Remarks on Meteor Propagation

At the present time there is a large amount of theoretical and observational material available on most aspects of meteor propagation in the lower VHF range. As has been suggested in the previous sections, the available information is most complete for long wavelength underdense trails and least complete for the short wavelength overdense trails. Some of the areas where substantial work still remains to be done are studies of radiant distributions, properties of very small meteors, the effects of fragmentation, geographic factors, and the long-term fluctuations in propagation characteristics.

The adequacy of the presently available data can be examined from the viewpoint of the communication system design and engineering. If this is done, it appears that the present uncertainty in predicting the transmitter power required for a meteor communication circuit is probably of the order of 10 dB. At present it is not clear whether this number can be substantially reduced by further work. The whole field of system design is one where relatively little effort has been expended, and it is likely that major improvements in systems can still be achieved.

8.5. EQUATORIAL F SCATTER

8.5.1. History

Amateur radio operators had discovered that near the peak of the sunspot cycle (1947) they could communicate over long distances across the equatorial regions on frequencies (50 Mc/s) well above the maximum frequency to be expected for the distances involved. These radio contacts were most pronounced during nighttime in the equinoctial months.

During the International Geophysical Year more definite experiments were carried out on this phenomenon in the Far East [24] and in South America [25]. These experiments established that the enhanced signals were reflected from scattering centers located near the base of the F_2 layer.

8.5.2. Characteristics of F Scatter

8.5.2.1. Diurnal Variation

The signal appears usually during the evening and night when the signal level may rise 30 to 40 dB above the level produced by forward scatter.

8.5.2.2. Seasonal Variation

F scatter appears to be most prevalent around the autumnal equinox.

8.5.2.3. Geographical Variation

The echoes are aspect sensitive [25], so that the signal level depends on the orientation of the path relative to the earth's magnetic field. This also determines the direction of arrival of the signal. North-south paths, with midpoints within $\pm 20^{\circ}$ of the dip equator, are affected.

8.5.2.4. Fading

F scatter signals are characterized by flutter fading with fading rates of 10 c/s and more. The amplitude distribution is essentially Rayleigh and the carriers show Doppler shifts equivalent to a west-east motion of the order of 100 m/s.

8.5.2.5. Geophysical Factors

The occurrence of F scatter is associated with equatorial spread F [25] (frequency spread type) which is thought to be produced by patches of irregularities located at or below the bottom of the F layer. The thickness of these patches is estimated as 50 km. The scattering irregularities comprising these patches are elongated along the magnetic field with longitudinal dimensions of 1000 m or more and transverse dimensions of the order of 10 m or less. The geographical extension of a given patch may be as great as 1000 km in the east-west direction.

8.5.3. Flutter Fading

From the point of view of radio communications the most disastrous aspect of F scatter is the occurrence of flutter fading during the prime listening hours. The most severe fading sets in shortly after sunset (1800 local time) and lasts for 2 to 3 hr. During this period voice modulation is so "chopped up" it is almost unrecognizable.

Fixed frequency (50 Mc/s) pulse studies in the Far East have shown that, during the period of intense flutter fading, there is marked broadening of the echo pulses as shown in figure 8.16. Sweep-frequency studies (see fig. 4.16) in Africa have also shown this marked broadening which can amount to factors of more than 10 compared with the transmitted pulse width.

The spectra [26] of the F scatter signals (in Africa) was studied by means of the Doppler frequency technique described in section 3.2.3.2, and some records are shown in figure 5.13. The pre-sunset signals can be seen on the extreme left of figure 5.13; the spectra are relatively narrow. The post-sunset effect takes place around 1830. The frequency spectrum, during this period, has been known to broaden by at least 18 c/s. One of the remarkable features of these records is the striated structure which slopes downwards to the right. The broad nighttime spectra (and hence

Poro P. I. to Onna, Okinawa (837 miles) Range markers are 100 micro-seconds

Frequency: 49.84 Mc/s Power: 2 kw Antennas: 5 element H yagis Pulse length: 50 micro-seconds Pulse repetition rate: 100/second Receiver bandwidth: 120 kc/s

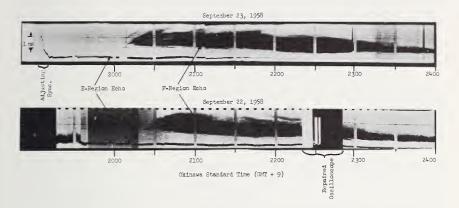


FIGURE 8.16. Range-time records showing pulse broadening of F-scatter echoes.

(After R. Bateman, J. W. Finney, E. K. Smith, L. H. Tveten, and J. M. Watts, 1959, IGY observations of F-layer scatter in the far east, J. Geophys, Res. 64, 403.)

the associated flutter fading) may be attributed to the motion of scattering irregularities.

Since the spread F responsible for flutter fading is limited in space and in time, there is a possibility that its effects may be minimized by suitable relaying of radio signals.

8.6. AURORAL SCATTER⁵

8.6.1. Radio Aurora

Radio aurora can be defined as "the ionospheric ionization, associated with auroral disturbances, that gives rise to radio reflection" [27]. While aurora itself may be defined as emitted radiation (visible and invisible), radio aurora is ionization which reflects radio waves. Thus we should not expect a one-to-one correlation between the spatial and temporal occurrences of one and those of the other. Radio aurora and visible aurora are separate phenomena with the same basic origin; that is, aurora is a manifestation of atomic excitation and ionization, and radio aurora

⁵ Based on a lecture by R. Cohen.

is constituted of the electrons and ions separated during the ionization process. However, reflections from radio aurora usually depend not only on the presence of ionization but also on the geometry involved. These aspect-sensitive reflections will not be observed unless the radio aurora is in the right place with respect to the observer. Thus from a given location one may see visible aurora but not radio aurora. On the other hand, radio aurora can be observed during the daytime when visible aurora cannot be seen.

A review of radio studies of the aurora has been made by Booker [28] and this should be consulted by the interested reader.

8.6.2. Bistatic Observations

The term "bistatic" is used to contrast a two-station (transmitter and receiver separated) method of observation with a single-station or monostatic method (radar). Auroral observations of this kind have always involved continuous-wave transmissions, so that the measurements of distances have had to be inferred from information on angles of arrival.

The most extensive bistatic studies of radio aurora are those of Collins and Forsyth [27], who have classified enhancements of the received signals into five categories:

- (1) E events, which are strong reflections probably from sporadic E patches,
- (2) S events, which are enhancements which are not accompanied by a magnetic disturbance.

The following A events are auroral phenomena closely associated with magnetic disturbance:

- (3) A_1 exhibits rapid fading (100 c/s) and is strongly aspect sensitive.
- (4) A_2 exhibits slow fading (1 cycle per 5 sec) and is slightly aspect sensitive.
- (5) A_3 exhibits slow fading and no aspect sensitivity, i.e., the signals arrive in the great circle.

This suggests that the A_3 signals are due to scattering from essentially isotropic irregularities.

Based on these results and some frequency-dependence measurements, Collins and Forsyth conclude that the A_1 and A_2 events can be ascribed to field-alined irregularities above a height of 100 km, and the A_3 events to more isotropic irregularities below that height. They also conclude from their frequency dependence measurements in the 32 to

50 Mc/s frequency range that the A_2 events can correspond to overdense irregularities with electron density as great as 3×10^7 cm⁻³, and that the usual electron density for the A_1 events was between 1.3 and 1.9×10^7 cm⁻³, corresponding to a plasma frequency range of about 32 to 39 Mc/s.

8.6.3. Monostatic (Radar) Observations

For localized observations of the radio aurora and the determination of its aspect sensitivity, radar methods are suitable. Furthermore, this method is useful in the study of movements. Numerous workers have contributed to radar-auroral research in the past 30 years and reviews of this subject are available [28, 29, 30]. Although the results of the radar studies are not altogether conclusive, certain facts are generally agreed upon and these will be summarized below.

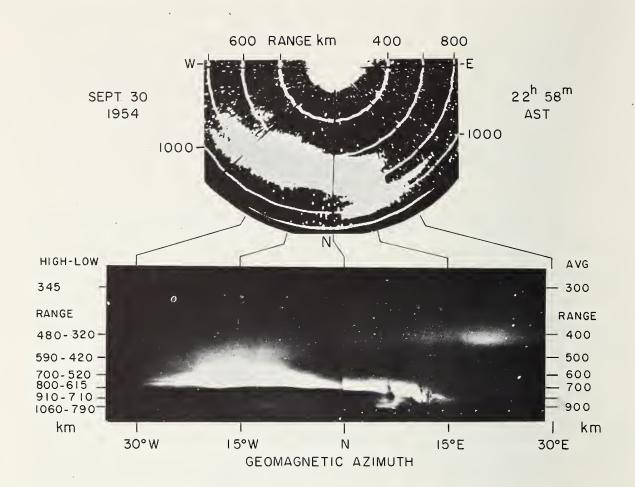
The determination of the spatial association between aurora and radio aurora is complicated by the aspect sensitivity requirements of the latter. By a comparison of the associated aurora with the radar echoes (at College, Alaska) Bowles obtained good correspondence as illustrated in figure 8.17. This figure shows, however, that radar echoes are obtained from only parts of the visual forms.

A striking demonstration of the aspect sensitivity of radio aurora has been given by Dyce [31], who operated a radar at Point Barrow, Alaska, located to the north of the visible aurora. The majority of radar echoes was obtained not from the south, but from the north.

The heights from which auroral radar echoes are reflected range from 75 to 135 km with a mean of about 110 km, which corresponds fairly well to the average height of the lower edge of most visual auroral forms.

Leadabrand et al. [32] also measured the azimuthal distribution and thence the aspect sensitivity of radar echoes on 398 Mc/s, and found that they could be obtained up to 10° away from the angle of perpendicularity to the earth's magnetic field. Presnell et al. [33] show that this departure is 12° on 216 Mc/s and 6° on 780 Mc/s. Thus, aspect sensitivity becomes more stringent as the frequency increases. It has been observed [32] that echoes from radio aurora at lower heights are confined to a narrower departure from perpendicularity than those from greater heights.

The frequency dependence of radar echoes from radio aurora has not been definitely determined. It is clear that the scattering cross section diminishes with increasing frequency, and that it is small at all frequencies, corresponding, for example, to a power reflection coefficient of order 10^{-4} on $106~{\rm Me/s}$.



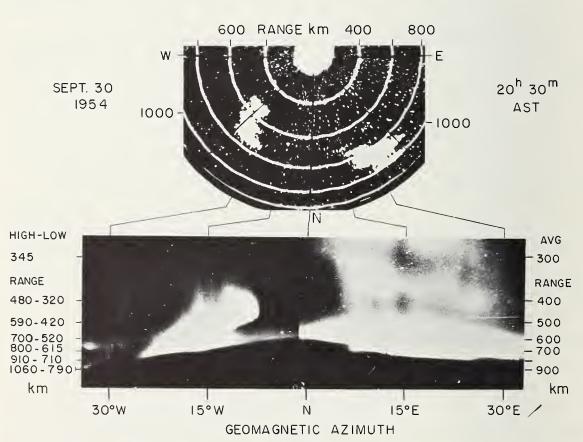


FIGURE 8.17. Association between visible aurora and radio aurora.

(After K. L. Bowles, unpublished.)

A number of workers have measured the frequency spectrum of radar echoes from radio aurora. Some of the spectra obtained by Bowles [34] in Ithaca, N.Y., and in College, Alaska, are shown in figure 8.18. The Doppler shifts and spreads of these spectra correspond to the motion of the irregularities in the radio aurora, and range motions observed simultaneously do not always correlate with them in magnitude or direction. Inasmuch as the range motions are probably spatial drifts resulting from redirection of the source of ionization, this apparent discrepancy is not surprising.

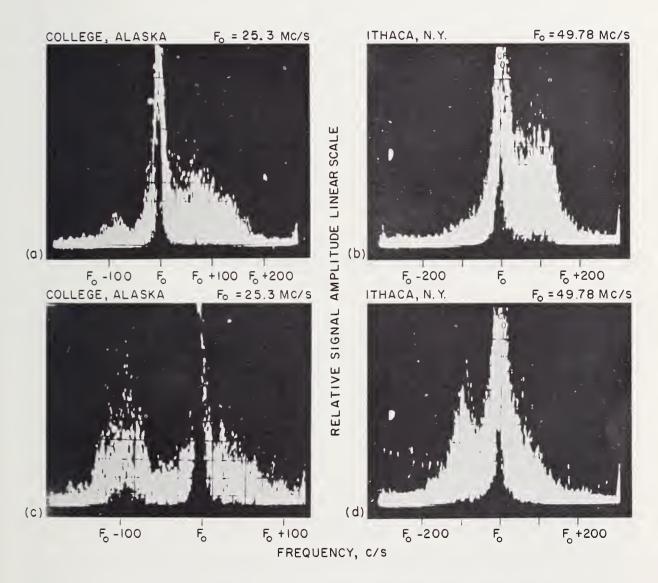


Figure 8.18. Spectra of VHF signals reflected from radio aurora.

(After K. L. Bowles, unpublished.)

8.7. INCOHERENT SCATTER⁶

8.7.1. Historical Note

It has been known for many years, especially in connection with x-ray scattering, that an individual electron has a cross section for the scattering of electromagnetic waves. In 1958, Professor W. E. Gordon [35] pointed out that with the existing radar sensitivities it should be feasible to measure ionospheric electron densities by detecting this weak Thomson scattering. Gordon pointed out that, from the theory, the Doppler spread (pressure broadening) imparted to the radiofrequency by the thermal motion of the electrons provided a means of measuring electron temperatures.

The existence of incoherent scatter was demonstrated in October 1958 by Bowles [36] with a scatter-radar in Long Branch, Ill. To obtain the high sensitivity required he used an antenna with a cross-sectional area of almost 5 acres and a pulse transmitter of about 1 MW peak power on a frequency near 40 Mc/s. The receiver bandwidth was of the order of 10 kc/s. Much to his surprise Bowles found that the line broadening was about 10 kc/s rather than the 100 kc/s predicted by Gordon. These results were corroborated, on a frequency of 440 Mc/s, at the Massachusetts Institute of Technology [37].

8.7.2. Scattering From an Individual Electron

The reason for high equipment sensitivity is, of course, the small value of the Thomson scattering cross section σ for a free electron (10^{-28} m²). The echo amplitude to be expected from a single free electron can be calculated as follows: The incident power density is $p_t g/4\pi R^2$ where p_t is the power transmitter, g is the antenna gain, and R is the range. The power absorbed (and re-emitted) is $p_t g \sigma/4\pi R^2$ and the received power p_r is $(p_t g \sigma/4\pi R^2)$ ($a/4\pi R^2$), where a is the antenna cross section. With a typical radar and scattering from the F region we assume the following values: $p_t = 10^6$ W, $g = 10^4$, $a = 10^4$ m², and $R = 3 \times 10^5$ m. This gives $p_r = 6 \times 10^{-39}$ W. For unity signal/noise we need about 10^{-15} W so that the scattering volume must contain something like 10^{24} electrons. In the F region N is about 10^{12} per cubic meter so that the scattering

⁶ Based on a lecture by K. L. Bowles.

volume required must be of the order of 10^{12} m³ (i.e., 10 km³). Thus a limit is set to the smallest volume that can be studied by a given radar system.

If the electrons are in thermal equilibrium with the ions and neutral molecules they will have, essentially, a Maxwellian distribution of ve-

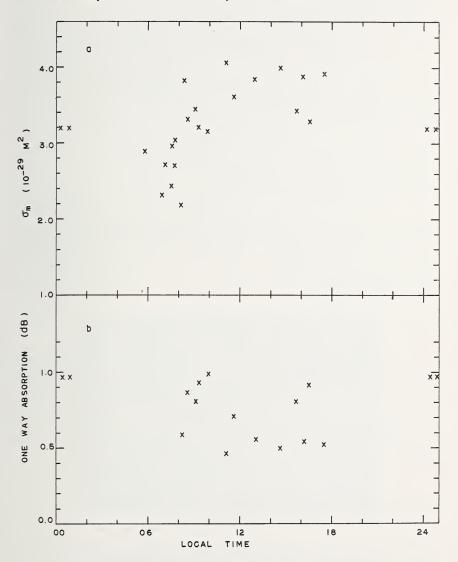


FIGURE 8.19. Electron cross sections for incoherent scatter measured at Jicamarca, Peru. (After K. L. Bowles, G. R. Ochs, and J. L. Green, 1962, J. Res. NBS 66D (Radio Prop.), No. 4, 395.)

locities and these motions will impose various Doppler shifts on the reradiated waves. For an average F region temperature of 1500 °K one expects that the spectrum on 41 Mc/s should be about 100 kc/s wide. The experimental width turned out to be about one tenth this value and it was realized that something was wrong with the simple theory. The reason for this discrepancy has been found to lie in the long-range Coulomb interactions between the positive ions and the electrons. Because of their charges and motions, the ions and electrons produce statistical fluctuations of charge density which almost cancel in space. If this were not so, strong space charges would develop, tending to restore neutrality. Because of this necessity to maintain electrical neutrality the motions of the electrons are constrained by those of the heavy ions. The observed line broadening is, therefore, not that due to the free electrons but rather to the ions wherein most of the momentum lies [36]. Because of this constraint it has been proposed to call the phenomenon "quasi-incoherent scatter." The theoretical implications of this idea have been studied by a number of workers [38, 39, 40].

It turns out that, for thermal equilibrium between ions and electrons, the scattering cross section per free electron is just about one-half the classical Thomson cross section. In the more general case, when the electron and ion temperatures (T_e and T_i , respectively) differ, the relationship between the measured cross section σ_m and the classical value σ is given approximately by

$$\sigma_m = \frac{1}{1 + T_e/T_i} \sigma. \tag{8.17}$$

Measurements of σ_m have been made by Bowles at the Jicamarca radar near Lima, Peru, and the results are shown in figure 8.19a. It will be seen that the values are all less than the theoretical value of 5×10^{-29} m². It is believed that during the middle of the day the discrepancy is due to absorption in the D region (approximately 0.5 dB, as shown in figure 8.19b.). On the other hand, near sunrise it is thought that the electrons are in fact hotter than the ions.

8.7.3. Electron Density Profiles

We have seen above that the power received from a given volume in the ionosphere is proportional to the number of electrons present. The incoherent scatter technique thus provides a means of determining the electron density profile above the F_2 peak provided that the geometry of propagation is known. The power p_r received from a distance R is given by

$$p_{\tau} = \frac{p_t a \sigma c \tau \eta_{\tau}^2 \eta_s^2 \eta_A}{8\pi R^2} \,, \tag{8.18}$$

where a is the antenna aperture area,

 σ is the cross section per unit volume,

c is the velocity of light,

 τ is the pulse duration in seconds,

 η_r , η_s , and η_A are factors to correct the aperture for the effects of resistive losses, side lobes, and tapered feed, respectively.

The following features of (8.18) are worth noticing:

- (1) p_r is proportional to R^{-2} rather than R^{-4} as in the case of a single scatterer. From the divergence of the beam it can be seen that the scattering volume increases proportional to the square of the range; this removes a factor of R^{-2} .
- (2) The aperture a appears to the first power only. This is because increased aperture (i.e., increased gain) results in a smaller scattering volume.

Further corrections have to be made to (8.18), depending on the type of antenna used.

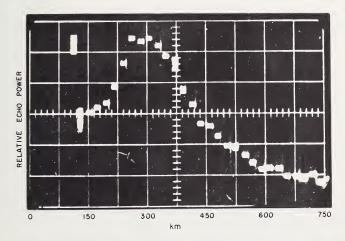


FIGURE 8.20. Oscillogram showing echo power versus range made with scatter radar at Jicamarca, Peru.

(After K. L. Bowles, 1961, J. Res. NBS 65D (Radio Prop.), No. 1, 1.)

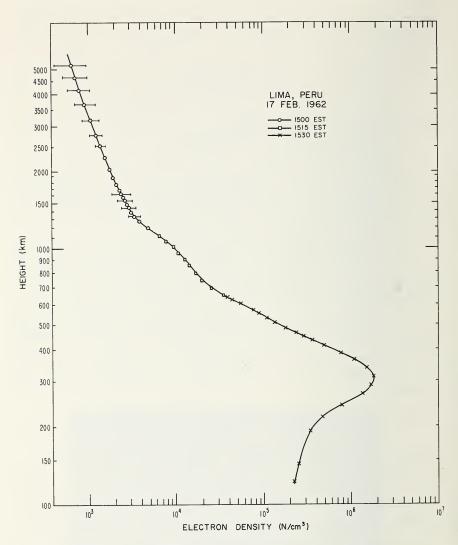


FIGURE 8.21. Electron-density profile obtained from incoherent scatter measurements.

(After K. L. Bowles, Mar. 1963, NBS Tech. Note 169.)

Turning to the experimental results, in figure 8.20 we see an actual oscilloscope photograph made with the radar. Each spot is the result of averaging the echo power taken over many radar sweeps and is thus a plot of power versus range. With a knowledge of the equipment characteristics it is possible to determine the cross section per unit volume σ from (10.18) and, hence, the electron concentration averaged over a cer-

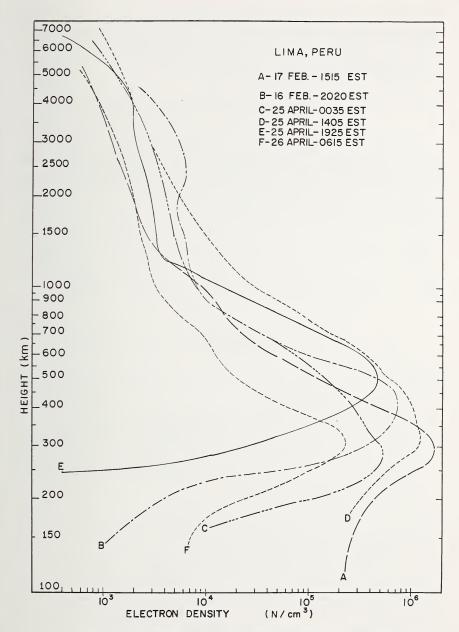


Figure 8.22. Sample electron-density profiles obtained from incoherent scatter measurements.

(After K. L. Bowles, 1964, Radio wave scattering in the ionosphere, Advances in Electronics and Electron Physics 19, 55, Academic Press.)

tain volume and over a given time. A sample profile obtained with this technique is shown in figure 8.21. The curve has to be calibrated at least at one point and this is done at the peak of the F layer. The peak electron density is determined from the f_0F_2 as observed with a conventional ionosonde and substitution in the formula

 $N=1.24\times10^{10}~(f_0F)^2$ electrons per cubic meter.

Further sample profiles are shown in figure 8.22 from which we see that there are rather large variations in the shape of the profiles with time of day and from day to day. The daytime results for heights below about 200 km are probably too large by as much as a factor of two, due to the presence of weak coherent irregularities. At greater heights it has been verified that the echo power is proportional to electron density. One feature of particular interest is the abrupt change in electron-density gradient which often occurs on the topside. This change is probably associated with the changeover in atmospheric composition from one constituent to another (e.g., oxygen to helium or helium to hydrogen).

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CHAPTER 9

Propagation of Low and Very Low Frequency Waves

9.1. PURPOSE

The aim of this chapter is to discuss, briefly, those lower frequency bands which provide alternatives to the use of high frequencies. It has been seen, in the previous chapters, that high frequency propagation is characterized by the following undesirable features:

- (1) Unreliability during ionospheric disturbances.
- (2) Fairly rapid and deep fading.

The chief advantage of high frequencies is the relative simplicity of the terminal equipment required for long-distance communications.

These defects in high-frequency propagation can be largely overcome by the use of low and very low frequencies (LF and VLF). These waves, reflected from the lower boundary of the D layer, are not affected by ionospheric disturbances to the same degree as the HF waves, and are characterized by relatively slow fading rates. The chief disadvantages are the limited usable bandwidths and the relatively large, and hence expensive, transmitter installations which are required.

The VLF spectrum is nominally defined as 3 to 30 kc/s, but the usable band is confined to the range 10 to 30 kc/s. This is largely due to the difficulty in building efficient transmitting antennas for such wavelengths (10 km $<\!\lambda\!<\!30$ km). The propagation is characterized by relatively low path attenuation which is relatively stable with time. This feature, coupled with the fact that VLF energy is guided for long distances (5000 to 20,000 km) between the earth and ionosphere, makes the VLF spectrum attractive for long-distance paths when high reliability is important. In figure 7.10b we saw that the noise on VLF is very high and, as a result, large transmitter powers are required. This fact, together with narrow spectrum available, has resulted in most VLF systems having narrow bandwidths. In addition, the bandwidths of most VLF trans-

mitting antennas are of the order of 20 to 150 c/s and their radiation efficiency is of the order of 10 to 20 percent only.

The low-frequency (LF) spectrum, 30 to 300 kc/s, is characterized by higher path attenuation, lower background noise levels, and more stable propagation time delays relative to VLF. As a result LF systems are usually used for intermediate ranges (1000 to 5000 km). Terminal equipment is usually cheaper than in the VLF case and, in addition, the available bandwidths are greater.

Our primary concern is with the propagation, rather than with the engineering uses, of low and very low frequencies. We shall first discuss some elementary theory and then consider the observational material.

9.2. THEORETICAL CONSIDERATIONS

9.2.1. Ray Theory

The concepts of geometrical ray theory break down in the case of low and very low frequencies because the wavelengths are comparable with the thickness of the D region. However, in some cases, geometrical ray theory is useful for describing certain phenomena. For example, it is convenient to describe the diurnal change $\Delta \phi$ in phase as due to changes in the height of a fictitious reflecting layer, the phase shift on reflection being assumed constant. For example, if h is the mean height of this fictitious layer, Δh the diurnal change in height, 2d the distance between transmitter and receiver, and λ is the wavelength, then

$$\Delta h = \Delta \phi \, \frac{\lambda}{2\pi} \, \frac{\sqrt{d^2 + h^2}}{2h} \,, \tag{9.1}$$

where $\Delta \phi$ is in radians.

9.2.2. Waveguide Theory

9.2.2.1. Meaning of Mode

The propagation of VLF waves between the earth and the ionosphere, over large distances, can be likened to the propagation of microwaves along a waveguide. The "mode theory", as it is called, has been

considered in detail by Budden [1]¹ and Wait [2] and a few simple ideas based on these works will be discussed here.

Let us consider first the meaning of the term "mode." The International Dictionary of Physics and Mathematics (Van Nostrand) defines mode of propagation as follows: "A form of propagation of waves that is characterized by a particular field pattern in a plane transverse to the direction of propagation, which field pattern is independent of position along the axis of the guide."

In this section it shall be assumed that the transmitted waves are vertically polarized, i.e., the electric vectors are vertical. Furthermore, we shall confine attention to *long*-distance propagation where a single mode predominates (see reference [1], sec. 9.13).

9.2.2.2. Basic Concepts

In the simple model shown in figure 9.1, the earth and ionosphere are represented by perfectly conducting planes. With respect to a cylindrical coordinate system (ρ, ϕ, z) , the ground is the plane z=0 and the lower

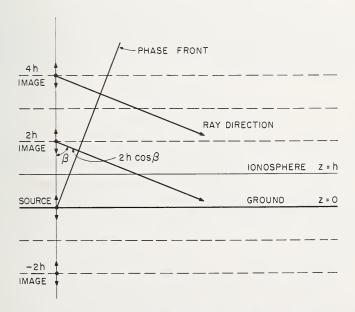


Figure 9.1. Ray geometry corresponding to the first mode between parallel conducting planes.

¹ Figures in brackets indicate the literature references on p. 441.

boundary of the ionosphere is the plane z=h, ρ is the radial coordinate in a horizontal plane and ϕ is the azimuthal coordinate. Let the source be a vertical dipole located on the ground, at the origin. The electric field observed at some other point on the ground is in the vertical direction. To an observer on the ground, the signal would appear to come from the dipole plus a whole series of images in the ground and in the ionosphere [2]. The images are located just below the ground and at $z=\pm 2h,\,\pm 4h$, and so on, as shown in figure 9.1.

Consider the wavelets emanating from the images in the ionosphere. These will reinforce in a direction making an angle β with the vertical (see fig. 9.1) such that

$$2h\cos\beta = 2hC = n\lambda,\tag{9.2}$$

where $C = \cos \beta$, which is a function of the integer n. Thus for a given value of n

$$C_n = \frac{n\lambda}{2h}. (9.3)$$

The ground images will add up at an angle $(\pi-\beta)$ with the vertical. Thus, for a given value of n, there are two families of waves which have the same horizontal component (c/S_n) but which have opposing vertical components of velocity, where

$$S_n^2 = 1 - C_n^2. (9.4)$$

We can imagine the resultant of these two sets of waves as a single wave traveling parallel to the z=0 plane with a phase velocity $v_p=c/S_n$.

Consider the wave directed broadside (n=0). We can imagine this wave to originate in a line source in which the effective uniform current is I_a . Let s be the length of the transmitting dipole carrying a current I. Since images occur as pairs of dipoles all of the same strength (because of the perfect reflectors), and since they are separated by distances of 2h we have

$$I_a = -\frac{s}{h} I. (9.5)$$

The field E_z produced by such a line current is given by [3]

$$E_z = \frac{1}{4}\mu_0 \omega I_a H_0^{(2)}(k\rho) = \frac{1}{4}\mu_0 \omega I h^{-1} s H_0^{(2)}(k\rho), \qquad (9.6)$$

in which $H_0^{(2)}(k\rho)$ is the Hankel function of the second kind with argument $k\rho$, μ_0 is the permeability of free space, ω is the angular frequency, and $k=2\pi/\lambda$. At very great distances, i.e. when $\rho\gg\lambda$, the Hankel function can be replaced by the first terms of its asymptotic expansion, giving

$$E_z = \frac{1}{2} \left(\frac{\mu_0}{\epsilon_0} \right)^{\frac{1}{2}} \frac{Is}{h} (\lambda \rho)^{-\frac{1}{2}} \exp i \frac{\pi}{4} \exp (-ik\rho). \tag{9.7}$$

Note that this field corresponds to the mode obtained by putting n=0 in (9.2). We shall call this, for convenience, the zero-order mode.

Next let us consider the mode produced by the pair of nth images (that is, those located at distances of 2nh above and below ground). Because of the obliquity of the rays the equivalent line current is $I \sin \beta$ (= IS_n). Also the electric field at a point in the plane of the diagram will be perpendicular to the radius vector from the point to the image so that to obtain the vertical component of the electric field we must again multiply by S_n , so that, for the nth mode, the field is given by

$$E_{zn} = 2 \frac{\mu_0 \omega Is}{4h} S_n^2 H_0^{(2)}(k\rho S_n). \tag{9.8}$$

Note that the factor 2 arises because of the two sets of images. For the zero-order mode we have only one set. The resultant field is obtained by summing over all modes for integral values of n from 0 to ∞ . This gives

$$E_{z} = \frac{\mu_{0} \omega Is}{4h} \sum_{n=0}^{\infty} \zeta_{n} S_{n}^{2} H_{0}^{(2)}(k \rho S_{n}), \qquad (9.9)$$

where $\zeta_0 = 1$, $\zeta_n = 2 (n = 1, 2, 3, \cdots)$.

For the far field $(\rho \gg \lambda)$ this expression reduces to

$$E_{z} = \frac{1}{2} \left(\frac{\mu_{0}}{\epsilon_{0}} \right)^{\frac{1}{2}} Ish^{-1}(\lambda \rho)^{-\frac{1}{2}} \exp\left(i \frac{\pi}{4}\right) \sum_{n} \zeta_{n} S_{n}^{\frac{3}{2}} \exp\left(-ik\rho S_{n}\right), \quad (9.10)$$

where $S_n = (1 - C_n^2)^{\frac{1}{2}}$ and $C_n = n\lambda/2h$.

It has been assumed above that the earth and the ionosphere are perfect electrical conductors and that the reflection coefficients of the rays are always +1. In practice, for long-distance propagation the ionosphere behaves more like a perfect magnetic conductor with a reflection coefficient of -1, while the ground still has a reflection of +1. In this case the images are located at $z=2h, \pm 4h$, and so on, but now they alternate in sign. If we write down the resonance condition similar to (9.2)

we must include the reversal of sign of the image which is simply the same as changing the phase by π . Thus,

$$2hC_n = (n - \frac{1}{2})\lambda, \tag{9.11}$$

where n=+1, +2, etc. This shows that there is no zero-order mode (n=0) so that there is no coherent family of waves directed broadside. In this case the corresponding expression for the electric field E_z is

$$E_z = \frac{\mu_0 \omega Is}{2h} \sum_{n=1}^{\infty} S_n^2 H_0^{(2)}(k \rho S_n). \tag{9.12}$$

For great distances this reduces to

$$E_z \simeq \left(\frac{\mu_0}{\epsilon_0}\right)^{\frac{1}{2}} Is(\lambda \rho)^{-\frac{1}{2}} h^{-1} \exp\left(i\frac{\pi}{4}\right) \sum_{n} S_n^{\frac{3}{2}} \exp(-k\rho S_n).$$
 (9.13)

The E field patterns along the direction of propagation are shown in figure 9.2 for the first- and second-order modes when the earth is a perfect electrical conductor (R=+1) and when the ionosphere can be regarded

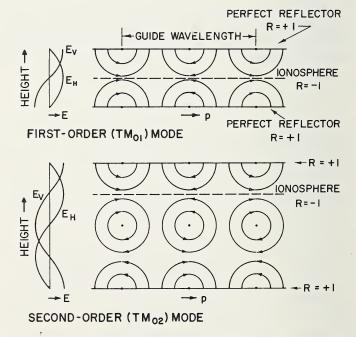


FIGURE 9.2. E field in an idealized earth-ionosphere waveguide.

as a perfect magnetic conductor (R=-1). Since we are dealing with waves polarized in the plane of incidence, the modes are transverse magnetic (TM). When the ionospheric reflection coefficient is -1, the mode pattern can be obtained from the mode pattern of the same order for perfectly conducting boundaries by placing the ionosphere in the plane of the first null in the vertical electric field below the upper perfectly conducting boundary.

We have seen above that the phase velocity v_p in the z-direction is given by

$$v_p = \frac{c}{S_n} \,. \tag{9.14}$$

If we let λ_g be the wavelength in the z direction we have that

$$\lambda_g = \frac{\lambda}{S_n} \,, \tag{9.15}$$

where λ is the free space wavelength. Combining (9.2) and (9.15) we obtain

$$\left(\frac{1}{\lambda_g}\right)^2 = \left(\frac{1}{\lambda}\right)^2 - \left(\frac{n}{2h}\right)^2. \tag{9.16}$$

This shows that, for $\lambda < 2h/n$, λ_g is imaginary and, hence, the mode is evanescent. There is a minimum cutoff frequency f_n below which waves will not propagate where

$$f_n = \frac{nc}{2h} \,. \tag{9.17}$$

The cutoff frequency for n=1 is, therefore, $f_1=c/2h$ and, taking h=75 km for the height of the daytime D layer, we obtain $f_1\approx 2$ kc/s. For the case of a magnetically conducting ionosphere, (9.11) and (9.15) give, for the cutoff frequency,

$$f_n = \frac{(n - \frac{1}{2})c}{2h} \,. \tag{9.18}$$

It will be seen that the change of R from +1 to -1 will change the cutoff frequency (for n=1) from 2 kc/s to 1 kc/s. To be consistent with the mode-numbering system for perfectly conducting electrical walls,

the idealized earth-ionosphere modes should be denoted by $n-\frac{1}{2}$ rather than by n.

9.2.2.3. Modifications for Imperfect Reflection

Equations (9.2) and (9.11) are based on the establishment of a standing wave pattern. This can be interpreted as the condition for a wave to transverse the wave guide, thus suffering reflection at each boundary, and suffer a net phase change of $2\pi n$ radians, thus permitting the twice reflecting wave front to interfere constructively with the original wave front. This condition can be written as

$$R_g(C)R_i(C) \exp(-i2khC) = \exp(-i2\pi n),$$
 (9.19)

in which $R_g(C)$ and $R_i(C)$ are the reflection coefficients of the ground and ionosphere respectively for waves incident at an angle β where $C = n\lambda/2h$. Note that by putting $R_g(C) = R_i(C) = 1$ we obtain (9.2) and by putting $R_i(C) = -1$ we obtain (9.11). In the case where R_g and R_i are not unity it is necessary to solve (9.19) for C_n for each mode and, hence, determine $S_n = (1 - C_n^2)^{\frac{1}{2}}$ for substitution in equations like (9.13). Now, in general, R_g and R_i will be complex so that C_n and S_n will be complex. The wave fields contain the term $\exp(-ik\rho S_n)$ so that when S_n is complex it implies attenuation (see also sec. 2.3.3.3). The absorption index (κ) is given by the imaginary part of S_n , the guide wavelength λ_n is given by

$$\lambda_g = \frac{\lambda}{\text{Re S}_n}, \qquad (9.20)$$

and the phase velocity v_p is given by

$$v_p = \frac{c}{\text{Re } S_n}, \tag{9.21}$$

where Im S_n and Re S_n represent the imaginary and real parts, respectively, of S_n .

The numerical solution of the mode (9.19) is complicated when the reflection coefficients of the earth and of the ionosphere depart from unity, but some solutions have been given by Wait [4]. When signals are propagated over long distances it must mean that the attenuation per unit distance is small and, thus, that the reflectivity of the boundaries must be relatively high. Also the angles of incidence must be large (near

90°). Under these conditions approximate solutions may be obtained as follows:

The Fresnel reflection coefficient R is given by

$$R = \frac{\mu^2 C - \sqrt{\mu^2 - S^2}}{\mu^2 C + \sqrt{\mu^2 - S^2}},$$
 (9.22)

where μ is the refractive index of the reflecting medium. For $\slash\!\!\!/ \text{LF}$ waves in the ionosphere, $\omega \ll \nu$, and thus [2]

$$\mu^2 \approx 1 - \frac{i}{L} = 1 - \frac{\omega_N^2}{\omega_V}$$
 (9.23)

Hence

$$R_i(C_n) = \frac{(L-i) C_n - (C_n^2 L^2 - iL)^{\frac{1}{2}}}{(L-i) C_n + (C_n^2 L^2 - iL)^{\frac{1}{2}}}.$$
 (9.24)

Similarly for the ground

$$R_g(C_n) = \frac{(KG - i) C_n - \{G^2(K - 1) - iG + C_n^2 G^2\}^{\frac{1}{2}}}{(KG - i) C_n + \{G^2(K - 1) - iG + C_n^2 G^2\}^{\frac{1}{2}}},$$
 (9.25)

where $G = \epsilon_0 \omega / \sigma$, $K = \epsilon_e / \epsilon_0$, where ϵ_e and σ are the permittivity and conductivity of the ground.

The value of L for very low frequencies is of the order of unity and, for long distances, C_n is small so that (9.24) reduces to

$$R_i(C_n) \approx -1 - \left[\frac{2(L-i)C_n}{\sqrt{C_n^2 L^2 - iL}} \right].$$
 (9.26)

Note that at great distances it is sufficient to take the first-order mode only.

When the ground conductivity is large, $G \ll 1$ and (9.25) reduces to

$$R_g(C_n) \approx 1 - 2G^{\frac{1}{2}}C_n^{-1} \exp[i(\pi/4)].$$
 (9.27)

Now for low-order modes $C_n^2 \ll L$ and, assuming that L is real, (9.19) can be solved, approximately, using (9.26) and (9.27), which gives

Re
$$S_n = \bar{S}_n + (2\sqrt{2}\pi[(h/\lambda)]\bar{S}_n)^{-1}[(\bar{C}_n)^2(L^{\frac{1}{2}} - L^{-\frac{1}{2}}) + G^{\frac{1}{2}}],$$
 (9.28)

Im
$$S_n = -(2\sqrt{2}\pi[(h/\lambda)]\bar{S}_n)^{-1}[(\bar{C}_n)^2(L^{\frac{1}{2}} + L^{-\frac{1}{2}}) + G^{\frac{1}{2}}],$$
 (9.29)

where

$$\bar{S}_n = (1 - \bar{C}_n^2)^{\frac{1}{2}}$$
 and $\bar{C}_n = \frac{n - \frac{1}{2}}{2h} \lambda$.

These two equations, together with (9.13), determine (approximately) the phase velocities and rates of attenuation of the modes for the simple case of a flat earth and a flat sharply bounded ionosphere, when the effect of the earth's magnetic field is neglected. It should be noted also that finite ground conductivity always affects the phase velocity. The phase velocity is affected also by L except when L=1. The rate of attenuation is a minimum when L=1 and it increases with decreasing ground conductivity. It will be seen also that the higher order modes are more highly attenuated than the first order.

The above presentation is intended to illustrate the application of waveguide theory to VLF ionospheric propagation rather than to develop a quantitatively correct theory. It is defective, as it stands, in two major aspects:

- (1) It neglects earth and ionosphere curvature.
- (2) It neglects the earth's magnetic field.

9.2.2.4. Effect of Earth Curvature

The most important influence of the curvature of the earth is that it prevents the angle of incidence at the ionosphere from becoming grazing while it can become grazing at the surface of the earth. If the radius of the earth is a, the height of reflection is h, and ϕ' and ϕ are the angles of incidence at the ionosphere and at the ground respectively we have, from (4.9), that

$$a \sin \phi = (a+h) \sin \phi'. \tag{9.30}$$

Both the above effects tend to reduce the magnitude of the reflection coefficients of the ionosphere and earth. On the other hand, antipodal focusing (sec. 5.2.4.3) may modify the rate at which the signal amplitude decreases with distance.

A detailed theory of the modifications introduced by the earth's curvature has been worked out elsewhere [3] and a modified mode equation has been derived namely:

$$R_g(C)R_i'(C')\exp\left[-2ik\int_0^h\left(C^2+\frac{2z}{a}S^2\right)^{\frac{1}{2}}dz\right]=\exp\left(-i2\pi n\right),\quad (9.31)$$

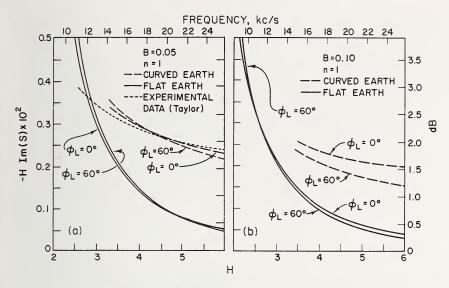


FIGURE 9.3. Attenuation factor as a function of height.

The upper and right-hand scales are specifically for h=70 km, which is a typical daytime height $(B=\lambda L/h)$ (After J. R. Wait and K. Spies, 1960, Influence of earth curvature and terrestrial magnetic field on VLF propagation, J. Geophys. Res. 65, 2325.)

where $C = \cos \phi$, $C' = \cos \phi'$, and z is height. Since (a+h) S' = aS, this reduces to the flat earth equivalent as $h/a \rightarrow 0$. Actually (9.31) is also an approximation and is strictly only valid if $|(ka/2)^{\frac{1}{3}}C| \gg 1$.

A higher degree of approximation has been used by Wait and Spies [5]. Some numerical results of these authors, given in figure 9.3a and 9.3b, indicate that the curvature of the earth can increase the attenuation by a factor of 3 above that calculated on the basis of a plane-earthplane-ionosphere model. Some curves showing the attenuation rate as a function of frequency are given in figure 9.4.

The effect of earth curvature on the phase velocity is of interest in that the velocity is reduced to less than c in most cases of interest as shown in figure 9.5. It will be seen that the effect of the curvature is greatest on the lowest order mode. This is to be expected since the higher order modes involve rays which are less grazing, and the differences between the angles of incidence for the flat- and curved-earth cases becomes smaller as the mode order increases.

Another effect of earth-ionosphere curvature is the efficiency with which a given mode can be launched into the waveguide (see page 221 of reference 2). For ionosphere heights of the order of 70 km and for fre-

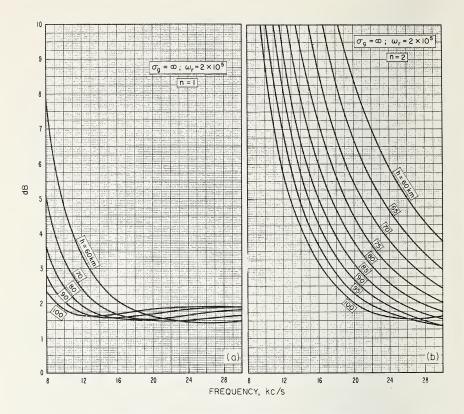


FIGURE 9.4. Attenuation rate as a function of frequency.

(After J. R. Wait and K. Spies, 1960, Influence of earth curvature and terrestrial magnetic field on VLF propagation, J. Geophys. Res. 65, 2325.)

quencies less than 16 kc/s, there is little difference but, for higher frequencies or greater heights, the excitation of the first mode becomes relatively weak. However, in a few cases the excitation factor may be greater than unity, particularly for the higher order modes.

9.2.2.5. Effect of the Earth's Magnetic Field

The chief effect of the earth's magnetic field is to make the ionosphere an anisotropic medium (see ch. 2). A wave polarized in the plane of incidence (E vector in the vertical plane) gives rise to two reflected waves and two transmitted waves. One of each of these is polarized in the plane of incidence, while the others are polarized normal to this plane (i.e.,

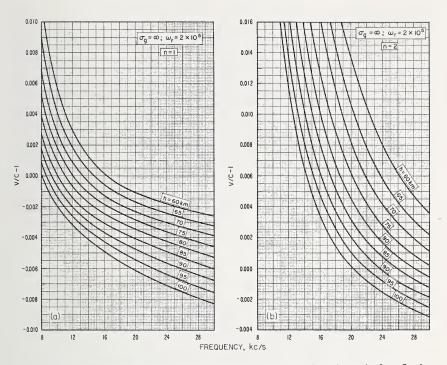


Figure 9.5. Phase velocity for a perfectly conducting earth and an imperfectly reflecting ionosphere.

(After J. R. Wait and K. Spies, 1960, Influence of earth curvature and terrestrial magnetic field on VLF propagation, J. Geophys. Res. 65, 2325.)

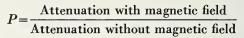
horizontally). Thus, a vertically polarized wave incident on the ionosphere gives rise to a horizontally polarized component which, after a ground reflection and another ionospheric reflection, gives rise to further vertically and horizontally polarized waves. This results in polarized modes which are "coupled." However, the degree of coupling is usually small and will be ignored in this book.

In principle, the ray properties of VLF signals in the ionosphere can be determined from the complex refractive index (2.76). It is much more convenient, however, to use the quasi-longitudinal and quasi-transverse approximations (sec. 2.3.3.2), retaining the collision term.

In order to take into account the double refraction in the ionosphere, it is convenient to use the two reflection coefficients $_{||}R_{||}$ and $_{\perp}R_{\perp}$ together with two conversion coefficients $_{||}R_{\perp}$ and $_{\perp}R_{||}$. The first subscript denotes whether the electric field of the incident wave is parallel (| |)

to or perpendicular (\bot) to the plane of incidence and the second subscript refers to the same characteristic in the reflected wave.

For details of the calculations of these reflection coefficients the interested reader can start with chapter IX of reference [2] and follow up the references given therein. It will be sufficient for our present purpose to note how the attenuation and phase velocity is affected by the inclusion of the earth's magnetic field. Some results for the first-order mode are shown in figures 9.6 and 9.7 for attenuation and phase velocity respectively for a real angle of incidence of 82°, for various dip angles I, and with different directions of propagation ϕ_a (measured clockwise from the north). The attenuation results are presented in terms of the ratio [2]



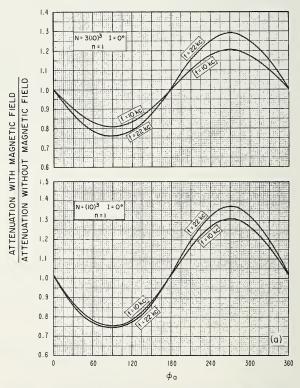


Figure 9.6. Ratios of attenuation (with and without the magnetic field) as a function of azimuth.

(After J. R. Wait and K. Spies, 1960, Influence of earth curvature and terrestrial magnetic field on VLF propagation, J. Geophys. Res. 65, 2325.)

and, in figure 9.6, P is plotted for various dip angles and frequencies of 10 kc/s and 22 kc/s. In all these curves the electron density N is 10^3 per cm³, $\nu = 2 \times 10^7 \text{ sec}^{-1}$, and the strength of the earth's field is 0.5 G.

When the azimuth ϕ_a is 0° (propagation towards the north) or 180° (to the south) the magnetic field has little effect on the attenuation. For east-west and west-east propagation P departs significantly from unity. The effect becomes less noticeable as I approaches 90°. The effect of the magnetic field on the phase velocities of VLF waves is relatively small.

One feature, which is evident in both figures 9.6 and 9.7, is the non-reciprocity in P, and in velocity, for $\phi_a=90^\circ$ and 270°. The difference in P has been observed experimentally [6, 7] and the physical explanation involves the action of the transverse field component on the motion of the ionospheric electrons in the plane of incidence [6, 8]. These electron motions should not be confused with those giving rise to the ordinary

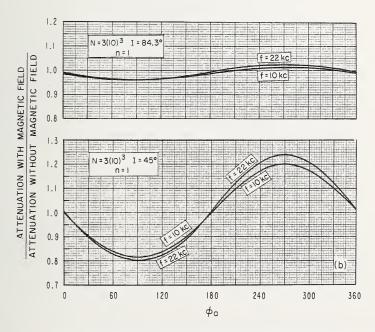


Figure 9.6b. Ratios of attenuation (with and without the magnetic field) as a function of azimuth.

(After J. R. Wait and K. Spies, 1960, Influence of earth curvature and terrestrial magnetic field on VLF propagation, J. Geophys. Res. 65, 2325.)

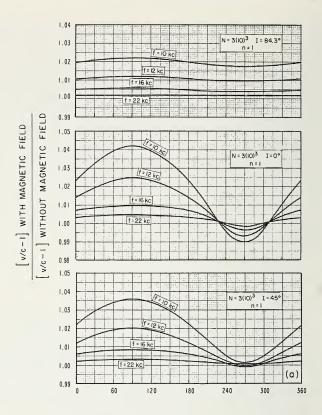


FIGURE 9.7a. Differences between phase velocities (with and without the magnetic field).

(After J. R. Wait and K. Spies, 1960, Influence of earth curvature and terrestrial magnetic field on VLF propagation, J. Geophys. Res. 65, 2325.)

and extraordinary waves which are in the plane transverse to the direction of propagation. It is important to notice that the results shown in figure 9.7 refer to a particular model and the results may be entirely different with a different model.

9.2.2.6. Modes and Rays on Very Low Frequencies

The question frequently arises as to (a) the relationship between mode and ray (or geometrical-optical) theories, and, sometimes, (b)

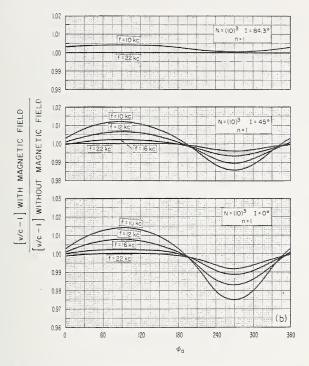


FIGURE 9.7b. Differences between phase velocities (with and without the magnetic field).

(After J. R. Wait and K. Spies, 1960, Influence of earth curvature and terrestrial magnetic field on VLF propagation, J. Geophys. Res. 65, 2325.)

whether one is more correct than the other.

It has been shown [9] that for the case of propagation between perfectly reflecting parallel planes, the series expansions based on ray and mode theory are related by a Fourier cosine transform. This suggests that, provided all modes and all rays are taken into account with appropriate corrections for losses, the results from both methods will be the same as has been demonstrated [10]. In fact the derivation of the mode formula given earlier is based on the ray approach. It is not uncommon, however, for a ray model of VLF propagation to be used which considers just one ray, reflected several times between earth and ionosphere, from the trans-

mitter to the receiver. A single ray model is satisfactory only at short distances.

The appropriate question to ask, then, is which method of calculation is simplest. On VLF, the wavelength and height of the ionosphere are such that only a few modes are important since the higher-order modes are attenuated at a much greater rate than that of the lowest mode. At great distances only one mode need be considered. In this case, however, many rays have to be considered. On the other hand, at short distances all propagating modes are comparable in amplitude and must be considered. Only a few rays need to be considered, however, since the higher-order rays are incident at smaller angles of incidence where the reflection coefficient is decreasing rapidly.

On higher frequencies (in the LF band) and at long distances many modes may be important, and the attenuation coefficients of many of the less attenuated modes may be comparable. Thus there is less advantage in using mode theory. Wait [10] has given an account of ray theory for use at LF which takes account of the curvature of the earth, showing how the rays which are identifiable inside the horizon behave as the horizon is passed.

9.2.2.7. Effect of lonospheric Stratification

It has been assumed that the ionosphere is a sharply bounded, semi-infinite medium. This is only a first approximation because what little evidence we have suggests that the D layer is not sharply bounded. It has been found [2, 3, 11, 12] that a two-layered model is necessary to explain the observed attenuation rate in the frequency range from 500 c/s to 1.5 kc/s. For frequencies in the range 8 kc/s to about 20 kc/s, however, the sharply bounded model is convenient for a simple description of what must be a complicated reflection process. Extensive justifications for the idealized model have been given recently by Wait and Walters² in a series of four papers dealing with the reflection of VLF waves from inhomogeneous ionospheric models.

² Wait, J. R., and L. C. Walters (1963), Reflection of VLF radio waves from an inhomogeneous ionosphere, Parts I, II, III, and IV, J. Res. NBS 67D, and (1964) Radio Science.

9.2.3. Ionospheric Coupling on Low Frequencies³

In our discussion of the propagation of waves in a magneto-ionic medium (ch. 2) we assumed that the ordinary and extraordinary waves are propagated independently. While this is substantially true on high frequencies, it is not so on low frequencies. Experimental studies have shown that the echo structure of low-frequency pulses is more complicated than that on high frequencies. One of the most interesting effects is known as coupling [13], which has been studied extensively at the Pennsylvania State University on a frequency of 150 kc/s at night.

Coupling may be thought of as arising in the following way. In the case of long waves, propagation in an inhomogeneous medium must be considered. It is no longer possible to consider a purely progressive wave, because each point in the medium gives rise to a forward and a backward wave, and these two waves must be taken into account in describing the propagation. Furthermore, the component magneto-ionic waves no longer propagate independently; hence coupling occurs not only between magneto-ionic components but also between the progressive wave of one component and the backward wave of the other. For a detailed description of the propagation, a full wave theory is required. It has been shown [13] that when the level X = 1 occurs near the level where $\nu = \nu_c = \omega_H \sin^2 \theta / \cos \theta$, strong coupling can occur. This level depends on the strength and direction of the magnetic field and on the collision frequency profile $\nu(h)$. The sketch in figure 9.8 indicates, schematically, the reflection processes for long waves, including the possibility of coupling. Above the base of the ionosphere (where X=0), the two circularly polarized ordinary and extraordinary waves travel independently with different speeds. Near the level where coupling can occur, the upgoing extraordinary wave gives rise to a backscattered ordinary wave and to a progressive ordinary wave in addition to the progressive extraordinary wave. This progressive extraordinary wave is known as the "whistler mode." Similarly the upgoing o wave gives rise to a backwards x wave. These backward-moving waves combine to produce a downcoming coupling echo. The polarization of the coupling echo should be fairly constant, since the backscattering o and x waves should be in proportion. This is, in fact, observed. The polarization of the coupling echo is roughly constant and the same as

³ This section is taken verbatim from a lecture by Dr. J. S. Belrose.

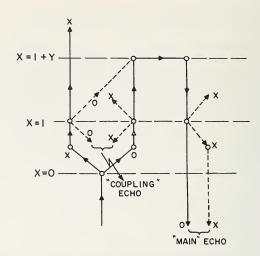


FIGURE 9.8. Sketch to illustrate the mechanism of reflection of LF waves from the ionosphere.

(After J. S. Belrose, 1964, unpublished.)

that transmitted. However the amplitude would depend markedly on how closely the X=1 level approaches the $\nu=\nu_c$ level.

A second effect of coupling is concerned with the polarization of the main echo. The upgoing x wave, in the region of coupling, gives rise to a forward-scattered o wave, which combines with the forward progressive o wave, and proceeds to the level X=1+Y, where it is reflected. Now, when this downcoming o wave reaches the coupling level, it generates a forward-scattered x wave which, when combined with the progressive o wave below this level, alters its polarization. In fact the resulting polarization ellipse, in the presence of strong coupling, may have its major axis outside the magnetic north-east south-west quadrants, that is, in a direction "forbidden" by simple magneto-ionic theory.

If the bottom of the ionosphere is "rippled" and these ripples pass over the level where $\nu=\nu_c$ so as to change the X=1 level from below to above the "critical coupling" level, we would expect that the polarization could change rapidly [14]. This phenomenon has been observed by the Pennsylvania State University workers, who have called it "flip-overs," i.e., the polarization of the "main echo" can change from right-handed to left-handed depending on whether $\nu <$ or $> \nu_c$ at the level where X=1, and in the case of "critical" coupling the polarization of the downcoming wave may be in the pair of "forbidden" quadrants mentioned in the previous paragraph.

"Coupling" effects, where studied, namely at Pennsylvania State University, are strongest on frequencies near 150 kc/s at night. No day-time coupling effects have been observed, but if they were, the effect should be strongest for waves of frequency between 300 and 500 kc/s.

9.3. SOURCES OF VERY LOW FREQUENCY SIGNALS

9.3.1. Atmospherics

The majority of the energy in the VLF band comes from radiation due to lightning discharges (see sec. 7.2.2.2), which are called atmospherics. A typical discharge radiates about 5×10^4 joules [15, 16]. A large part of this energy is radiated in the VLF band, with peaks near 10 kc/s. The transmitted waves are mostly vertically polarized and the field strengths produced by these discharges can be as great as several volts/meter at short distances. The energy level, at the receiver, is generally greatest between sunset and midnight and tapers off to a broad minimum after sunrise.

9.3.2. Manmade Signals

These generally originate in transmitters with Morse code or pulsed CW carriers, and are spread through the range from 10 to 25 kc/s. Radiated powers vary from a few kilowatts to more than a megawatt, and the signals are vertically polarized.

Another type of manmade radiation comes from nuclear explosions in the atmosphere.

9.3.3. VLF Signals Associated with the Exosphere

These signals are generated within or are propagated along paths in the outer atmosphere. The length of such a path may amount to 30,000 or 50,000 km. Whistlers [17] are generated in lightning discharges and are guided along the earth's magnetic field to conjugate points. VLF emissions, chorus, hiss, etc., are believed to originate in the exosphere.

9.4. PHASE VARIATIONS ON VERY LOW FREQUENCIES

9.4.1. Method of Observing Phase Changes

This is, essentially, described in section 3.2.3.1. For short distances, up to about 200 km, the groundwave provides a suitable reference signal because it can be separated from the skywave signal [19]. For longer distances, the reference signal has to be transmitted by some other means, e.g. telephone line [20]. Both the above methods have the advantage that the actual frequency transmitted need not be very stable. This is not the case when a local reference oscillator is used. The latter is required for distances greater than about 200 km because of the difficulty of separating the groundwave from the skywave.

9.4.2. Regular Diurnal Changes Over Short Distances

It was pointed out above that an incident wave, polarized in the plane of incidence, will, after reflection, be elliptically polarized. This reflected wave can, therefore, be resolved into two components:

- (a) the normal component, polarized in the plane of incidence;
- (b) the abnormal component, with its electric vector horizontal.

The abnormal component can be observed by the use of a loop antenna set with its plane perpendicular to the plane of propagation. The normal component can be observed by means of a loop in the plane of propagation. In the latter case, the groundwave signal induced in the loop has to be cancelled by means of a signal received on a vertical whip antenna [21, 22].

In studies of the diurnal variations of phase, it has been found convenient to describe them in terms of changes Δh of height h of a fictitious mirror reflector. If the ground distance is 2d and the wavelength is λ , then

$$\Delta h = \Delta \phi \, \frac{\lambda}{2\pi} \, \frac{\sqrt{d^2 + h^2}}{2h} \,, \tag{9.32}$$

where $\Delta \phi$ is the diurnal phase change in radians.

The diurnal variation in the phase of WWVL (on 20 kc/s) over a 113 km path near Boulder, Colo., is shown in figure 9.9. The phase curves are dish-shaped with the deepest depression centered near local noon. The

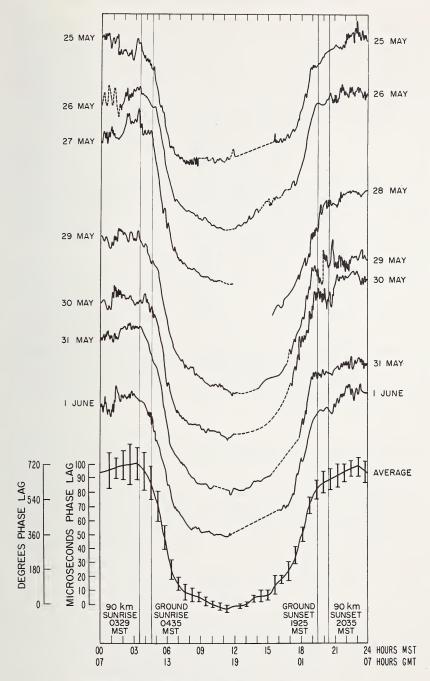


FIGURE 9.9. The diurnal variation of phase of WWVL.

(After C. J. Chilton, D. D. Crombie, and A. G. Jean, 1963, Phase variations in VLF propagation, AGARDograph 74, 257, Pergamon Press.)

diurnal phase shifts in May 1961 were approximately 720°, corresponding to a height change of about 18 km. This result agrees well with similar observations in England [19] over a 90 km path. There, on 16 kc/s, phase changes varying from 430° in November to 600° in June were observed, which correspond to height changes of 13 km and 18 km respectively. The English results showed also that the effective height of reflection $h(\chi)$ varied in a Chapman-like manner (see (1.29)), namely:

$$h(\chi) = H_0 + H \sec \chi, \tag{9.33}$$

provided that $\chi < 85^{\circ}$. Here h_0 is the effective height if the sun were overhead, and H is the scale height of the atmosphere (sec. 1.2) at the height of reflection. It was found that the mean value of h_0 was about 69 km and that the values of H varied from 4 km in June and January to about 7 km in October and April with a mean value of around 5.5 km.

Observations of the abnormal component over a distance of 540 km [23] showed that the diurnal change starts about 1 hr before ground sunrise at the path midpoint, whereas at 90 km the change commences about 10 min after ground sunrise. Over this distance (540 km), the phase change reaches a maximum value near ground sunrise and then decreases for about 2 hr thereafter. This phase reversal, together with a much smaller one occurring during the main phase change (neither being observed over 90 km), are thought to be due to reflections from different D layers [24]. It is possible, however, that these effects may be due to interference between multiple rays or modes.

9.4.3. Regular Diurnal Changes Over Long Distances

In these experiments, it is necessary to use a local reference oscillator and allowance must be made for oscillator drift. When this is done, it is found that, on an east-west path, the diurnal variation of phase commences some half hour before sunrise at the eastern terminus and continues smoothly until just before sunrise at the western terminus [25]. The relative phase then remains constant until about a half hour after sunset at the eastern terminus when a smooth transition of nighttime conditions sets in. This trapezoidal diurnal variation is illustrated in figure 9.10. It must be remembered that this trapezoidal representation is highly idealized and, in practice, the diurnal pattern undergoes considerable variation from day to day and from season to season.

Observations of the phase of the GBR (Rugby, England) signal in New Zealand [26] can be explained in terms of the times at which the

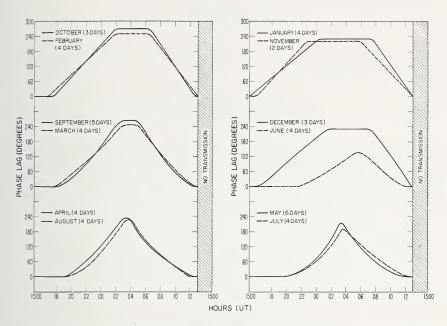


Figure 9.10. Diurnal variation of phase of the GBR (Rugby, England, 16 kc/s) signal received in Boulder, Colo. (7400 km).

(After C. J. Chilton, F. K. Steele, and R. B. Norton, 1963, Very-low-trequency phase observations of solar flare ionization in the D region of the ionosphere, J. Geophys. Res. 68, 5421.)

sunrise or sunset line crossed the nearly north-south path, and the angle between these lines and the path. It is necessary to assume that the height changes suddenly from its daytime to its nighttime value at the time of sunset and vice versa at sunrise. The magnitude of the phase change can be explained in terms of a waveguide mode theory provided that the ionosphere is treated as a magnetic conductor [27]. To a first approximation, it has been shown [27] that the phase velocity v_p in a curved earth-ionosphere waveguide is given by

$$v_p{\approx}c\left\{1-\left(\frac{(n-\frac{1}{2})\lambda}{2h}\right)^2\right\}^{-\frac{1}{2}}\!\!\left(1-\frac{h}{a}\right)\!,$$

so that for the first-order mode (n=1) we have

$$v_p \approx c \left(1 - \frac{\lambda^2}{16h^2}\right)^{-\frac{1}{2}} \left(1 - \frac{h}{a}\right)$$
 (9.34)

$$pprox c \left(1 - rac{h}{a} + rac{\lambda^2}{32h^2} + ext{smaller terms}
ight).$$

If the height h changes by an amount Δh , the corresponding phase change $\Delta \phi$ is given by

$$\Delta \phi = -\frac{2\pi d}{\lambda} \left[\frac{h}{2a} + \frac{\lambda^2}{16h^2} \right] \frac{\Delta h}{h} \text{ rad}, \tag{9.35}$$

in which d is the great circle distance of the receiver from the transmitter and h is the mean height of reflection. Using this equation it has been shown [27] that the diurnal height change (day to night) is about 16 km. Curves showing the phase velocity as a function of reflection height and wave frequency have been shown in figure 9.5. As a particular path is crossed by a day/night boundary, the relative phase seen at the receiver will depend on the relative amounts of the path which are in daylight and in darkness at the instant concerned. If d_0 and d_n are the distances in daylight and darkness, and β_0 and β_n are the respective phase changes per unit length, the total phase lag ϕ_t between transmitter and receiver is given by

$$\phi_t = d_0 \beta_0 + d_n \beta_n = d_0 (\beta_0 - \beta_n) + \beta_n d. \tag{9.36}$$

For an east-west path this gives the trapezoidal variation noted above while for a north-south path they may tend to pass quickly from daylight to night giving a rectangular variation as illustrated in figure 9.11.

9.4.4. Influence of Geographical Location

The diurnal curves shown in figures 9.10 and 9.11 show up the effect on the phase of paths in high latitudes. The GBR-Boulder path lies in much higher latitudes than the NBA (Panama)-Boulder path. If one considers ground sunset and sunrise, the GBR-Boulder path becomes completely dark during June, but this is not reflected in the June curve. If we consider, however, sunset and sunrise at the level of the D region, then we see that the path never really becomes dark and, thus, we should not expect the full diurnal variation to develop. Examination of the diurnal phase changes during the months for which the path does become completely dark suggests that there is a seasonal change in the diurnal phase shift. In December and January, the mean phase change is 210° while in March it is 260°.

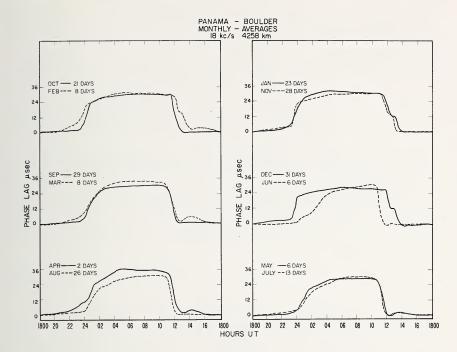


Figure 9.11. Diurnal variation in the phase of NBS (Panama, 18 kc/s) signals as received in Boulder, Colo.

(After C. J. Chilton, F. K. Steele, and R. B. Norton, 1963, Very-low-frequency phase observations of solar flare ionization in the D region of the ionosphere, J. Geophys. Res. 68, 5421.)

Some observations of the relative phase of GBR as measured in Point Barrow, Alaska (6000 km) are shown in figure 9.12. This is a very northerly path and, ignoring the effect of flares, etc., it is seen that the diurnal phase shift ($\approx 30^{\circ}$) is small. When allowance is made for the fact that two-thirds of the path is illuminated, the observed phase change represents an effective height change of 13 km for that portion of the path which changes from daylight to dark.

It is useful to note at this point that a phase change $\Delta \phi$ is sometimes measured in terms of a time delay Δt by the formula

$$\Delta t = \frac{\Delta \phi}{\omega} \,. \tag{9.37}$$

It should be remembered that Δt is not the change in transmission time since the latter usually refers to group propagation time (see sec. 2.4.2).

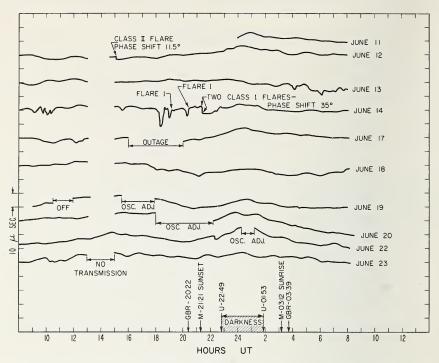


Figure 9.12. Relative phase of GBR (Rugby, England, 16 kc/s) signals at Point Barrow, Alaska.

(After C. J. Chilton, D. D. Crombie, and A. G. Jean, 1963, Phase variations in VLF propagation, AGARDograph 74, 257, Pergamon Press.)

9.4.5. Determination of Phase Velocity

The measurements, over long distances, of the diurnal variation of phase do not permit a determination of the actual phase velocity.* The latter requires the determination of the absolute phase change of a signal as it travels between points separated by a known distance. This in turn requires an independent link between the two points having a known phase shift.

Wait [28] has examined such experimental results and finds that the data fit waveguide theory if the reflection height is taken to be 70 km during the day and 90 km at night. Even better agreement is obtained when allowance is made for the finite conductivity of the ionosphere. These data, as given by Wait, show that on 10 kc/s the phase velocity is approximately equal to the free space velocity c during the night, while

^{*} See Steele, F. K., and C. J. Chilton (1964), The measurement of the phase velocity of VLF propagation in the earth-ionosphere waveguide, Radio Sci. J. Res. NBS/USNC-URSI 68D, 1269.

during the day it is approximately 0.3 percent higher than c. On 14 kc/s, the phase velocity is approximately equal to c during the day and about 0.2 percent smaller at night. On 16 kc/s the phase velocity is approximately 0.3 percent and 0.1 percent less than c by night and by day respectively.

9.4.6. Effects of Meteors

Effects attributed to meteors have been observed both on VLF [29] and on LF [30]. On VLF the effect is observed on the GBR-Boulder path as a delay in the onset of the sunrise advance of phase until the meteor shower has passed or until the entire path has become sunlit, at which time the phase returns to the normal daytime value. On low frequencies the diurnal phase curve is also unsymmetrical during meteor showers.

9.4.7. Effects of Solar Flares

In section 6.2.2, we mentioned the effect on VLF waves of a solar flare. These sudden phase anomalies build up rapidly (1 to 5 min) and recover slowly (30 min to 3 hr). The magnitude of the phase shift is related to the increase in the flux of the solar radiation, its angle of incidence at the ionosphere and to the length of the circuit over which a lowering of the apparent reflection height occurs. Phase shifts of 30° to 60° are common for flares of importance 2.

Certain large flares which produce polar cap absorption events (sec. 6.1) produce also unusually large phase changes. A phase advance of 240° occurred on the GBR-Boulder circuit on May 4, 1960. Such events are, however, relatively rare; about 10 were observed during 1960, for example. The larger sudden phase anomalies indicate changes in effective height of the order of 18 km whereas more moderate height changes are 7 km or less. There is no simple relationship between the optical importance of flares and their ionizing effects in the ionosphere.

9.4.8. Effects of Magnetic Disturbance

9.4.8.1. Sudden Commencements

Phase advances have been observed during magnetic sudden commencements on paths which traverse a certain range of geomagnetic

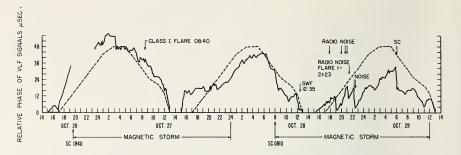


FIGURE 9.13. Effect of magnetic disturbance on the phase of GBR received at Boulder, Colo.

(After C. J. Chilton, D. D. Crombie, and A. G. Jean, 1963, Phase variations in VLF propagation, AGARDograph 74, 257, Pergamon Press.)

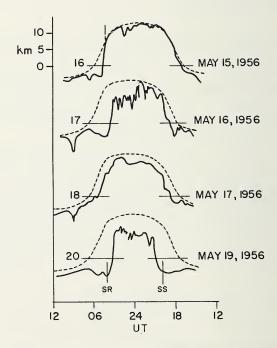


Figure 9.14. Observations of the phase height of 16 kc/s waves observed at Cambridge during an ionospheric storm.

May 15 is a normal day; May 16-17, the primary storm effects; May 19-20, the aftereffect. The dashed curve represents the expected variation in the absence of a disturbance. (After J. S. Belrose, The oblique reflection of low-frequency waves from the ionosphere, AGARDograph 74, 151, Pergamon Press.)

latitudes in the vicinity of 65° north. Such a phase advance is shown in figure 9.13.

9.4.8.2. Magnetic Storm Effects

The great fluctuations in the phase of GBR (fig. 9.13) on October 29, 1961 are typical of the VLF effects which accompany a severe magnetic storm. The effects on VLF waves are predominantly night effects and consist of rapid and deep fading during the main phase of the storm (primary effect). The phase of 16 kc/s with steep incidence is particularly susceptible to storms. This is shown in figure 9.14 for a transmission distance of 90 km. The dotted line indicates the mean diurnal variation of phase for the month. The storm began about 0400 UT on May 16 and was, essentially, over by about midday on May 17. Reference to the figure shows that a disturbance effect was, by and large, not detected until the night of May 16-17; even though the magnetic field was greatly disturbed during the day of May 16, no marked effect was observed until near sunset. Large and rapid variations of phase occurred during the night of May 16-17. These phenomena constitute the primary storm effect. The phase returned to near normal on May 17-18 but, beginning on May 19, the diurnal phase pattern took a form very different from normal. After this day, a gradual recovery set in over three days.

9.5. AMPLITUDE VARIATIONS ON VERY LOW FREQUENCIES

9.5.1. Reflection Coefficients

Experimental determinations of the reflection and conversion coefficients ($_{||}R_{||}$ and $_{||}R_{\perp}$) have been made in England [19, 21, 22, 23]. The measurements were obtained on a pair of crossed vertical loops in and perpendicular to the plane of incidence. The first loop responds to the sum of the groundwave signal and the component of the electric field parallel to the plane of incidence while the second loop responds to the horizontal (abnormal) component. On the assumption that the groundwave is constant, its amplitude and phase can be determined from a sufficient number of observations. The numerical results are summarized in table 9.1. These measurements suggest considerable variability of reflection coefficient with season and with angle of incidence, in addition to the diurnal variation.

Table 9.1. Measurements of reflection coefficient (16 kc/s)

| Observers | Ionospheric incidence angle | Refl. type | Coeff. mag | Season and time |
|---|--|--|--|---|
| Best et al. [21] Best et al. Budden et al. [22] Budden et al. Bain et al. [23] Bain et al. Straker. [19] Straker. Straker. Straker. | (deg) 30 30 36–60 36–60 75 70 30–45 30–45 30–45 30–45 | R R | 0.25 0.50 0.12 0.08 0.27 0.55 0.13 0.26 0.56 0.37 | Summer day Winter night Autumn day Autumn day Summer day Summer night Summer day Winter day Summer night Winter night |

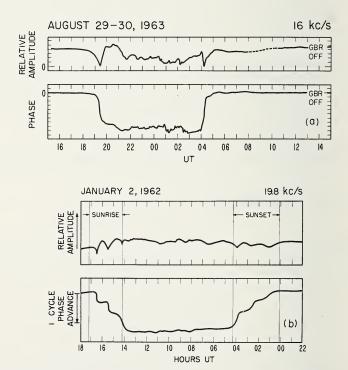


FIGURE 9.15. Diurnal variation of the amplitudes and phases of VLF signals.

(a) Short distances: Rugby, GBR-Frankfurt (840 km). (After A. G. Jean, unpublished.) (b) Long distances: Hawaii, NPM-Boulder (5374 km). (After D. D. Crombie, unpublished.)

9.5.2. Amplitude

The resultant amplitude of a VLF signal propagated over short distances is highly variable due to interference between the various components and particularly between the ground wave and the once reflected signal. For a given distance, the amplitude is very sensitive to the magnitude and phase of the reflection coefficients, and to the height of reflection.

This sensitivity is seen in the diurnal variation where the night-to-day ratios are around 6 dB in CW signal strength and as much as 20 dB in the level of broadband sferics. In addition, rapid changes of amplitude occur near sunrise and sunset along the path. The amplitude usually goes rapidly through a minimum or maximum before reaching its steady daytime or nighttime level—see figure 9.15.

Changes in the usual pattern of the field behavior are introduced by such factors as a land-sea boundary or changes in ground characteristics. At these boundaries standing wave patterns are set up which modify the field distribution over distances of several wavelengths.

9.5.3. Attenuation Rate

The variation with distance of the vertical field E of the far field in a waveguide mode is given [31], approximately, by

$$E = \frac{300}{h} \left[\frac{P\lambda}{a \sin d/a} \right]^{\frac{1}{2}} \exp(-\alpha d). \tag{9.38}$$

P is the radiated power (kilowatts), α is the attenuation rate, and the other symbols have their usual meanings. Expressing (9.38) in decibels we have [31]

$$20 \log E + 10 \log \sin (d/a) = a \operatorname{constant} - \alpha d, \qquad (9.39)$$

where α is in decibels per unit distance (usually 1000 km) and all the other factors are lumped together in the constant. If, therefore, the left hand side of (9.39) is plotted against d the slope of the resulting straight line will give the value of α .

Observations on signals from VLF stations have been made by Heritage et al. [32] on frequencies of 16.6 kc/s and 18.6 kc/s. An example is shown in figure 9.16. These data give an attenuation rate of 3.0 dB per thousand kilometers.

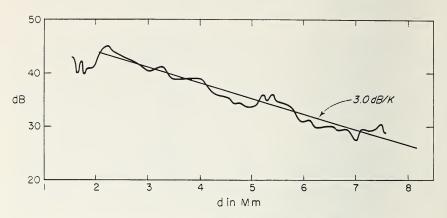


FIGURE 9.16. Experimental data showing attenuation rate over the Pacific.

(After J. L. Heritage, S. Weisbrod, and J. E. Bickel, 1947, A study of signal versus distance data at VLF, VLF Symposium Record 4, 77.)

The value of α over the North Atlantic averages around 3 dB per 1000 km on frequencies near 20 kc/s. The night values are consistently lower than the day values. A typical land path increases the attenuation rate by about 3 dB per 1000 km compared to that over sea water. Paths over the Arabian Sea and the Indian Ocean show rates of about 2 dB per 1000 km at great distances. The result of daytime measurements [32] in the Pacific give average rates as 1.7 dB per 1000 km.

Observations on sferics by Taylor show that the best conditions for a signal of frequency between 15 and 20 kc/s occur for west-to-east propagation (sec. 9.2.2.5) over sea at night. The rate under these conditions is a minimum and is about 1.0 dB per 100 km. The maximum attenuation for this frequency range occurs for a land path from east to west during daylight and is about 3.5 to 4.0 dB per 1000 km.

In general, propagation in the 15 to 20 kc/s frequency range over land adds about 1.0 to 1.5 dB per 1000 km to the sea water value. Daytime propagation adds about 1.0 dB per 1000 km to the nighttime value. The nonreciprocity causes about 1.0 dB per 1000 km more attenuation for east-west propagation as compared with west-east propagation. There is some evidence which indicates that attenuation is higher in the auroral zone and over large expanses of ice such as Greenland (A. G. Jean, private communication).

9.5.4. Polarization

Over short distances (100 to 300 km) the skywave is essentially circularly polarized, that is, the ratio $_{||}R_{\perp}:_{||}R_{||}$ is approximately unity with a 90° phase shift. At longer distances (500 to 800 km), the polarization is approximately linear with $_{||}R_{||}$ being much larger than $_{||}R_{\perp}$. For distances over 1000 km, it appears that the polarization is essentially vertical during the daytime and that this changes to an elongated ellipse (10:1 axis ratio) at night. The polarization is highly variable during disturbed conditions for short and medium distances. Little is known, in general, about polarization for long distances.

9.6. PHASE VARIATIONS ON LOW FREQUENCIES

9.6.1. Normal Behavior Over Short Distances

Experimental data obtained by Belrose [33] indicates that the heights of reflections of waves, in the frequency range 70 kc/s to 245 kc/s, are roughly the same as those of VLF waves. For transmission distances of the order of 1000 km the heights of reflection change from about 90 km by night to about 72 km by day as sketched in figure 9.17. It will be seen also that the reflecting layer is closely controlled by the sun. When these frequencies are transmitted over shorter distances (less than about 300 km) they appear to be reflected at somewhat higher heights, namely 80 to 85 km by day and 90 to 100 km by night.

9.6.2. Normal Behavior Over Long Distances

When LF waves are propagated over distances of 2000 km and greater, the diurnal variation of phase is quite different from that for distances of around 1000 km and less. This is seen in figure 9.18, where the trapezoidal shape of the curve is emphasized by the dashed line. The fact that the phase changes during daylight are independent of solar zenith angle χ has led to the suggestion that the height of reflection (zero phase) is less than 70 km (probably around 65 km). Note that the phase of LF signals appears to be highly variable at night over most paths. It is important to remember that the deductions about the height of reflection are made on the assumption that the one-hop signal predominates

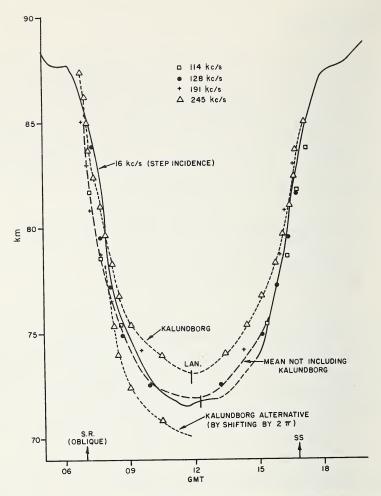


Figure 9.17. Diurnal variation of the height of reflection of low-frequency waves, February 1955.

(After J. S. Belrose, unpublished.)

at all times. Some doubt has been cast on this assumption by pulse observation on 100 kc/s [34].

9.6.3. Effects of Solar Flares

The effects on LF observed during an SID are similar to those on VLF (sec. 9.4.7). In fact, it is found that the lowering of the apparent

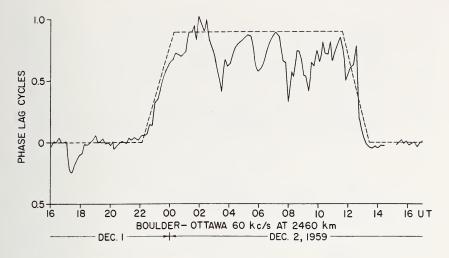


Figure 9.18. The diurnal phase variation, on December 1-2, 1959, of 60 kc/s waves received at Ottawa from Boulder (2400 km).

(After J. S. Belrose, 1963, The oblique reflection of low-frequency radio waves from the ionosphere, AGARDograph 74, Pergamon Press.)

height is much the same for all waves in these bands for both long and short [35] distances. Large flares (of importance 3) may drop the apparent reflection height to 60 km, but no reflections have yet been observed from lower heights.

9.6.4. Polar Cap Disturbances

These disturbances are associated with certain large solar flares and occur primarily in geomagnetic latitudes greater than about 60°. Along with polar cap absorption (sec. 6.4.), LF propagation disturbances occur. The latter may last from 5 to 15 days during which the phase height is less than normal, principally at night.

9.7. AMPLITUDE VARIATIONS ON LOW FREQUENCIES

9.7.1. Normal Behavior Over Short Distances

The morning variation of amplitude is illustrated in figure 9.19. It is characterized by successive maxima and minima. It has been shown

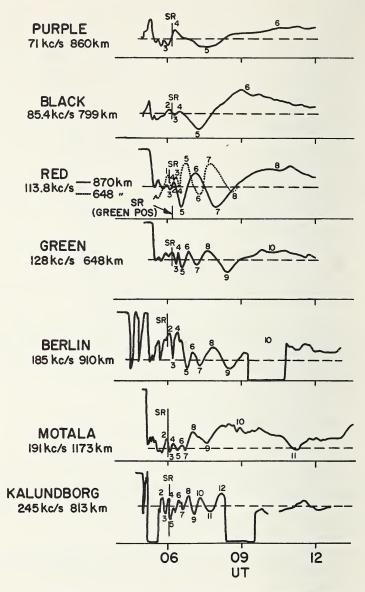


Figure 9.19. Amplitude variation of an LF signal over a distance less than 1000 km, Berlin-Cambridge.

(After J. S. Belrose, unpublished.)

[33] that, by starting at midday and working back towards sunrise, these maxima and minima can be explained in terms of the interference between a single skywave, the amplitude of which decreases with time of day, and the groundwave. If this analysis is continued earlier than ground sunrise, the results are no longer consistent and it is necessary to assume that more than one skywave is present. It appears unlikely that the additional skywave is the two-hop signal because of the small magnitude of the reflection coefficient.

9.7.2. The Reflection Coefficient

The variation of $_{||}R_{||}$ with the equivalent vertical frequency ($f\cos\phi$, where ϕ is the angle of incidence) is sketched in figure 9.20 for the months of November 1954, March 1955, and June 1955. Except in the case of

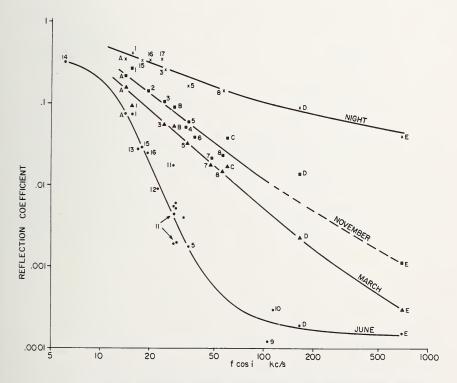


Figure 9.20. Variation of reflection coefficient ||R|| with equivalent frequency.

(After J. S. Belrose, The oblique reflection of low-frequency radio waves from the ionosphere, AGARDograph 74, 1963.)

June, the variations are essentially linear. It should be noted that, for short distances, since the downcoming wave is approximately circularly polarized, the reflection coefficient $_{||}R_{||}$ and the conversion coefficient $_{||}R_{||}$ are essentially equal. On the whole, the data from which figure 9.20 was constructed refer to sunspot minimum years.

Detailed studies [36] on waves of frequency 245 kc/s over a distance of 180 km have shown that the difference in attenuation between sunspot maximum and sunspot minimum is a function of solar zenith angle. There is a maximum difference in attenuation of 15 dB at $\chi = 70^{\circ}$. Monthly mean values of $\log_{11}R_{11}$ at constant χ are closely related to sunspot number

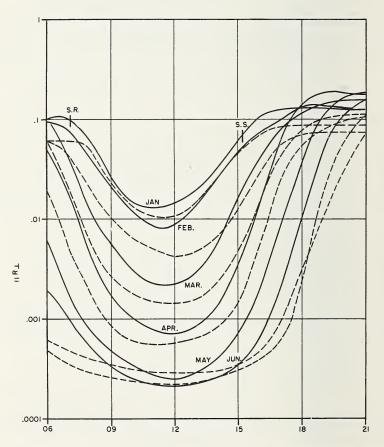


Figure 9.21. Diurnal variation of $||R_{\perp}|$ for 245 kc/s over a distance of 180 km for 1954 (solid line) and 1956 (broken line).

(After J. S. Belrose, unpublished.)

up to a value of 150 above which there is little change. This "saturation" effect is also evident in the monthly mean curves of figure 9.21 giving the diurnal variation of $_{11}R_{\perp}$ (plotted from data in ref. [37]). In winter and equinox months there is a difference in attenuation over the whole of the day. In summer the ionospheric absorption, during a year of high sunspot number, reaches a maximum soon after sunrise. This maximum is about the same as the midday value during a sunspot minimum year.

There is some evidence that suggests that the sunspot cycle effect on LF waves is opposite to that on VLF waves. Thus 16 kc/s waves are more strongly reflected at sunspot maximum than at sunspot minimum whereas on 245 kc/s the reverse appears to be true. The magnitude of the difference depends on the sunspot number and, in part, on the season (for instance on 245 kc/s a difference is found for equinoctial and winter months only) and is about 3 to 6 dB. On intermediate frequencies the effect will be less.

9.7.3. Normal Behavior Over Long Distances

9.7.3.1. Diurnal Variation

The diurnal variation of the amplitude of waves of frequency 97 kc/s propagated between Ottawa and Goose Bay in Canada (1500 km) is shown in figure 9.22.

In summer the diurnal variation of amplitude is very regular and, to a first order, symmetrical about local noon. In winter the daytime amplitude is greater, and much less regular and the equinox months are erratic. Deep fluctuations are present near dawn. In these records the groundwave is negligible in comparison with the total skywave so that the fluctuation is due probably to the beating between two waves reflected from different heights.

9.7.3.2. Seasonal Variation

The seasonal variation of the signal strength on 80 kc/s over the 1910 km path from Ottawa to Churchill is shown in figure 9.23a. This shows the usual seasonal trend with winter signals stronger than the summer ones. The seasonal variation of the signal strength in the case of 70.4 kc/s waves over the 1700 km path from Comfort Cove, Newfoundland, to Ottawa is opposite to that obtained for all other transmissions as can be seen in figure 9.23b.

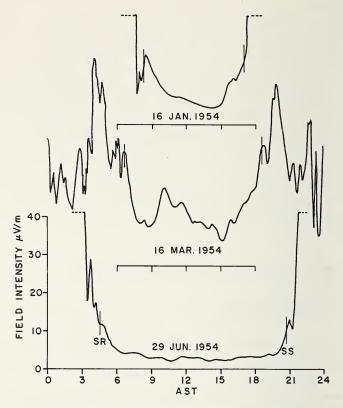


Figure 9.22. Diurnal variation of total field intensity received on a loop antenna at Goose Bay for 97.1 kc/s transmissions from Ottawa (1 kW radiated).

(After J. S. Belrose, unpublished.)

9.7.4. Effects of Solar Flares

The detailed variation of amplitude during a SID depends on the conditions prevailing prior to the disturbance and so depends on the season. On the whole, however, it appears that on LF the amplitude increases during a flare, whereas on VLF and for steep incidence, the amplitude decreases as illustrated in figure 9.24.4 It can be seen that the

⁴ Note that with oblique incidence there is only a small amplitude change, and this is usually an increase.

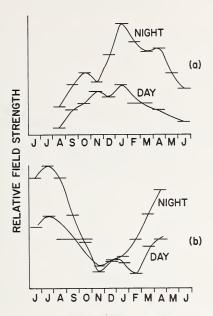


FIGURE 9.23. Seasonal variation of monthly median midday and midnight values of total field intensity.

(a) Ottawa-Churchill (80 kc/s). (b) Comfort Cove—Ottawa (70.384 kc/s). (After J. S. Belrose, unpublished.)

change in height of reflection is essentially the same on both frequencies. The detailed time sequence usually takes the form of a rapid decrease of amplitude at the beginning followed by an increase at the time of maximum disturbance and a second decrease before the final recovery—as shown by the 16 kc/s curve in figure 9.24. On some occasions, however, the "subsidiary" peak may be smaller than the initial decrease of amplitude. On the whole it appears, that the magnitude of the subsidiary peak is such as to result in an overall increase in summer and an overall decrease in winter.

The amplitudes of low-frequency waves in the range 60 kc/s to 80 kc/s transmitted over distances of 1700 to 2400 km (in North America) always increase during an SID.

9.7.5. Polar Cap Disturbances

The effects of a sudden cosmic ray event (SCR) on the propagation of LF waves in high latitudes are as follows:

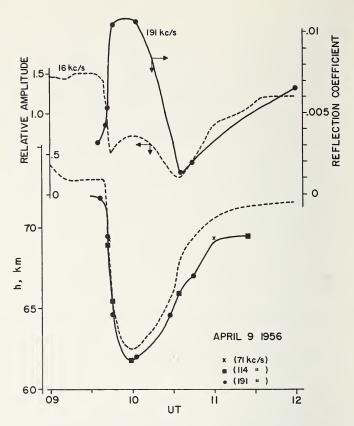


FIGURE 9.24. Estimated reflection heights and amplitudes observed at Cambridge (April 9, 1956) during a SID.

(After J. S. Belrose, 1963, The oblique reflection of low-frequency radio waves from the ionosphere, AGARDograph 74, Pergamon Press.)

- (1) When the SCR is weak the ionospheric effects can usually be detected by means of LF waves in high geomagnetic latitudes only. The disturbance effect is mainly one of weaker than normal signal strengths at night and nighttime reflection heights which are lower than normal.
- (2) When the disturbance is moderate, the diurnal variation of signal strength is opposite to that normally observed. The diurnal change of apparent reflection height is less than normal, and the greater reduction occurs at night.
- (3) When the polar cap disturbance is strong the diurnal variation of both phase and amplitude disappears almost entirely. The apparent reflection heights are some 10 to 12 km below the normal daytime values

(i.e., the waves may be reflected from heights between 50 and 55 km). The signal strengths are about the same as those on a normal day.

9.7.6. Magnetic Storm Effects

The behavior of LF waves during magnetic storm in middle latitudes has been summarized by Lauter [38] as follows:

- (1) The sudden commencement was not associated with any change of amplitude;
- (2) at night, rapid and deep fading accompanied the main phase of the storm (primary storm effect);
- (3) daytime records were not usually disturbed during the main phase of the storm;
- (4) when the storm was intense the signal strength during the night was unduly weak for a period which began about 3 to 4 days after the start of the storm and continued for several days (the after effect).

9.7.7. Nocturnal Anomalies [33, 38]

At night it is not uncommon to observe phase and amplitude anomalies lasting for about an hour or so. Both phase and amplitude changes occur together. The phase anomalies always correspond to a decrease in apparent height. Although they are somewhat similar to sudden phase anomalies, they frequently start more gradually. The decrease in apparent height can be as great as 8 to 10 km, which is the size of a normal SPA. Furthermore, there is evidence to indicate that these nocturnal anomalies have spatial extents of at least 600 km.

Nocturnal anomalies are associated sometimes with magnetic variations, but not always. They are found both in middle and high latitudes and are usually accompanied by other "auroral" type phenomena such as enhanced forward scatter of VHF signals, HF absorption, and so on.

9.7.8. The Winter Anomaly

During winter days of high absorption on HF (sec. 3.3.6.5), low-frequency waves appear to be reflected from heights lower than normal and the amplitude of waves transmitted over distances of 1000 to 2000 km is greater than normal. When these waves are propagated over short

distances their amplitudes may be greater or less than normal but, when the HF absorption is intense, their amplitudes are usually greater than normal.

9.7.9. Variation of Amplitude With Distance

9.7.9.1. Short Distances

At distances less than 100 km the variation is dominated by interference between the groundwave and the skywave. If the amplitude of the vertical electric field is measured on the ground, or in an airplane flying at a constant height, and allowance is made for the inverse distance attenuation, a pattern of the type shown in figure 9.25 is obtained. This pattern is called the Hollingworth pattern. From the positions and signal strengths of the turning points it is possible to deduce the characteristics of the downcoming wave.

9.7.9.2. Long Distances

Some idea of the decrease of amplitude with distance can be obtained from figure 9.26 which is based on data for 180 kc/s waves over land

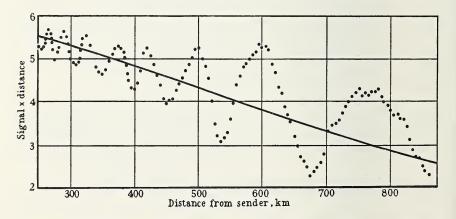
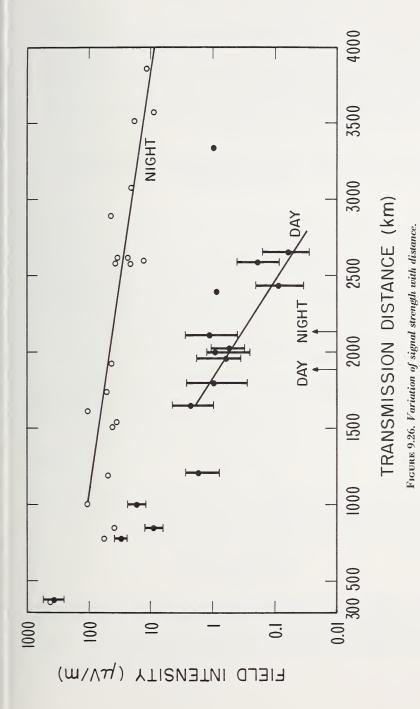


Figure 9.25. The Hollingworth interference pattern observed during the midday hours on 85 kc/s on November 3, 1949.

The full curve represents the calculated groundwave signal. (After R. N. Bracewell, K. G. Budden, J. A. Ratcliffe, T. W. Straker, and K. Weeks, 1951, The ionospheric propagation of low-frequency radio waves over distances less than 1000 km, Proc. IEE 98, Pt. III, 221.)



(After J. S. Belrose, W. L. Hatton, C. A. McKerrow, and R. S. Thain, 1959, The engineering of communications systems for low radio frequencies, Proc. IRE 47, 661.)

[43]. The following features are worthy of note:

- (1) At the geometrical limits of the one-hop path (\approx 2000 km) there is no sharp drop in signal strength. This is in agreement with waveguide theory.
- (2) The amplitudes fall off approximately exponentially with distance both by day and by night.

(3) The amplitudes are greater by night than by day.

(4) The attenuation rate is somewhat greater by day than by night.

9.8. USE OF VERY LOW FREQUENCIES IN FREQUENCY COMPARISONS

The relatively high phase stability of VLF signals propagated over long distances makes it possible to transmit reference frequencies to remote parts of the world. For this purpose, the frequency of the transmitter must be stabilized by means of a stable crystal oscillator or preferably an atomic standard. Under these conditions the limitation on the accuracy to which a received frequency can be measured is determined by

- (a) the relatively high atmospheric noise [39] and
- (b) the phase fluctuations due to ionospheric changes [40].

Frequency is essentially the time rate of change of phase (i.e., $d\phi/dt$). It can be shown that if N and C are the rms noise and signal powers respectively, then the standard deviation of phase $\sigma(\phi)$ is given by

$$\sigma(\phi) = \frac{N}{C}.\tag{9.40}$$

If n cycles are observed in a time (T) the error in n is $1/2\pi\sigma(\phi)$ and thus the rms error E in the frequency (f) measurement is

$$E = \frac{1}{n} \frac{\sigma(\phi)}{2\pi} = \frac{1}{2\pi} \frac{N}{C} \frac{1}{fT}.$$
 (9.41)

Now the noise power N is proportional to the bandwidth (b) of the receiving system, which can be made small (e.g., 0.01 c/s) by suitable instrumentation [41]. Using such a system, a precision of 1 part in 10^9 has been achieved in an hour's observations over a distance of 19,000

km. From this it will be seen that atmospheric noise will rarely be the limiting factor.

The effect of ionospheric height changes is more serious because the variations are so slow and, thus, long averaging times are required. If the phase of a VLF signal relative to that of a local oscillator changes by an amount ϕ in a time T, then the angular frequency difference $\Delta \omega$ is given by

$$\Delta\omega = \frac{\phi}{T} \,. \tag{9.42}$$

If $\sigma(\phi)$ is the standard deviation in the fluctuations of ϕ , the precision of the frequency measurement will be

$$\sigma(\omega) = \frac{\sigma(\phi)}{T} , \qquad (9.43)$$

provided that the phases at the beginning and end of the measurement are uncorrelated. Thus the precision increases linearly with the time of observation. Pierce gives values of $\sigma(\phi)$ for GBR-Boston (16 kc/s) of 0.28 rad for quiet nights and 0.14 rad by day. For GBR-Boulder the day value of $\sigma(\phi)$ is 0.26 rad. The natural limit of frequency comparison over a north-Atlantic path is about 2 parts in 10^{11} for a 24-hr period [42].

9.9. USES OF VERY LOW AND LOW FREQUENCIES

The main uses of VLF are

- (1) Long-distance communications (on-off keying),
- (2) Continuous-wave navigation systems,

and of LF,

- (3) Broadcasting (e.g., Droitwich, 200 kc/s),
- (4) Communications (on-off keying and frequency shift-keying),
- (5) Continuous wave navigation systems (e.g., Decca),
- (6) Pulse navigation and timing systems (e.g., Loran C, 100 kc/s).

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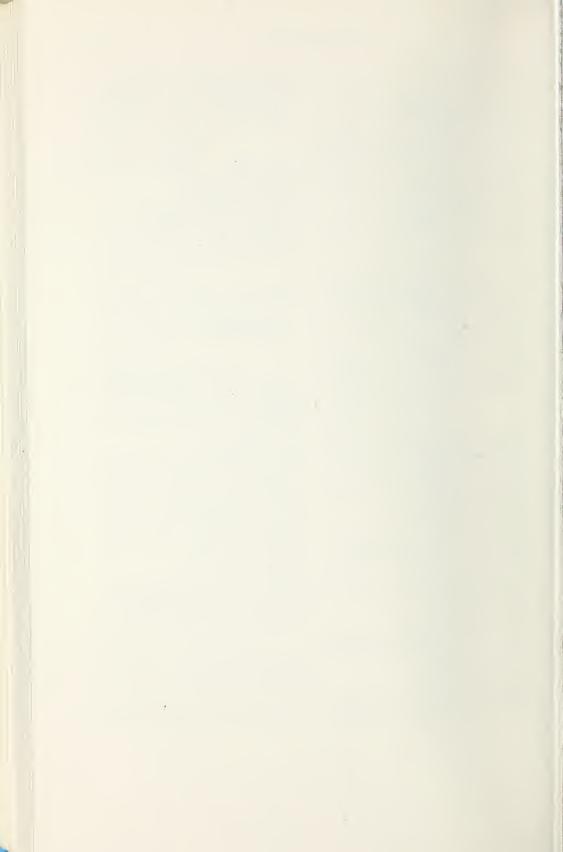
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IONOSPHERIC RADIO PROPAGATION BY KENNETH DAVIES

Errata as of December 17, 1965

| Page | | Correction |
|-------|------------------------------------|---|
| 12 | Equation (1.15) (c) | XA tin place of XY tin place of XY |
| 13 | Equation 1.18 | h ∫ Nodh ∞ |
| 13 | Equation 1.19 | $\int\limits_{\infty}^{h}$ |
| 14 | Equation 1.23 | $\int_{h}^{\infty} N dh = = = \frac{\sigma NT}{mg}$ |
| 17 | Equation 1.34 | N_{\max}^2 |
| 22 | Figure 1.6 | is incorrect (F isosurfaces should be rotated through 90°) |
| 25 | Figure 1.8 (title) | (1) should be (I) |
| 7+7+ | | Kuper should be Kuiper in 13, 15, 18. |
| 58 | Equation 2.42 | $\frac{v}{\mu_0}$; should be $\frac{1}{v\mu_0}$ |
| 62 | Line 6 | WB/m^2 not Wb/cm^2 |
| 70-71 | Equations 2.73, 2.74, and 2.76 | Extend root sign to include $4Y_{ m L}^2$ |
| 74 | Figure 2.9 (b) | Curve through $X = 1$ should be o. Curve through $X = 3$ should be x. (Interchange o and x) |
| 76 | Line ll | Use small "c" on Budden ref. Bracket at end of sentence. |
| 79 | Figure 2.11 (a) Figure 2.11 (b) | 3 should be on left. 3 should be on left. |
| 80 | Equation 2.95 | - before χ |
| 84 | Equation 2.103 | Nv not N_v . v not subscript, should be as in 2.98. |
| 85 | Figure 2.14 (a) Figure 2.14 (b) | 3 on left 2 on top, 3 on left. |



| Err | ata as of December 17,1965 - | IONOSPHERIC RADIO PROPAGATION |
|-------|------------------------------|--|
| 86 | Table 2.1 (title) | should be same as equation (2.105) on page 88. |
| 92 | Figure 2.16 | Insert "nearly" between of and equal |
| 126 | Figure 3.13 | Defence spelled with c (Norwegian) |
| 137 | Figure 3.199 | One "t" in Britannic |
| 160 | Figure 4.1 | Insert letter C at midpoint of TR |
| 161 | Line 17 | Parentheses within parentheses, remove inner set. |
| 162 | 5th line from bottom of page | Expression for $h_{_{\!$ |
| 162 | Equation 4.6 | $P'(f) = 2 h'(f_V) \sec \phi_0$ |
| 163 | Equation 4.7 | Smudge on parentheses |
| 172 | Line ll | Insert "analytically" after determined. |
| 175 | Figure 4.12 | Time should be 2112 not 2012 |
| 178 | | Pedersen |
| 179 | Figure 4.18 Figure 4.19 | One "t" in Britannic |
| 182 | Figure 4.22 (caption) | Add, [Sterling-St.Louis, 1150 km, 0957 (75°WMT) May 15, 1962] |
| 195 | Figure 4.34 | Replace ϕ with i, as in equation 4.18. |
| 206 | Figure 4.43 | One "t" in Britannic |
| 208 . | Figure 4.45 | Redraw |
| 220 | Equation 5.4 | Add a term Laa, antenna aperture loss |
| 231 | Line 7, 9 | Parentheses within parentheses, remove inner set. |
| 233 | Figure 5.12 | hg - 80 km should read h_{D} = 80 km (2 place |
| 257 | Line 8 | Should read, (see section 1.7.2) |
| 258 | Line 6 | Same as above |
| 262 | Line 24 | Section 3.2.3.2 not 2.5.3, add "and the theory is given in section 2.5.3". |



| Errata | as | of | December | 17, | 1965 | _ | IONOSPHERIC | RADIO | PROPAGATION |
|--------|----|----|----------|-----|------|---|-------------|-------|-------------|
|--------|----|----|----------|-----|------|---|-------------|-------|-------------|

| 285 | Line 2 | Parentheses within parentheses, remove inner set. |
|------|------------------------------|---|
| 298 | Figure 7.6 | This nomogram is based on the equation $L = \frac{615.5 \text{ n sec } \phi \text{ [l + .0037R][cos .881 \chi]}^{1.3}}{(\text{f + f}_{\text{H}})^{1.98}}$ n = number of reflections. Note that it is inaccurate for frequencies less than about 5 Mc/s. |
| 304 | Figure 7.9 (a) | Title should read 1800 UT not 0800 |
| 313 | Figure 7.10 (b) & (c) | Abscissas should be labeled Mc/s. |
| 325 | Line 10 | Change $E_S \simeq$ to $E_S \approx$ |
| 329 | Figure 7.19 (b) & (c) | Insert figure title. Abscissas should be labeled Mc/s. Should be consistent with figure 7.10. |
| 342 | | Jasik not Josik |
| 360 | Line 9 | (10.8) should read (8.8) |
| 388 | Last line | (10.18) should read (8.18) |
| 401 | Line 5 | V smudge |
| 413 | 2nd line under section 9.3.1 | (see sec. 7.2.2) should read (see sec. 7.5.1) |
| 4,47 | | Chapman layer, reference to page 34 should be page 134. |
| 449 | | E layer note repetition |
| 452 | | Under height phase repeated, real or true split. |
| 457 | | Pedersen |
| 466 | | Hefley not Hefly |
| 466 | Last Line | Kuiper not Kuper |
| | | |



